

ERL  
2013



## Analysis of Injection and Recovery Schemes for a Multi-turn ERL based Light Source

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1. Introduction
2. ERL as a light source
  - a) Single-turn scheme with direct injection
  - b) Single-turn scheme with a preinjector
  - c) Multi-turn scheme with a preinjector
3. BBU instability and Linac optics for different schemes
4. Summary:
  - a) Comparison of the results
  - b) Rough estimation/comparison of costs

# Projects with ERLs

MESA @  
MAINZ

HZB Helmholtz  
Zentrum Berlin

Cornell ERL

eRHIC @ BNL

BERLinPro,  
FSF @ HZB

ERL FEL @  
BINP

MEIC @ JLAB

LHeC @ CERN

SINAP





- high average current
- technologically mature
- energy efficient



- low emittance is possible
- low energy spread is possible
- long undulators
- short pulses

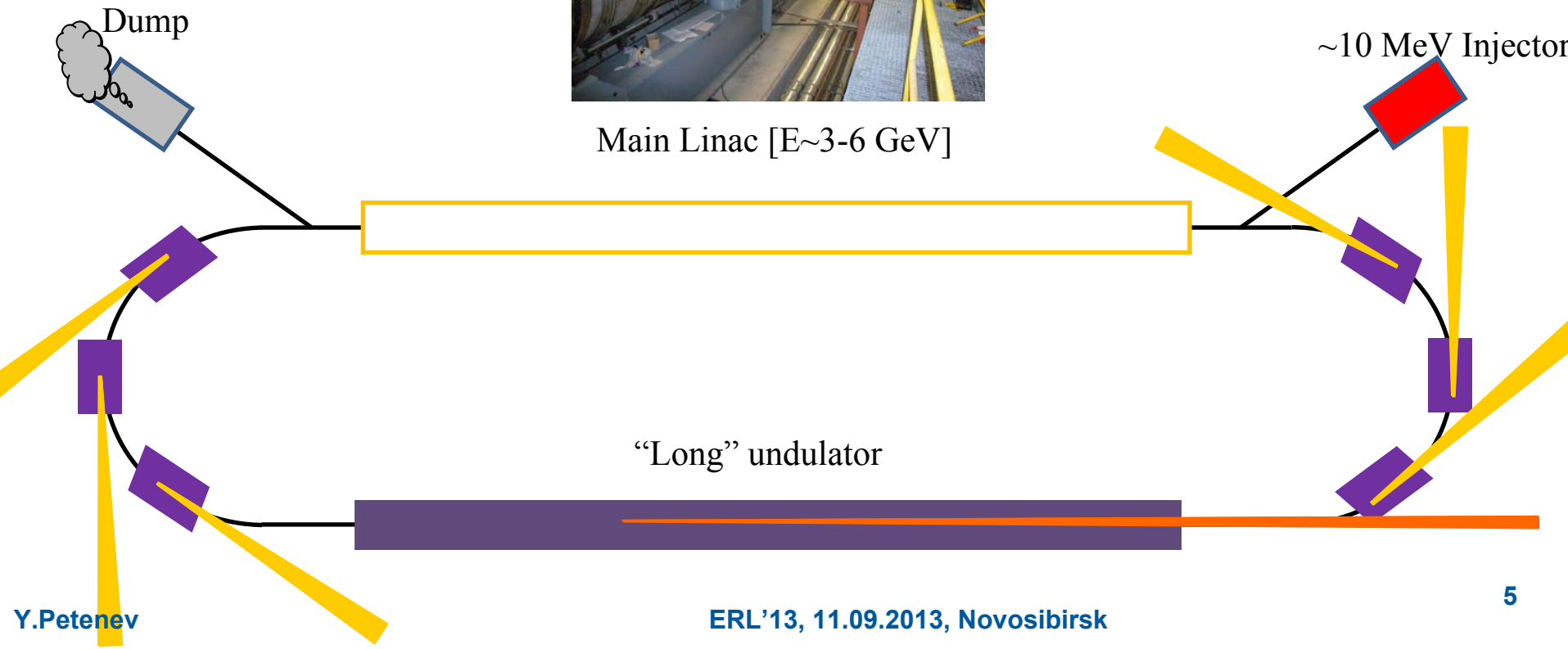


- high average current
- technologically mature
- energy efficient



Main Linac [ $E \sim 3-6$  GeV]

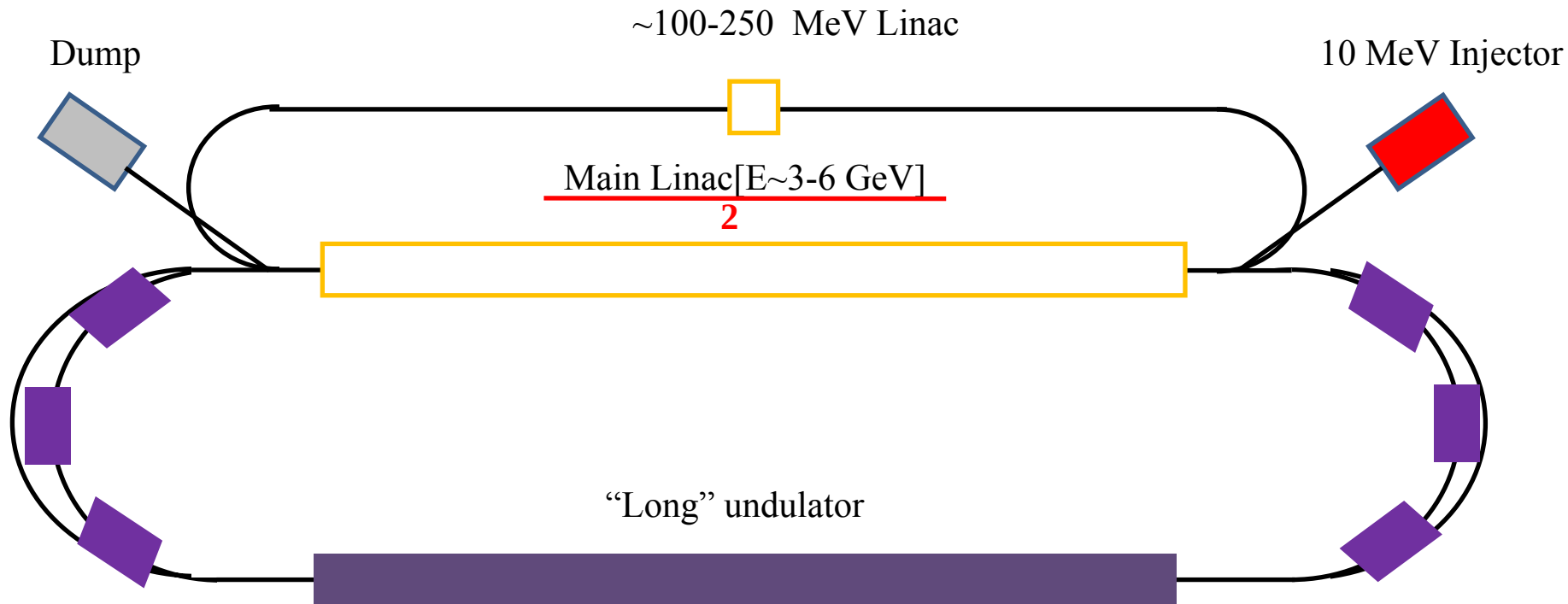
- low emittance is possible
- low energy spread is possible
- long undulators
- short pulses



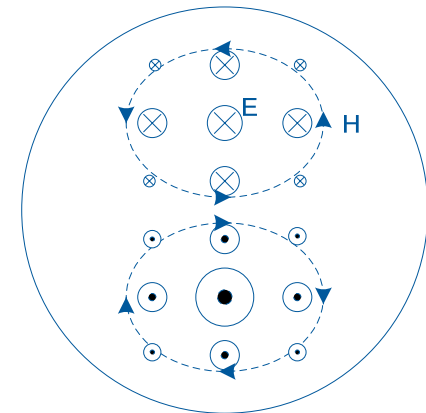
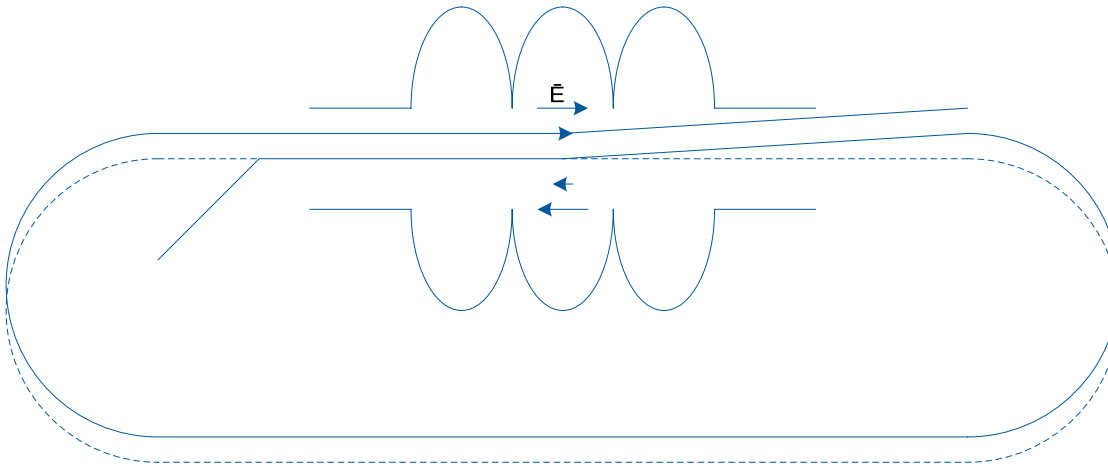
Like storage ring +  
✓ low emittance  
✓ low energy spread  
✓ long undulators  
✓ short pulses

or

Like linac +  
✓ high average current  
✓ energy efficient

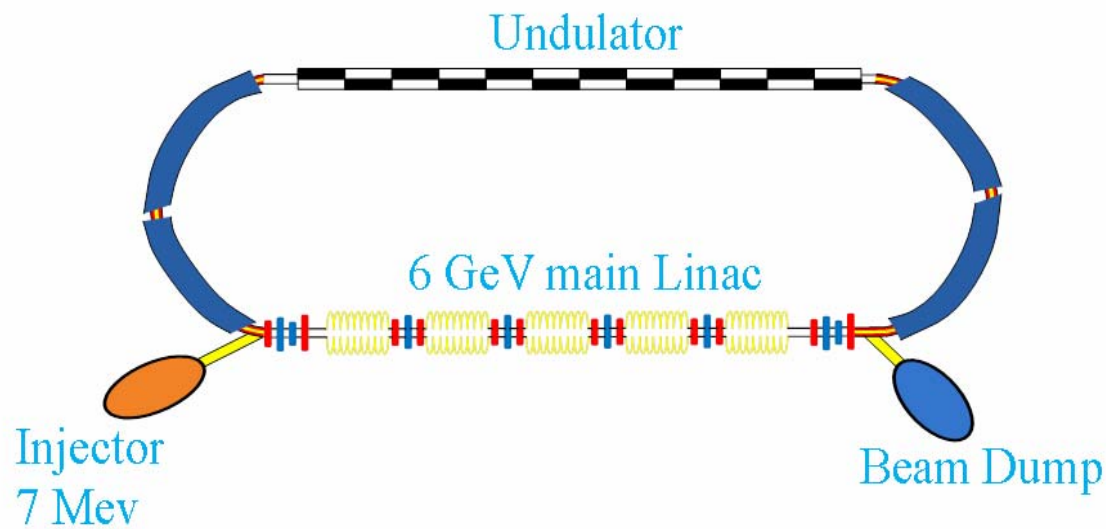


- Each of a high order dipole modes in a cavity deflects a Bunch;
- If the beam moving on the cavity axis there is no energy transfer;
- After the turn the bunch comes with an offset and transfers energy to cavity;
- Next bunch will be deflected stronger => instability.

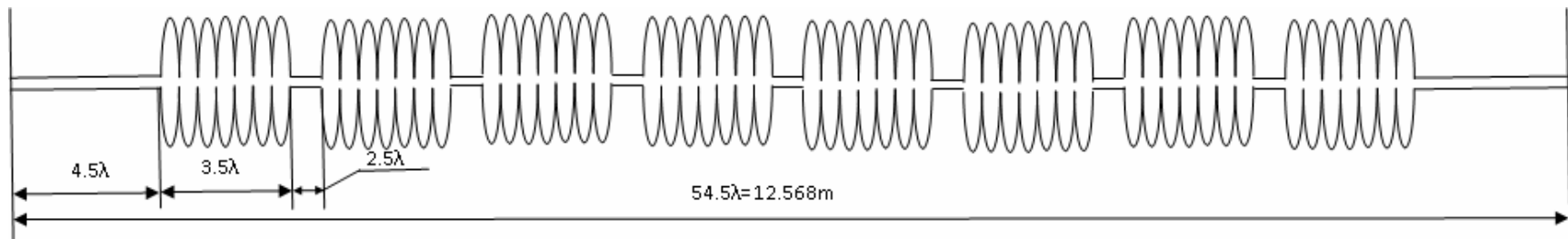


$$I_{th} = - \frac{2pc^2}{e\omega_\lambda \left(\frac{R}{Q}\right)_\lambda Q_\lambda \sum_{j=1}^{N-1} \sum_{i=j+1}^N m_{12}^{ij} \sin(\omega_\lambda (T_i - T_j))} \quad \longrightarrow \quad I_{th} = \frac{2mc^3}{e\omega_\lambda \left(\frac{R}{Q}\right)_\lambda Q_\lambda} \frac{1}{\sqrt{\sum_{j=1}^{N-1} \sum_{i=j+1}^N \frac{\beta_i \beta_j}{\gamma_i \gamma_j}}}$$

For estimations we will use a mode with  $(R/Q)_d \cdot Q_d = 6 \cdot 10^5 \Omega$ ,  $\omega = 2\pi \cdot 2 \cdot 10^9 \text{ Hz}$

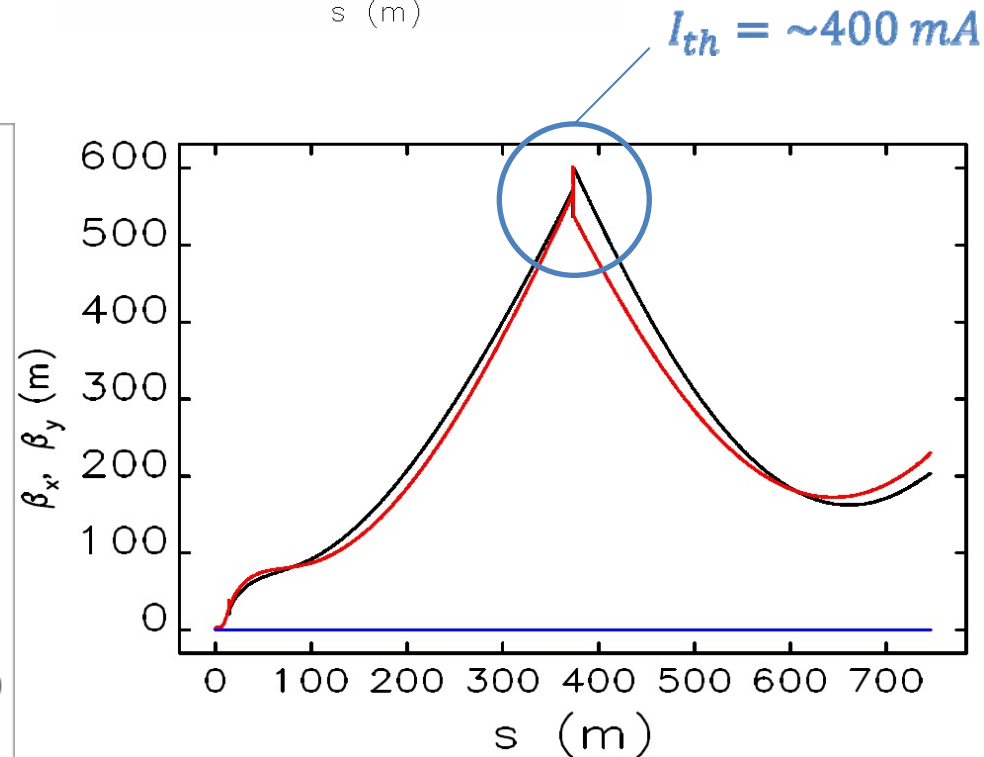
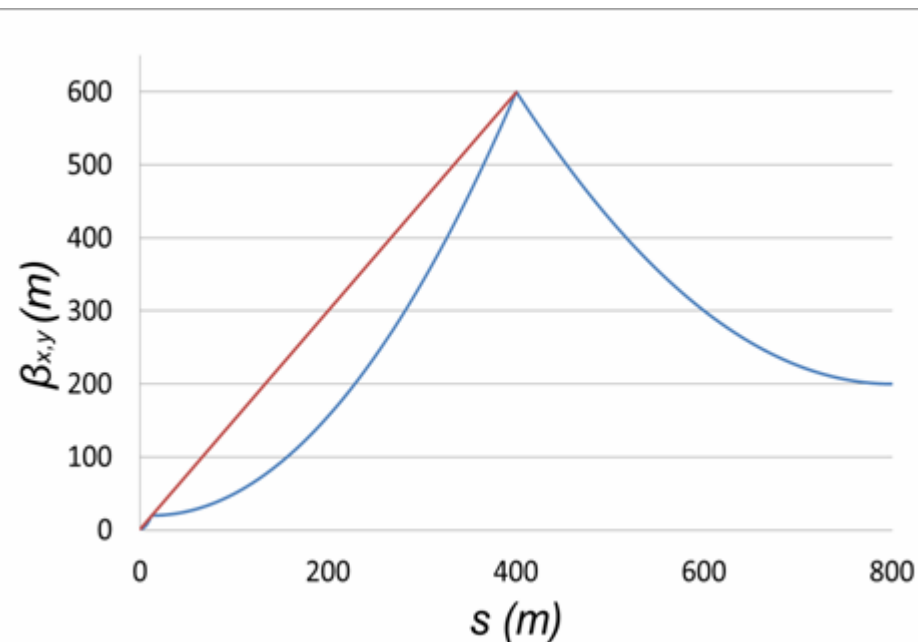
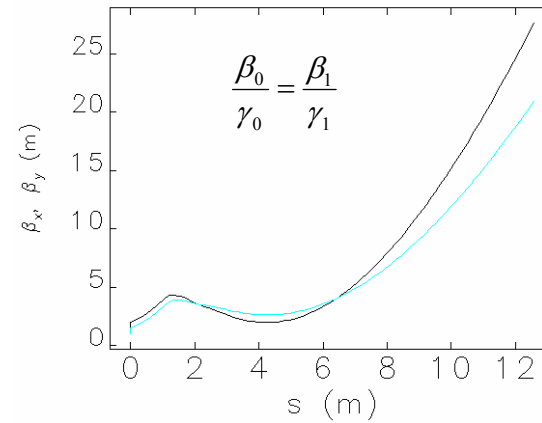


Linac is planned to be based on the cavities like in the BERLinPro.

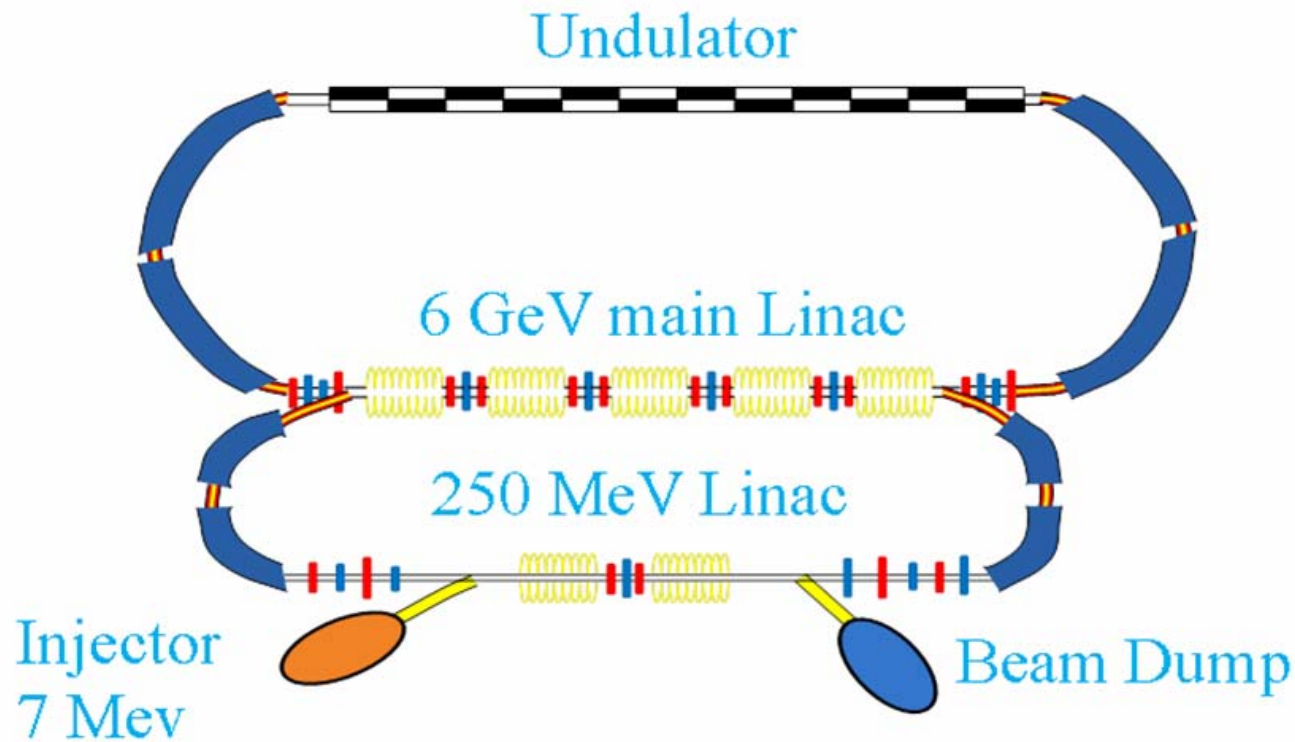


- Cryomodules are planned to have 8 cavities
- Triplets of quadrupoles are planned to be in between of the cryomodules in the Linac.
  - For this we make a distance between cryomodules to be equal to  $15\lambda$ .
  - Estimations shows that focusing in the Linac increases BBU threshold by the factor of **3!!!**

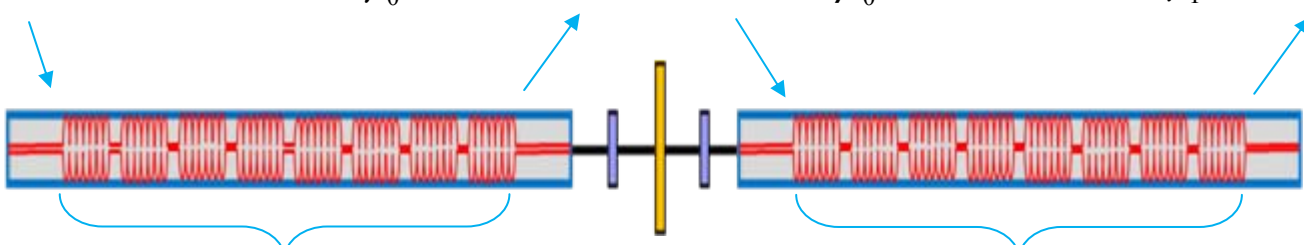
$$\begin{cases} \beta_0 = m_{12} \sim 2 \text{ m} \\ \alpha_0 = m_{11} \sim -0.61 \\ \beta_1 = \frac{\gamma_1}{\gamma_0} m_{12} \sim 31 \text{ m} \end{cases}$$



# Two stage injection scheme



# Two stage injection scheme: Preinjector

$$\beta_0, \alpha_0 \quad \beta_1 = \frac{\gamma_1}{\gamma_0} (\beta_0 m_{11}^2 - 2\alpha_0 m_{11} m_{12} + \frac{1+\alpha_0^2}{\beta_0} m_{12}^2) \quad \beta_2 = \frac{\gamma_2}{\gamma_1} (\beta_1 t_{11}^2 + 2\alpha_1 t_{11} t_{12} + \frac{1+\alpha_1^2}{\beta_1} t_{12}^2)$$


$$\frac{\partial \beta_2}{\partial \alpha_1} = 0 \quad \beta_2 = \frac{\gamma_2}{\gamma_1} \frac{t_{12}^2}{\beta_1}$$

$$M = \begin{pmatrix} \cos(\alpha) - \sqrt{2} \sin(\alpha) & \frac{\sqrt{8} \gamma_0 L \sin(\alpha)}{\Delta \gamma} \\ -\frac{3}{\sqrt{8}} \frac{\Delta \gamma \sin(\alpha)}{L \gamma_1} & (\cos(\alpha) + \sqrt{2} \sin(\alpha)) \frac{\gamma_0}{\gamma_1} \end{pmatrix}$$

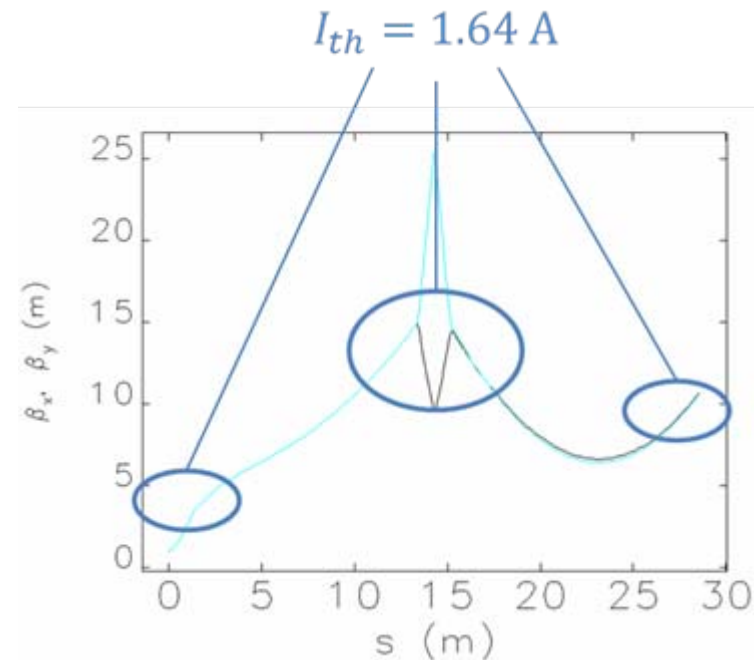
$$T = \begin{pmatrix} t_{11} & t_{12} \\ t_{21} & t_{22} \end{pmatrix}$$

where  $\alpha = \frac{1}{\sqrt{8}} \ln\left(\frac{\gamma_1}{\gamma_0}\right)$

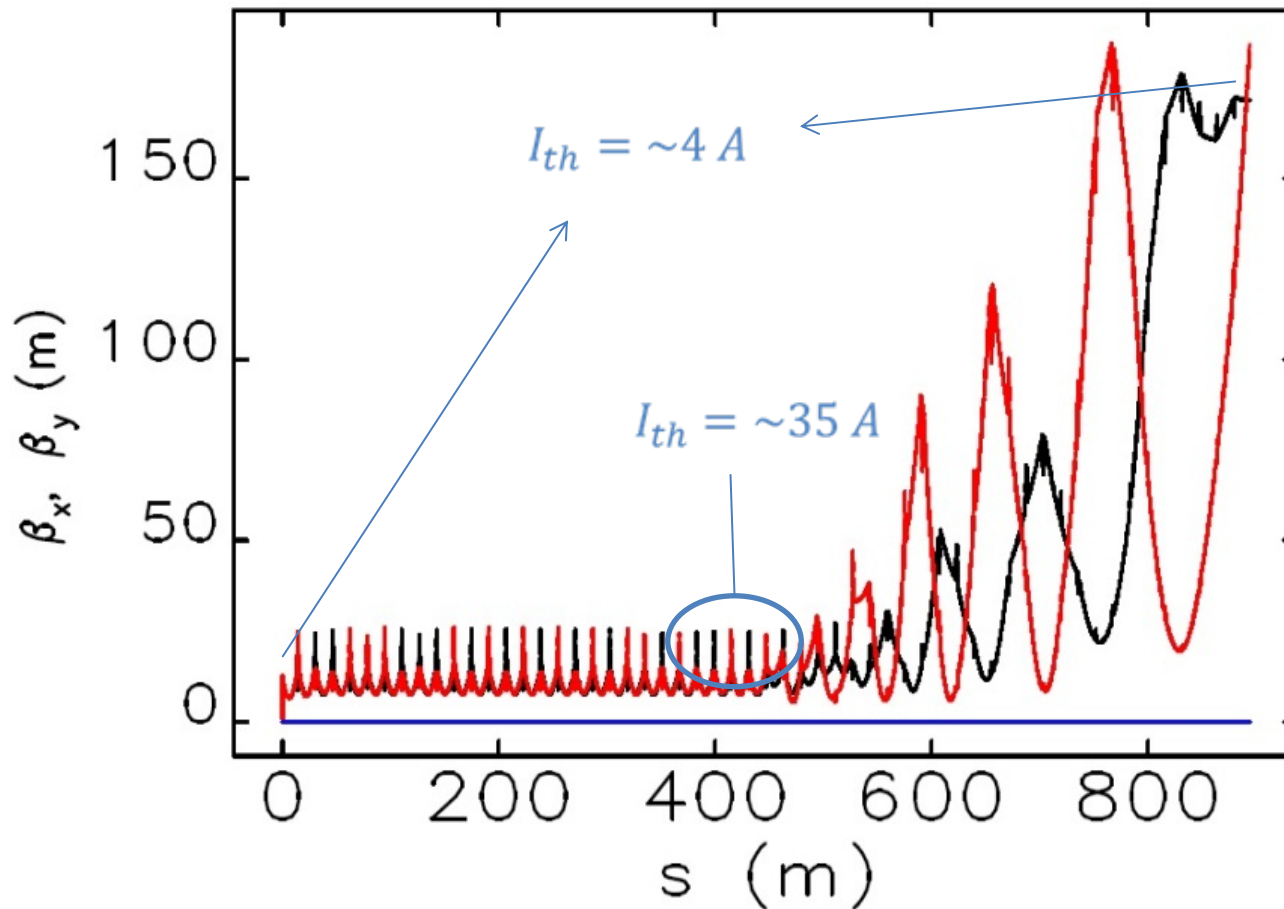
$$\sqrt{\frac{\beta_0 \beta_2}{\gamma_0 \gamma_2}} = \frac{\beta_1}{\gamma_1} \quad \rightarrow$$

$$\beta_0 = \sqrt{\frac{\gamma_1}{\gamma_0} \frac{m_{12}^3}{t_{12}}} = 2.757 \text{ m}$$

$$\alpha_0 = \frac{m_{11}}{m_{12}} \frac{\gamma_0}{\gamma_1} \frac{\beta_1^3}{t_{11}^2} = -1.421$$

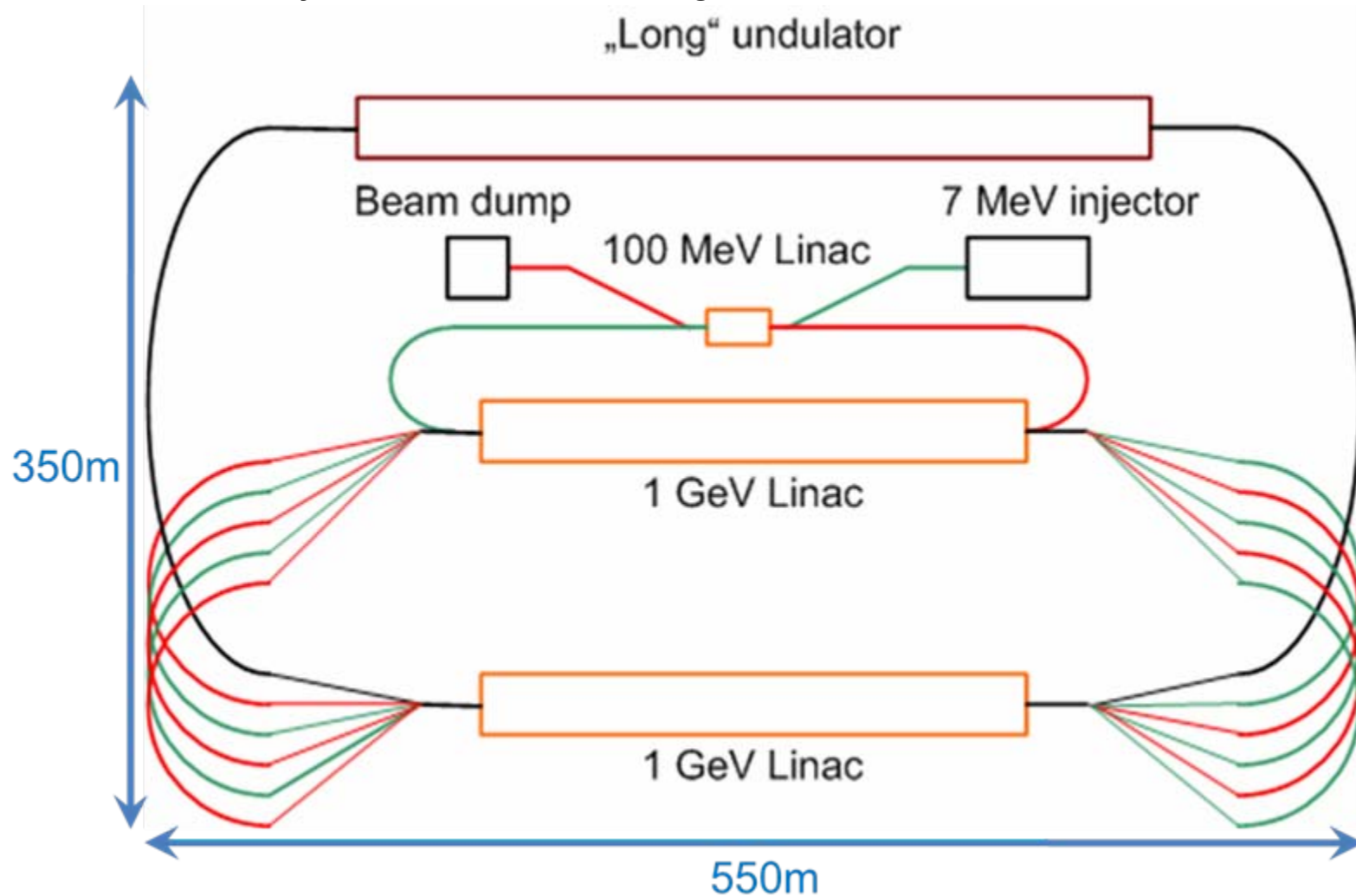


# Two stage injection scheme: main linac

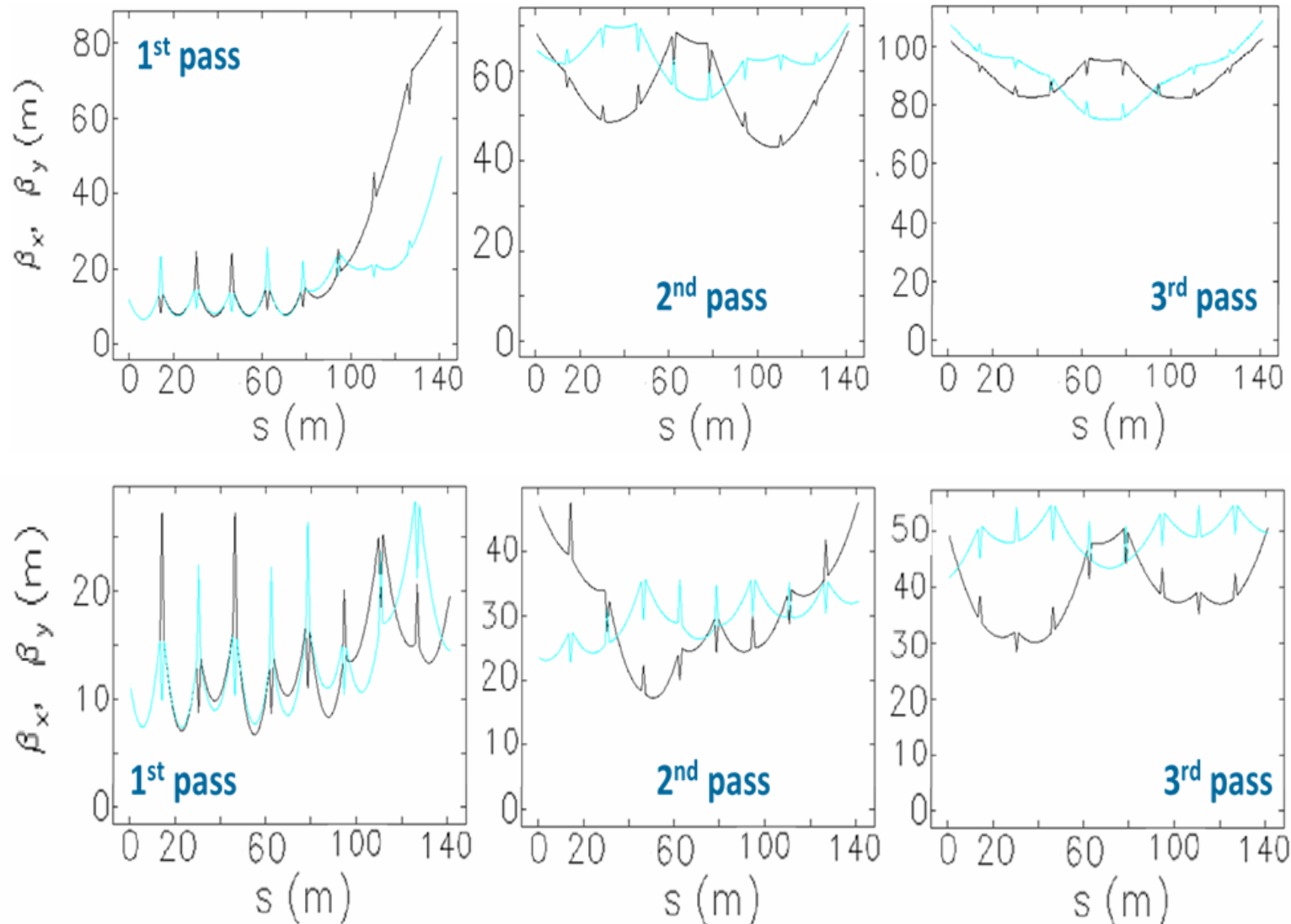


# Layout of a 6 GeV multi-turn ERL with 2-stage injection

Our group started to work for a new project which got the name: "Femto Science Factory" and will be future light source.



## 0.1+1+1 GeV model



# Different acceleration pattern

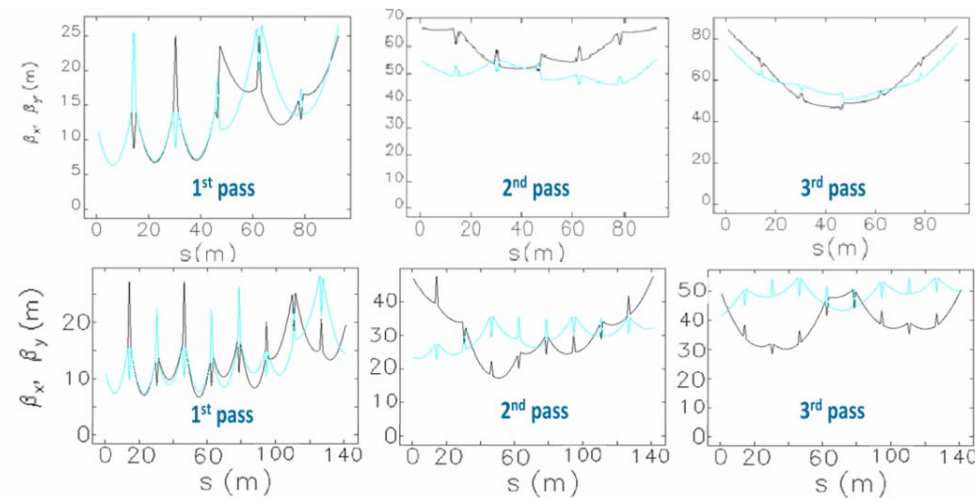
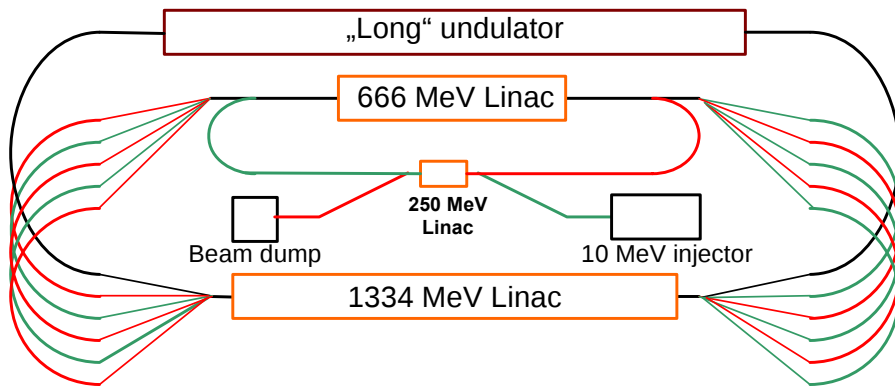
$\beta_{1,1(6)} = \beta_{2,1(6)} \sim 12.57 \text{ m}$  — because of triplets and

$\beta_{1,n} = x$  or  $\beta_{2,n} = L-x$  for the 1<sup>st</sup> and the 2<sup>nd</sup> linac respectively,  $n=2..5$ .

$$\sqrt{\sum_{m=1}^{2N-1} \sum_{n=m+1}^{2N} \frac{\beta_{1,n} \beta_{1,m}}{\gamma_{1m}(x) \gamma_{1n}(x)}} = \sqrt{\sum_{m=1}^{2N-1} \sum_{n=m+1}^{2N} \frac{\beta_{2,n} \beta_{2,m}}{\gamma_{2m}(x) \gamma_{2n}(x)}}$$

This equation can be solved numerically  $\longrightarrow x \sim L / 3$

$L = 2000 \text{ [MeV] / G}$ ,  $x$  is the length of the 1<sup>st</sup> linac,  $L-x$  is the length of the 2<sup>nd</sup>



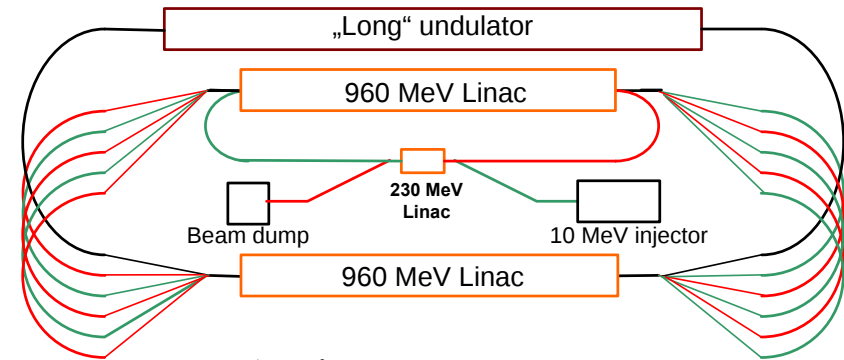
But this scheme has a more complicated spreader, because the energies of the beam in the spreader are: ...4250, 4916, 6250. Are closer then in 1+1 scheme: 4250 and 5250...

final energy of a beam:

$$E_{fin} = (E_0 + E_{preinj})(1 + 2Nk) = 6 \text{ GeV},$$

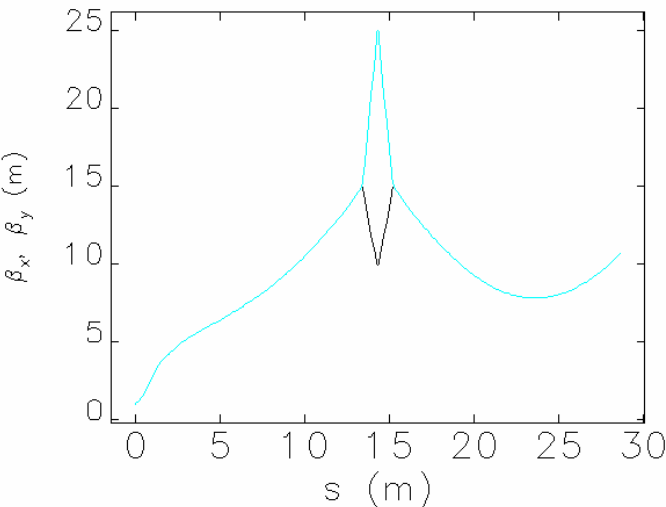
where:

$E_0 = 10 \text{ MeV}$  is the energy after booster,  
 $E_{preinj}$  is the energy gain in the preinjector,  
 $N$  is the number of passes during acceleration  
 and constant  $k = 4$ .

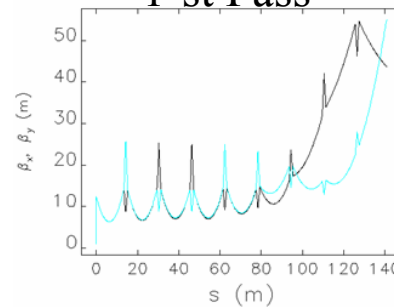


1<sup>st</sup> Linac

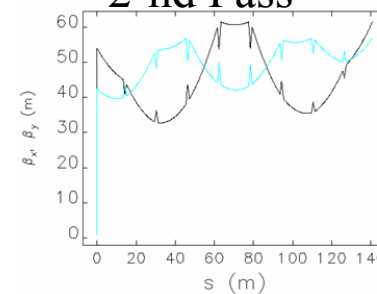
Preinjector



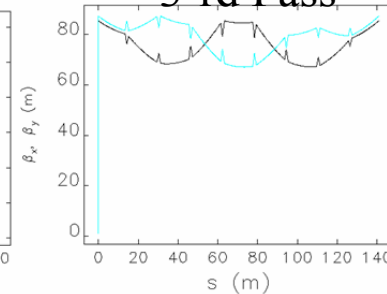
1-st Pass



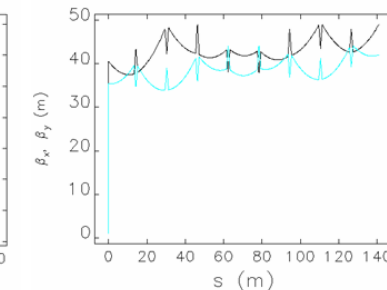
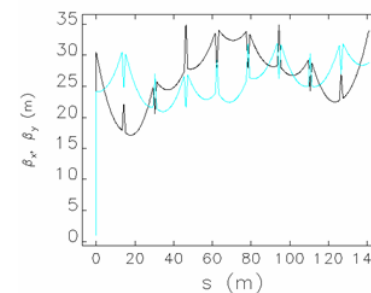
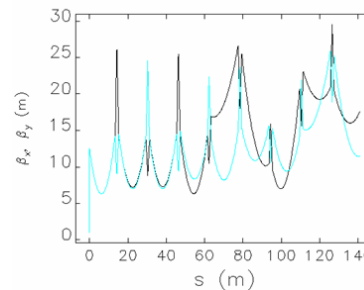
2-nd Pass



3-rd Pass



2<sup>nd</sup> Linac



| Linac scheme                 | $I_{th}$ , A |                       |                       |
|------------------------------|--------------|-----------------------|-----------------------|
|                              | Preinjector  | 1 <sup>st</sup> Linac | 2 <sup>nd</sup> Linac |
| $0.100 + 1 + 1\text{GeV}$    | 1.26         | 0.88                  | 3.73                  |
| $250 + 666 + 1334\text{MeV}$ | 1.64         | 1.46                  | 3.58 ??               |
| Scalable, estimations        | 1.58         | 0.73                  | 2.34                  |

*For this estimation we took a mode with  $(R/Q)_d \cdot Q_d = 6 \cdot 10^5 \Omega$ ,  $\omega = 2\pi \cdot 2 \cdot 10^9 \text{ Hz}$*

| Scheme           | $I_{th}$ , A (estimations)        |
|------------------|-----------------------------------|
| Direct injection | ~0.4 A in the middle of the linac |
| Two stage        | ~1.64 in the preinjector          |
| Scalable FSF     | ~0.7 in the 1-st linac            |

| Component                                                                                            | Direct injection<br>scheme, Cost, M€ | Scalable FSF,<br>Cost, M€ |
|------------------------------------------------------------------------------------------------------|--------------------------------------|---------------------------|
| Infrastructure/tunnel:<br>(land+tunnel+buildings)                                                    | 375                                  | 110                       |
| SRF:<br>(cryogenic plant+cryomodules+RF generators)                                                  | 485                                  | 190                       |
| Warm machine:<br>(magnets+undulators+ vacuum system +<br>diagnostics/control systems+power supplies) | 150                                  | 230                       |
| User stations                                                                                        | 200?                                 | 200?                      |
| People:<br>(staff for 10 years + beamline scientists)                                                | 100                                  | 100                       |
| Total Sum                                                                                            | 1310                                 | 830                       |

**Special thanks to:**

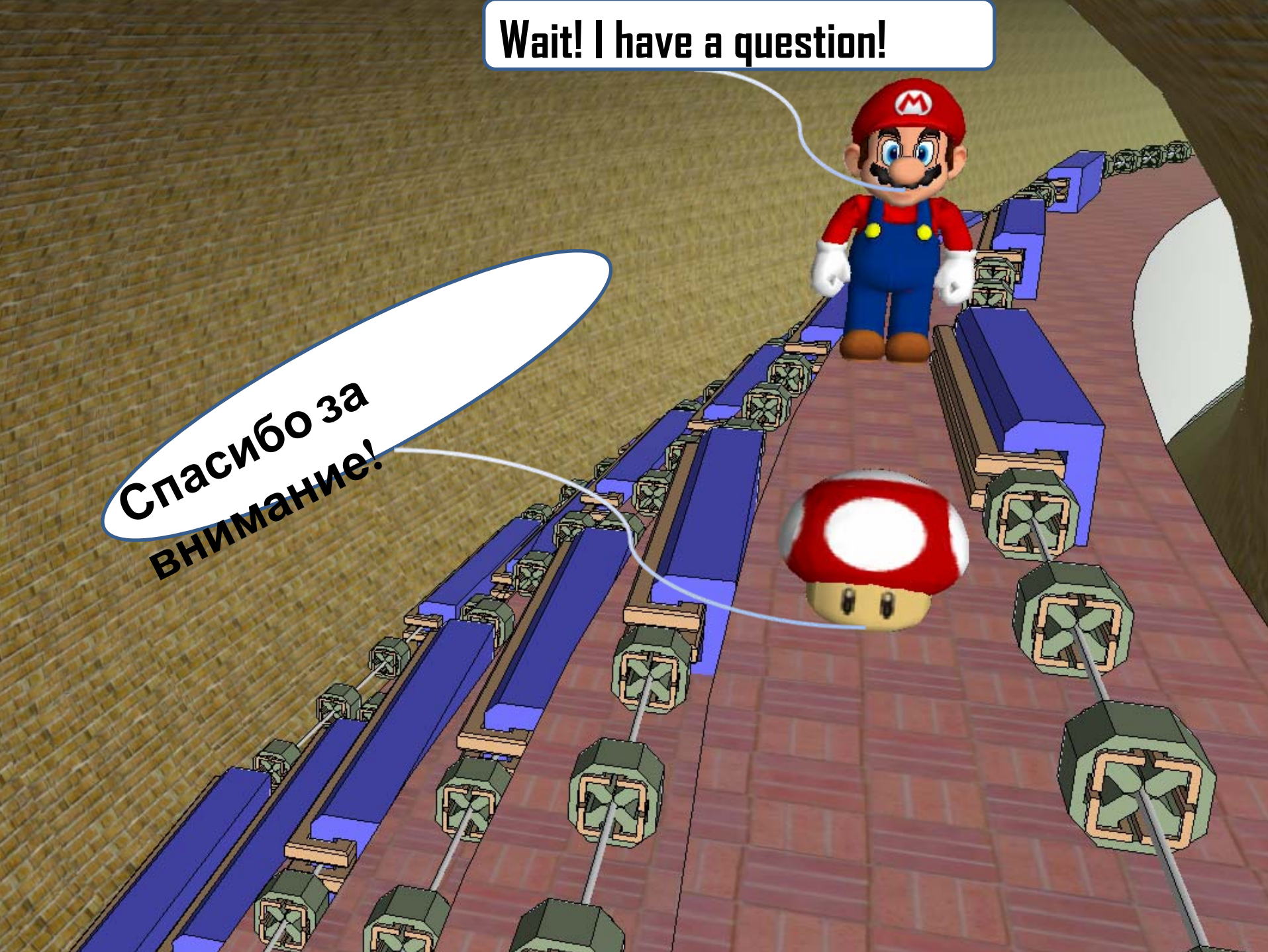
**T. Atkinson**

**A. Bondarenko**

**A. Matveenko**

Wait! I have a question!

Спасибо за  
внимание!



$$I_b \approx I_0 \frac{\tilde{\lambda}^2}{Q_a L_{eff} \sqrt{\sum_{m=1}^{2N-1} \sum_{n=m+1}^{2N} \frac{\beta_m \beta_n}{\gamma_m \gamma_n}}}, \quad 2N=6 - \text{passes}$$

|                                                                                        | With triplets | Without |          |
|----------------------------------------------------------------------------------------|---------------|---------|----------|
|                                                                                        | $\beta$       | $\beta$ | $\gamma$ |
| 1                                                                                      | 11.7          | 110     | 200      |
| 2                                                                                      | 65            | 110     | 2000     |
| 3                                                                                      | 105           | 110     | 6000     |
| 4                                                                                      | 105           | 110     | 10000    |
| 5                                                                                      | 70            | 110     | 6000     |
| 6                                                                                      | 85            | 110     | 2000     |
| $\sqrt{\sum_{m=1}^{2N-1} \sum_{n=m+1}^{2N} \frac{\beta_m \beta_n}{\gamma_m \gamma_n}}$ | 0.108         | 0.309   |          |

Addition focusing in the Linac increases BBU threshold by the factor of about **3!!!**

| Component                                     | Direct injection scheme,<br>Cost, M€                                                                                         | Scalable FSE, Cost, M€                                                                                                                                                       |
|-----------------------------------------------|------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 1. Infrastructure/tunnel                      |                                                                                                                              |                                                                                                                                                                              |
| a) Land                                       | $(3.14/4 \cdot 1050^2 \text{ m}^2 + (750 \text{ m} \cdot 1050 \text{ m})) \cdot 0.16 \text{ k€}/\text{m}^2 \sim 265$         | $350 \text{ m} \cdot 550 \text{ m} \cdot 0.16 \text{ k€}/\text{m}^2 \sim 31$                                                                                                 |
| b) Tunnel                                     | $(3.14 \cdot 1050 + 2 \cdot 750) \text{ m} \cdot 0.01 \text{ M€}/\text{m} = 48$                                              | $(3.14 \cdot 350 + 2 \cdot 200) \text{ m} \cdot 0.01 \text{ M€}/\text{m} = 15$                                                                                               |
| c) Buildings (users)                          | 2x400m or 10x? ~ 50                                                                                                          | 2x400m or 10x? ~ 50                                                                                                                                                          |
| d) Technical buildings                        | 10?                                                                                                                          | 10?                                                                                                                                                                          |
| Sum                                           | $265 + 48 + 50 + 10? = 373$                                                                                                  | $31 + 15 + 50 + 10? = 106$                                                                                                                                                   |
| 2. SRF                                        |                                                                                                                              |                                                                                                                                                                              |
| a) Cryogenic plant                            | 300 W/0.1 GeV * (2 beams at 6 GeV) = 5-10 kW @ 2 K=20?                                                                       | 300 W/0.1 GeV * (6 beams at 2 GeV and 2 beams at 0.25 GeV) = 5-10 kW @ 2 K=20?                                                                                               |
| b) Cryomodules                                | 56*5 M€=280                                                                                                                  | $(9 \cdot 2 + 2) \cdot 5 \text{ M€} \sim 20 \cdot 5 = 100$                                                                                                                   |
| c) RF generators                              | 20mA*10 MeV= 200 kW inj<br>10kW*56*8=4.48 MW Linacs<br>1.5+448*0.4~180.7                                                     | 20mA*10 MeV= 200 kW inj<br>10kW*20*8=1.6 MW Linacs<br>1.5+160*0.4~65.5                                                                                                       |
| Sum                                           | $20 + 280 + 180.7 = 480.7$                                                                                                   | $20 + 100 + 65.5 = 185.5$                                                                                                                                                    |
| 3. Warm machine                               |                                                                                                                              |                                                                                                                                                                              |
| a) Magnets                                    | $2 \cdot (6+6) \cdot 46(\text{arcs}) + 15(\text{triplets}) + 600(\text{undulators}) \sim 1719 \cdot 10 \text{ k€} \sim 17.2$ | $60 \cdot 4(\text{spread/rec}) + 6 \cdot (6+6) \cdot 46(\text{arcs}) + 100(\text{preinj}) + 50(\text{triplets}) + 600(\text{undulators}) \sim 4300 \cdot 10 \text{ k€} = 43$ |
| b) Undulators                                 | $60 \cdot 1 + 1 \cdot 5 = 65$                                                                                                | $60 \cdot 1 + 1 \cdot 5 = 65$                                                                                                                                                |
| c) Vacuum system +diagnostics/control systems | $(3.14 \cdot 1050 \text{ m} + 2 \cdot 750) \cdot 10 \text{ k€} = 48$                                                         | $(6 \cdot 3.14 \cdot 350 \text{ m} + 6 \cdot 4 \cdot 25 \text{ m} + 2 \cdot 150 \text{ m}) \cdot 10 \text{ k€} = 75$                                                         |
| d) Power supplies                             | ~ number of magnets ~ 17.2                                                                                                   | ~ number of magnets ~ 43                                                                                                                                                     |
| Sum                                           | $17.2 + 65 + 48 + 17.2 = 147.4$                                                                                              | $43 + 65 + 75 + 43 = 226$                                                                                                                                                    |
| 4. People                                     |                                                                                                                              |                                                                                                                                                                              |
| a) Staff                                      | 100(ppl)*10(years)*50 k€=50                                                                                                  | 100(ppl)*10(years)*50 k€=50                                                                                                                                                  |
| b) Beamline scientists                        | 50*10*100 k€=50                                                                                                              | 50*10*100 k€=50                                                                                                                                                              |
| c) Stations                                   | 200                                                                                                                          | 200                                                                                                                                                                          |
| Overhead                                      | ?                                                                                                                            | ?                                                                                                                                                                            |
| Sum                                           | 300+?                                                                                                                        | 300+?                                                                                                                                                                        |
| Total Sum                                     | $373 + 480.7 + 147.4 + 300 + ? = 1301.1 + ?$                                                                                 | $106 + 185.5 + 226 + 300 + ? = 817.5 + ?$                                                                                                                                    |