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# **Electron lenses for experiments on nonlinear dynamics with wide stable tune spreads in the Fermilab Integrable Optics Test Accelerator**

Giulio Stancari

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# Contributors and collaborators

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  - F. O'Shea, A. Murokh (Radiabeam)
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# Outline

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- ▶ **Introduction and motivation**

- ▶ high-power machines for particle physics
- ▶ the role of nonlinear integrable optics
- ▶ the Fermilab IOTA ring
- ▶ electron lenses

- ▶ **Nonlinear integrable optics with electron lenses in IOTA**

- ▶ Integrable optics scenarios with electron lenses
  - ▶ 1. thin kicks of McMillan type
  - ▶ 2. axially symmetric kicks in long solenoid
- ▶ Design considerations

- ▶ **Conclusions and next steps**

# Motivation

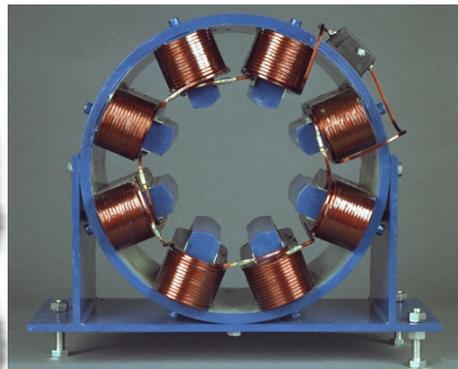
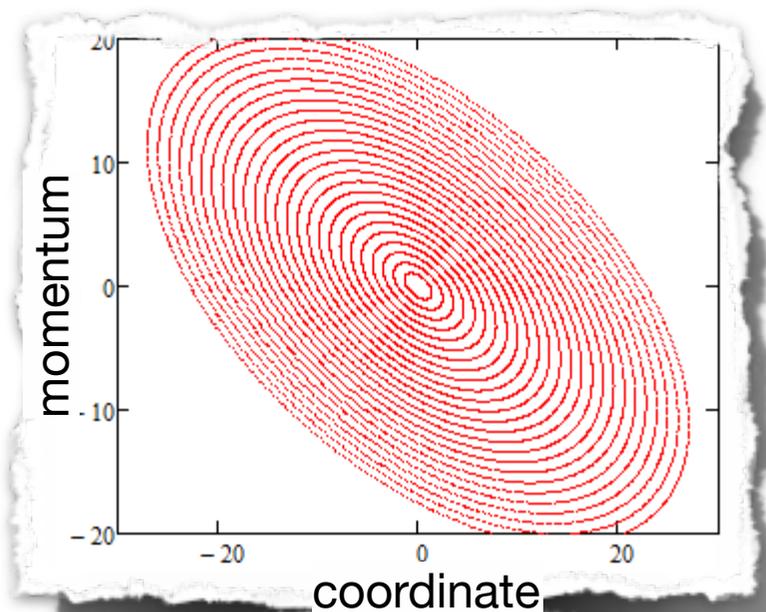
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- **High-power machines** are needed to study **neutrinos** and **rare processes** in particle physics
- Limitations:
  - **losses** and **beam halo**
  - **space-charge effects**
  - transverse and longitudinal **instabilities**
- **Innovative accelerator designs** could significantly reduce the cost of machines in the megawatt range, as emphasized by **US particle physics community priorities**: [www.usparticlephysics.org/p5](http://www.usparticlephysics.org/p5)
- A **possible roadmap** towards high-intensity rings:
  - develop **theories and models** for high-intensity circular machines
  - perform **proof-of-principle experiments** at ASTA/IOTA
  - design a **new kind of rapid-cycling synchrotron**
    - nonlinear optics and wide tune spread to suppress instabilities
    - stable motion up to large amplitudes
    - self-consistent or compensated space charge
- **Education and training** of accelerator scientists and engineers

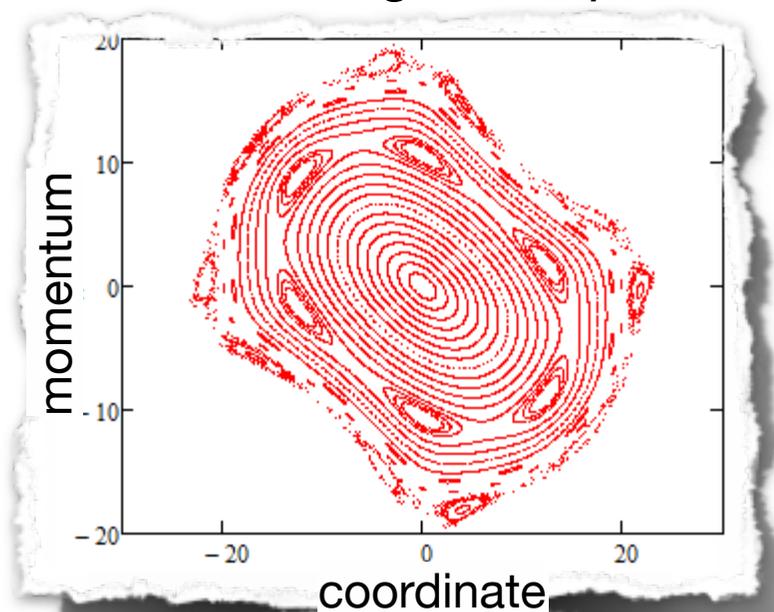
# Mainstream accelerator lattices

- **Conventional strong-focusing accelerators are based upon linear elements** (dipoles and quadrupoles). Same design betatron frequency for all particles. In the ideal case, the Courant-Snyder invariant is conserved
- **Nonlinear elements are necessary** (e.g., sextupoles for chromaticity, octupoles for Landau damping) **or unavoidable** (e.g., space-charge and beam-beam forces)
- Stability depends on initial conditions. Nonlinearities are the sources of resonances and their driving terms. Motion is unstable at large amplitudes.

*linear lattice*



*effect of single octupole*



# Intrinsically nonlinear stable lattices?

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- Advantages of a **nonlinear optics** with a **large natural tune spread**
  - increased Landau damping
  - improved stability to periodic perturbations
  - suppression of halo formation in space-charge dominated beams, driven by resonance between linear optics and space-charge breathing modes
  - mitigation of two-stream instability in space-charge compensation schemes

## Can accelerators be nonlinear yet stable?

If motion is **integrable**, i.e. with  $n$  independent conserved quantities for  $n$ -dimensional dynamics, then it is **bounded** and therefore **stable**

# The search for nonlinear integrable lattices

McMillan (1967) found a 1-dimensional solution: a **specific thin kick** in a linear lattice (rational polynomial function) yields an **integral of motion that is quadratic in coordinate and momentum**

$$\text{The map } \left. \begin{array}{l} \text{[after]} \\ x' = y \\ y' = -x + f(y) \end{array} \right\} \text{ [before]} \quad \text{with } f(x) = -\frac{Bx^2 + Dx}{Ax^2 + Bx + C}.$$

conserves the quantity  $Ax^2y^2 + B(x^2y + xy^2) + C(x^2 + y^2) + Dxy$

It can easily be **extended to 2D** in an **uncoupled symmetric lattice**. The **axially symmetrical kick can be generated by a charge distribution, such as an electron lens**

McMillan, UCRL-17795 (1967)

Danilov and Nagaitsev, PRSTAB **17**, 124402 (2014)

Mane, arXiv:1502.02604 [physics.acc-ph] (2015)

# The search for nonlinear integrable lattices

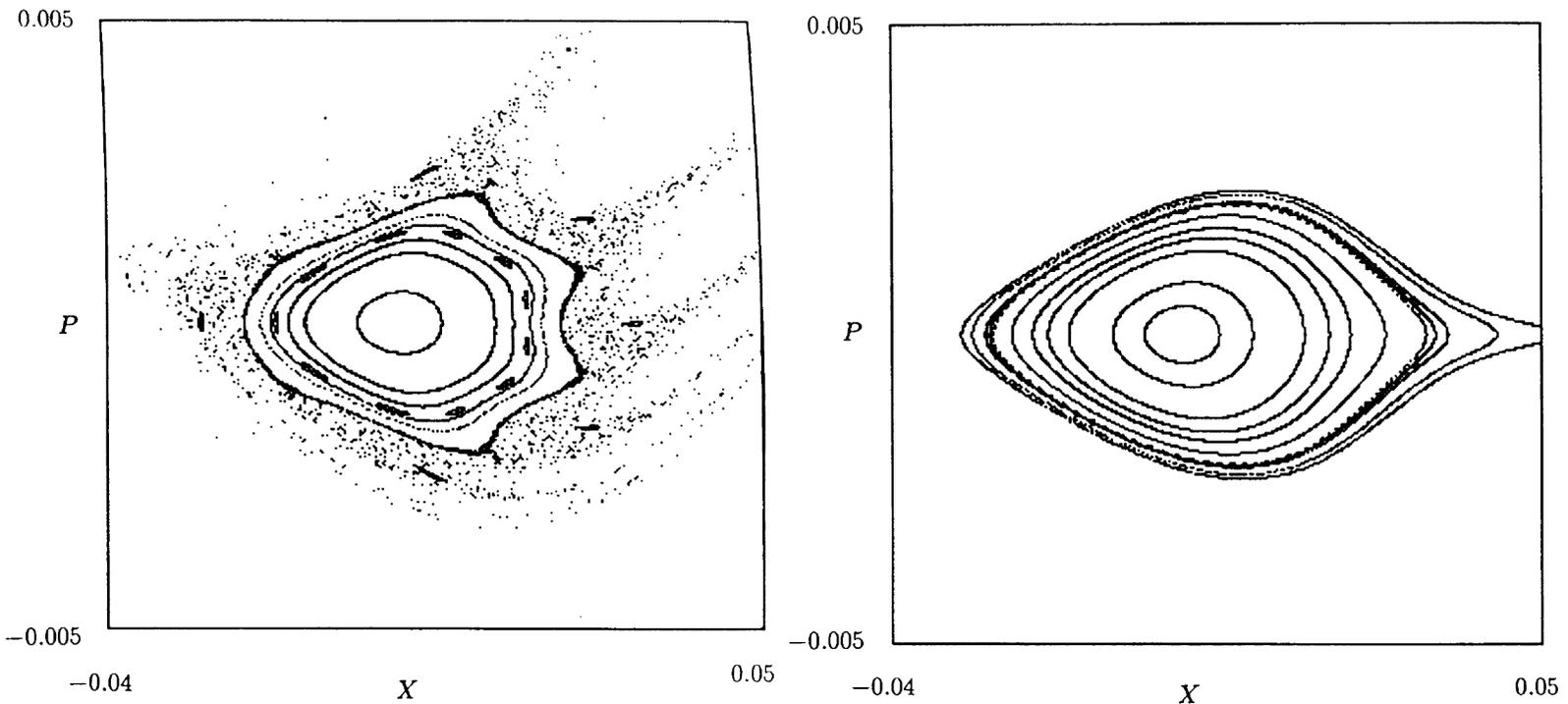
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- Danilov and Perevedentsev (1990s) studied extensions to 2D and proposed “**round colliding beams**” (i.e., equal beta functions, tunes, emittances, and no coupling in arcs):
  - **longitudinal component of angular momentum** is conserved, dynamics is “quasi integrable”
  - dynamics would be completely integrable if one could achieve a “McMillan-type” charge distribution in the opposing beam

Benefits of round beams were **demonstrated experimentally** at BINP VEPP-2000  $e^+ e^-$  collider: achieved record tune spread of 0.25 (Romanov, NA-PAC13)

# The search for nonlinear integrable lattices

Chow and Cary (1994) and Wan and Cary (1998, 2001) proposed an empirical method to increase dynamic aperture by minimizing the size of islands and chaotic regions with appropriately chosen sextupole, octupole, and decupole elements.



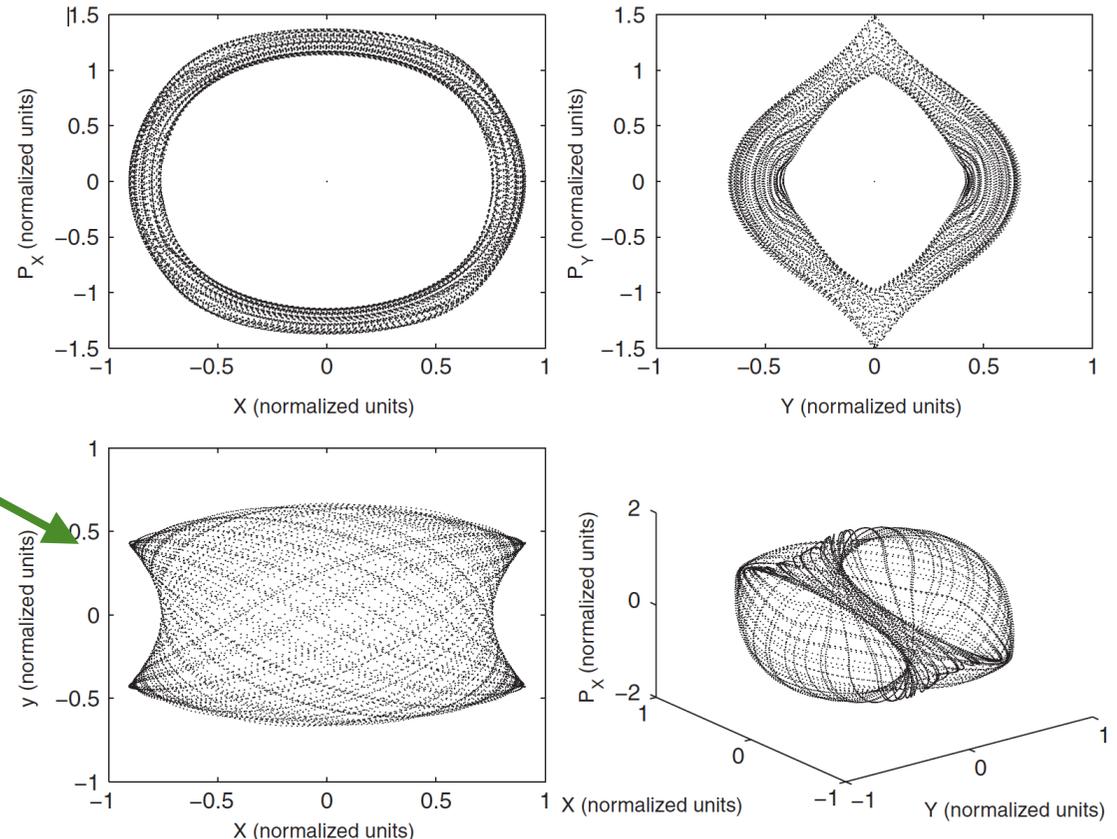
*Calculated Poincaré maps for the Berkeley ALS before and after optimization*

Chow and Cary, PRL **72**, 1196 (1994)

# The search for nonlinear integrable lattices

- Danilov and Nagaitsev (2010) found an **analytical solution for transverse motion with 2 invariants that can be implemented with Laplacian potentials (i.e., special multipole magnets)**. Integrals of motion are:
  - longitudinal component of angular momentum
  - “McMillan type” quantity, quadratic in momenta

*Examples of projected integrable trajectories*



Characteristic hourglass shape  
in transverse plane

Danilov and Nagaitsev,  
PRSTAB **13**, 084002 (2010)

# Proposed configurations for transverse integrable optics

- The lattice is made of **2 main building blocks**
  - an **axially symmetric, linear arc with specified phase advance**, equivalent to a thin lens (“**T-insert**”)
  - a **nonlinear section** with equal beta functions and
    - nonlinear magnet or
    - thin, round McMillan-type kick (**electron lens option #1**) or
    - any axially symmetric kick in solenoid (**electron lens option #2**)

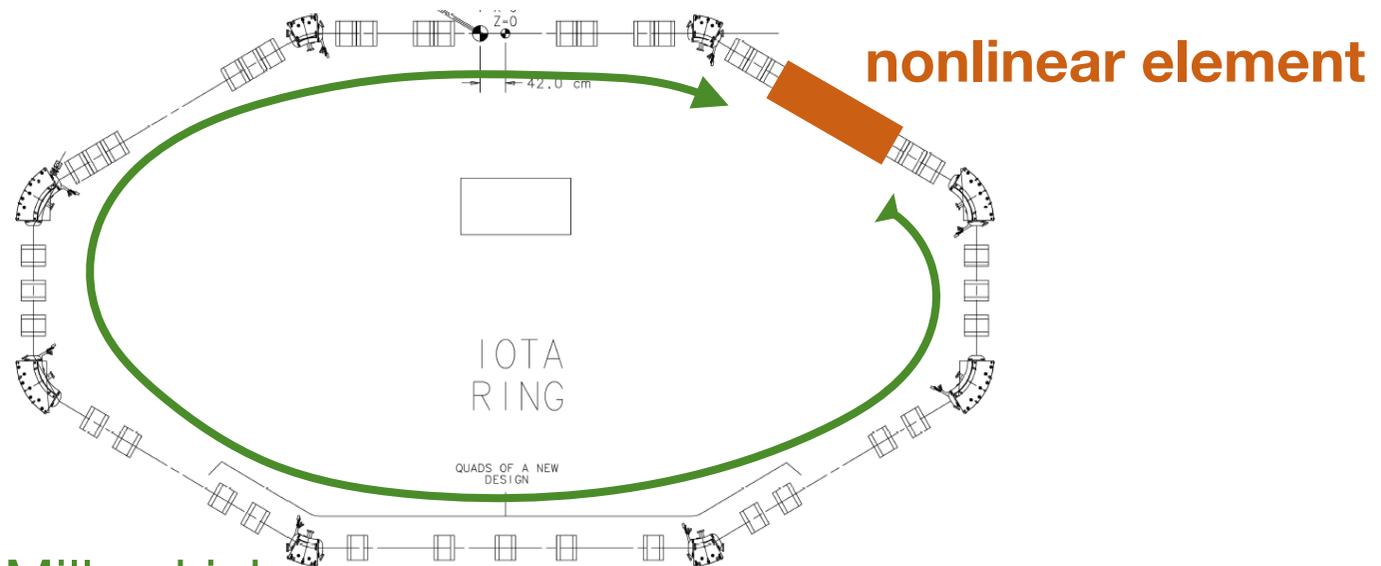
**linear arc:**

$$\begin{pmatrix} 1 & 0 & 0 & 0 \\ -k & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & -k & 1 \end{pmatrix}$$

**or**

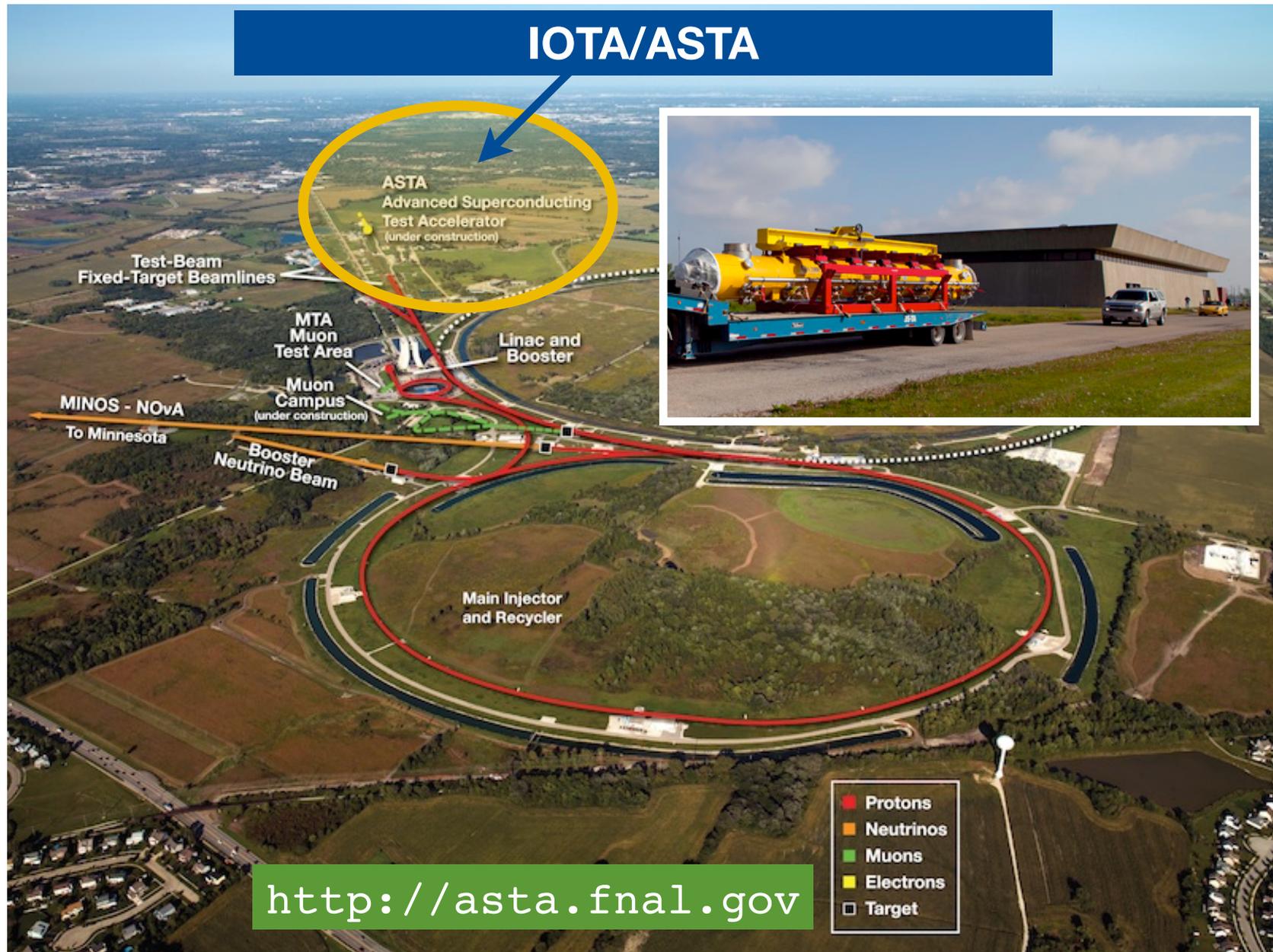
$$\begin{pmatrix} 0 & \beta & 0 & 0 \\ -1/\beta & 0 & 0 & 0 \\ 0 & 0 & 0 & \beta \\ 0 & 0 & -1/\beta & 0 \end{pmatrix}$$

for McMillan kicks

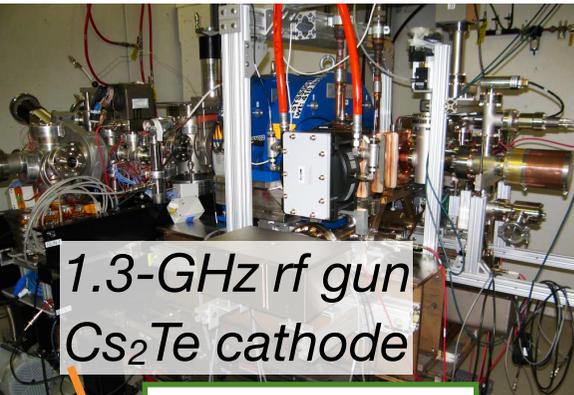


Existing large high-intensity machines may be tuned so that arcs become one or more “T-inserts”

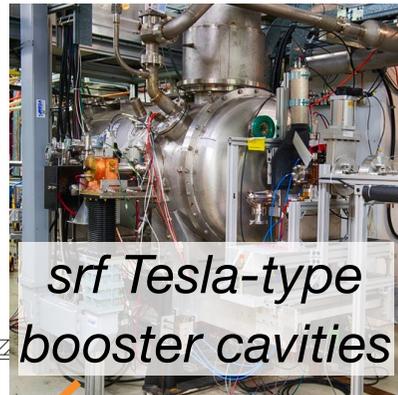
# A beam physics research center at Fermilab



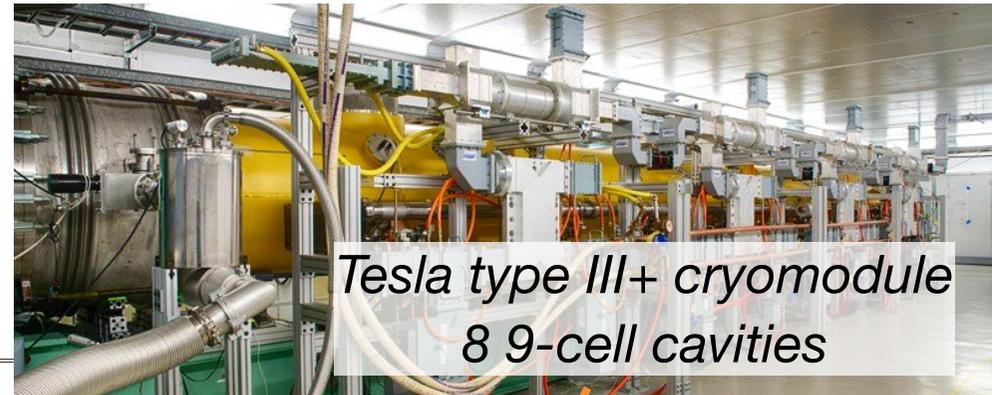
# ASTA photoinjector



1.3-GHz rf gun  
Cs<sub>2</sub>Te cathode



srf Tesla-type  
booster cavities

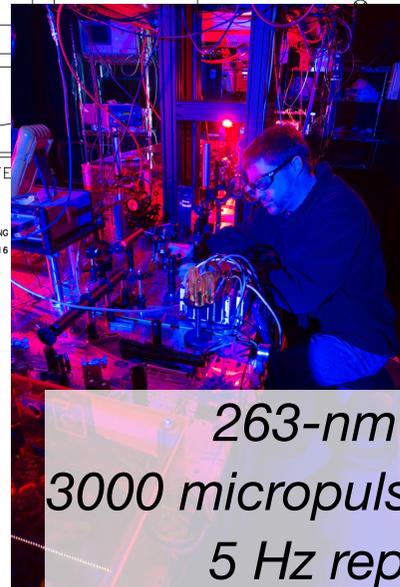


Tesla type III+ cryomodule  
8 9-cell cavities

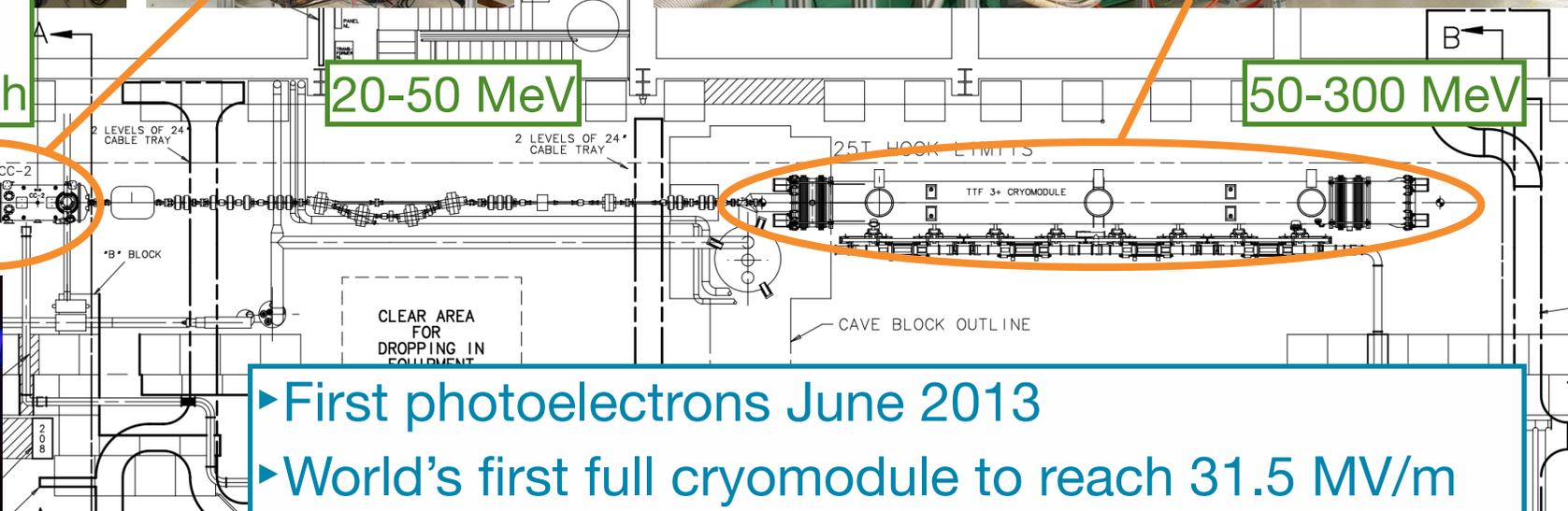
5-MeV e<sup>-</sup>  
3.2 nC/bunch

20-50 MeV

50-300 MeV



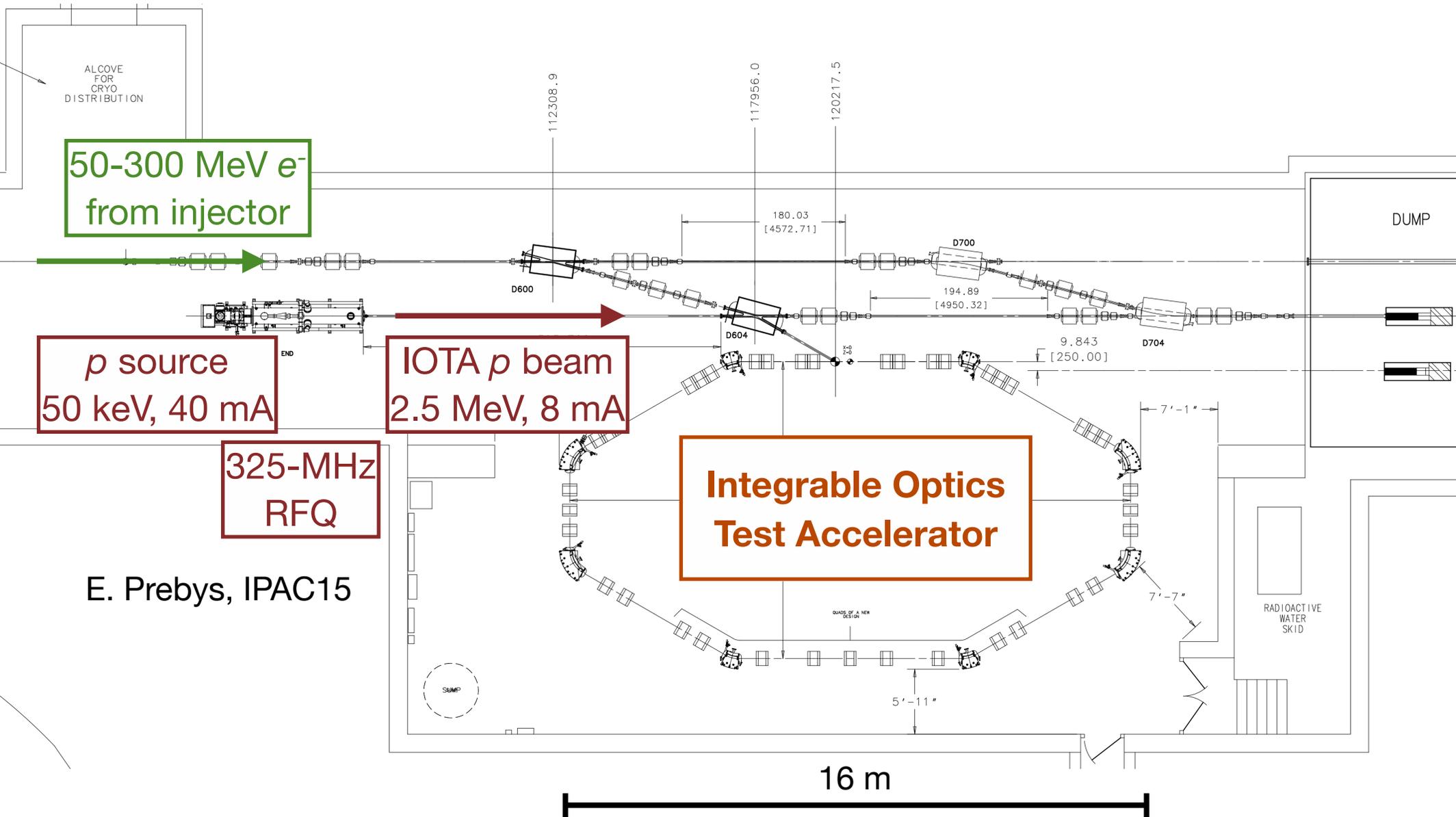
263-nm laser  
3000 micropulses @ 3 MHz  
5 Hz rep. rate



- ▶ First photoelectrons June 2013
- ▶ World's first full cryomodule to reach 31.5 MV/m average gradient (Oct 2014)
- ▶ 20-MeV beam line commissioning Mar-May 2015

D. Crawford et al., IPAC15

# High-energy beam lines and IOTA (under construction)



E. Prebys, IPAC15

# IOTA layout and main components

20 x/y/skew correctors  
8 x correctors in dipoles  
20 button BPMs

30 deg and  
60 deg  
dipoles  
with sync-  
light ports

injection  
S. Antipov, IPAC15

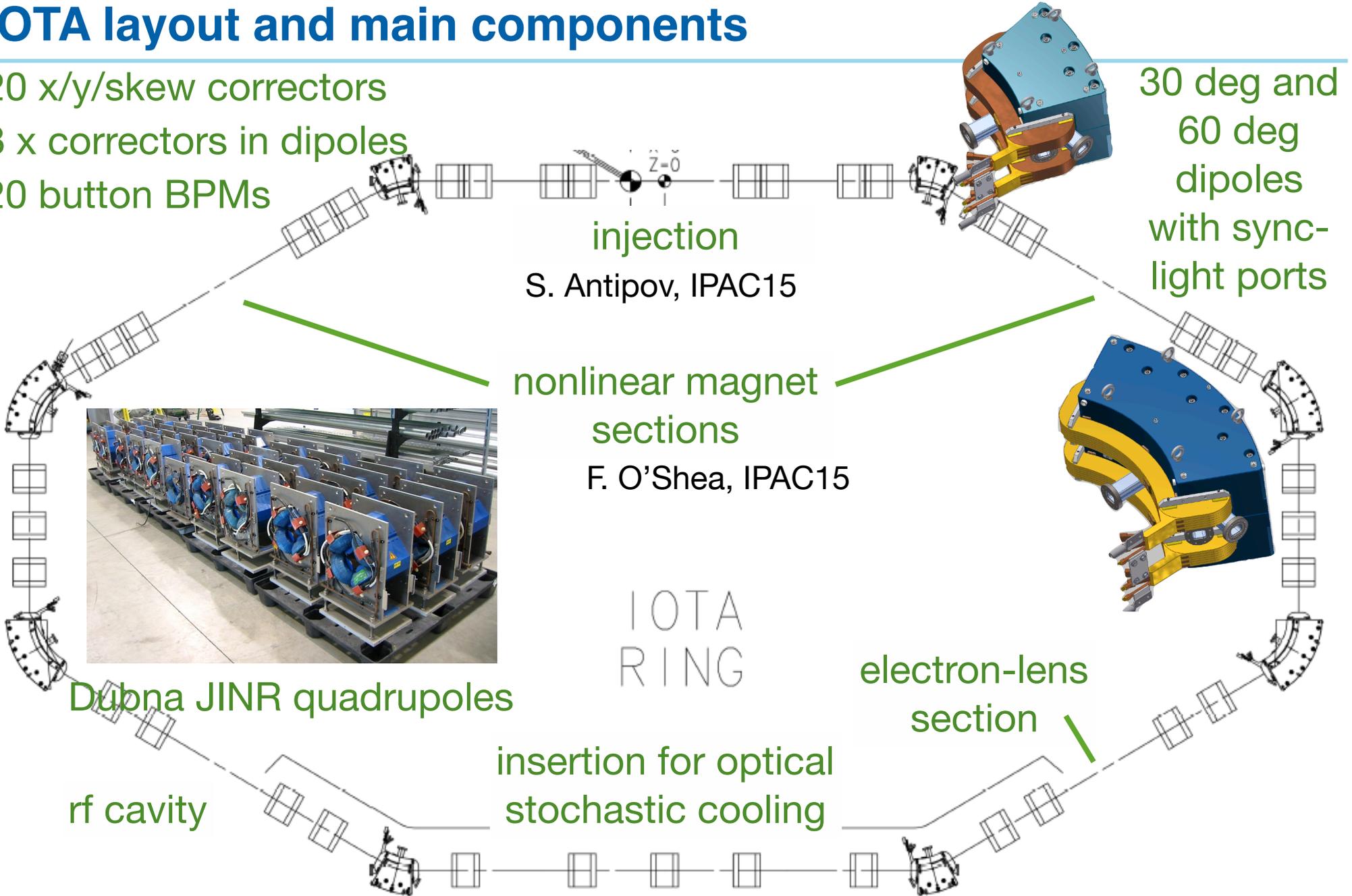
nonlinear magnet  
sections  
F. O'Shea, IPAC15

IOTA  
RING

electron-lens  
section

insertion for optical  
stochastic cooling

Dubna JINR quadrupoles  
rf cavity



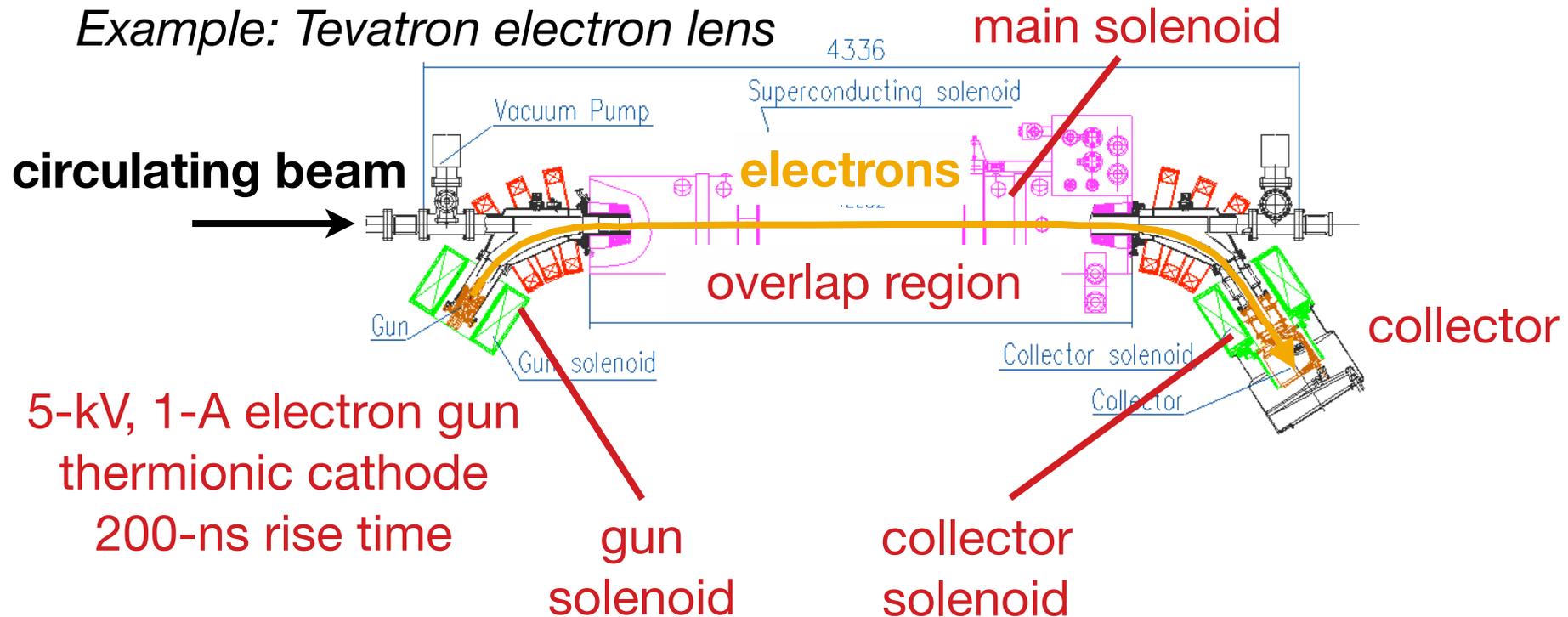
# IOTA parameters for circulating electrons

$e^-$ beam energy	150 MeV
gamma rel.	294.54
$e^-$ beam intensity	$10^9$ particles, 1 bunch
circumference	40 m
revolution freq. / period	7.49 MHz / 0.133 $\mu$ s
bend field	0.7 T
pipe diameter	50 mm
max. beta function h / v	12 m / 5 m
momentum compaction	0.02 – 0.1
betatron tune	3 – 5
natural chromaticity	-5 – -10
transverse rms emittance	10–40 nm
synch. rad. damping time	0.6 s ( $5 \times 10^6$ turns)
rf frequency	30 MHz (h = 4)
rf voltage	1 kV
synchrotron tune	$(2 - 5) \times 10^{-4}$
rms bunch length	12 cm
rms momentum spread	$1.4 \times 10^{-4}$

# What's an electron lens?

- Pulsed, magnetically confined, low-energy electron beam
- Circulating beam affected by electromagnetic fields generated by electrons
- Current-density profile shaped by cathode and electrode geometry
- Stability provided by strong axial magnetic fields

*Example: Tevatron electron lens*



For IOTA, we plan to use a resistive solenoid in the overlap region

Shiltsev et al., Phys. Rev. ST Accel. Beams **11**, 103501 (2008)

# Applications of electron lenses

## *In the Fermilab Tevatron collider*

- ▶ **long-range beam-beam compensation (tune shift of individual bunches)**
  - ▶ Shiltsev et al., Phys. Rev. Lett. **99**, 244801 (2007)
- ▶ **abort-gap cleaning (for years of regular operations)**
  - ▶ Zhang et al., Phys. Rev. ST Accel. Beams **11**, 051002 (2008)
- ▶ **studies of head-on beam-beam compensation**
  - ▶ Stancari and Valishev, FERMILAB-CONF-13-046-APC
- ▶ **demonstration of halo scraping with hollow electron beams**
  - ▶ Stancari et al., Phys. Rev. Lett. **107**, 084802 (2011)

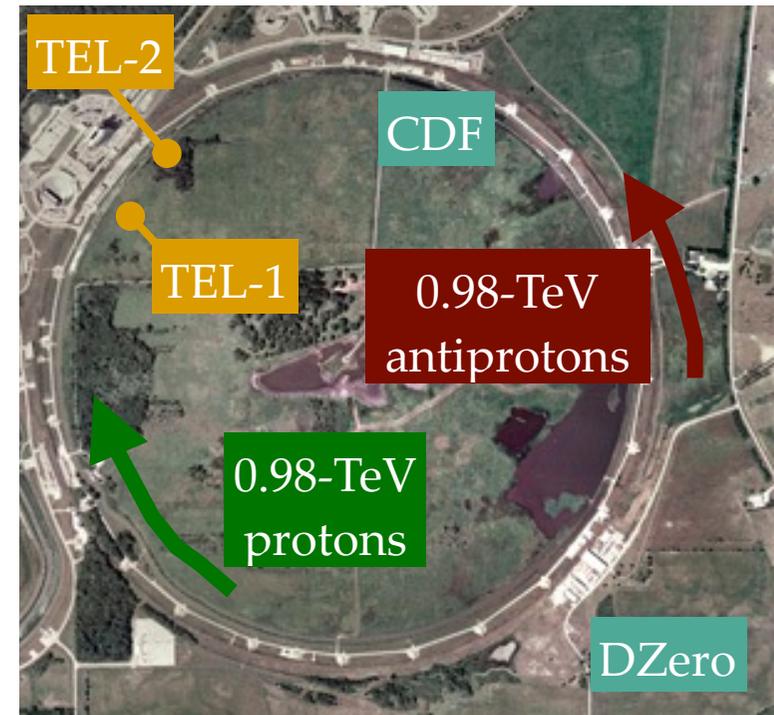
**Presently, used in RHIC at BNL for head-on beam-beam compensation, luminosity improvements**

- ▶ G. Robert-Demolaize, X. Gu, IPAC15

## **Current areas of research**

- ▶ **generation of nonlinear integrable lattices** in the Fermilab Integrable Optics Test Accelerator
- ▶ **hollow electron beam scraping** of protons in LHC
  - ▶ R. Bruce, IPAC15
- ▶ **long-range beam-beam compensation** as charged, current-carrying “wires” for LHC
  - ▶ A. Valishev, IPAC15
- ▶ to **generate tune spread for Landau damping** of instabilities before collisions in LHC

Tevatron electron lenses



2 km

# Nonlinear integrable optics with electron lenses

Use the electromagnetic field generated by the electron distribution to provide the desired nonlinear field.

Linear focusing strength on axis  $\sim 1/m$ :  $k_e = 2\pi \frac{j_0 L (1 \pm \beta_e \beta_z)}{(B\rho) \beta_e \beta_z c^2} \left( \frac{1}{4\pi\epsilon_0} \right)$ .

## 1. Axially symmetric thin kick of McMillan type

current density  $j(r) = \frac{j_0 a^4}{(r^2 + a^2)^2}$

transverse kick  $\theta(r) = \frac{k_e a^2 r}{r^2 + a^2}$

achievable  
tune spread  $\sim \frac{\beta k_e}{4\pi}$

**Larger tune spreads in IOTA**  
**More sensitive to kick shape**

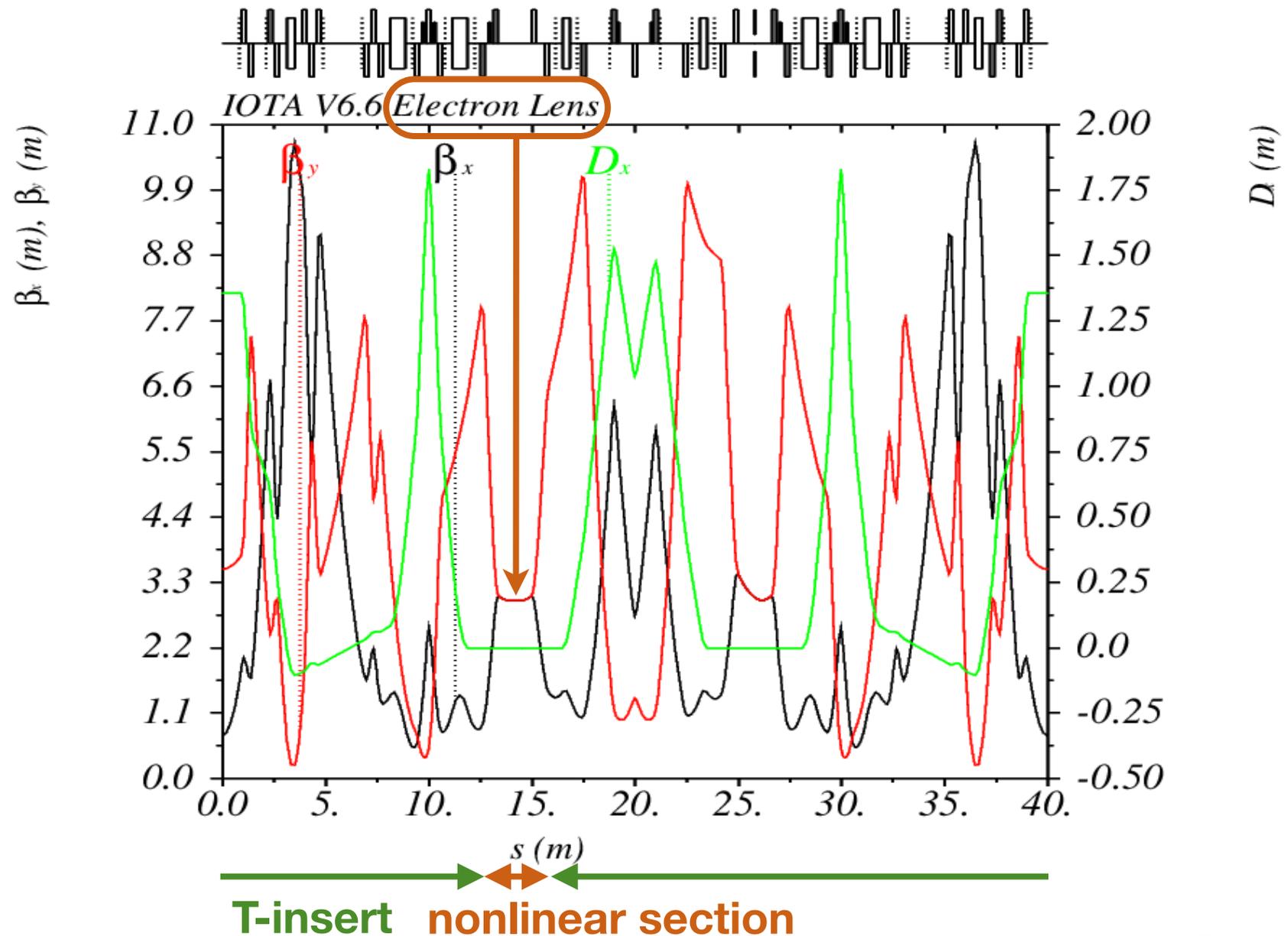
## 2. Axially symmetric kick in long solenoid

Any axially-symmetric current distribution

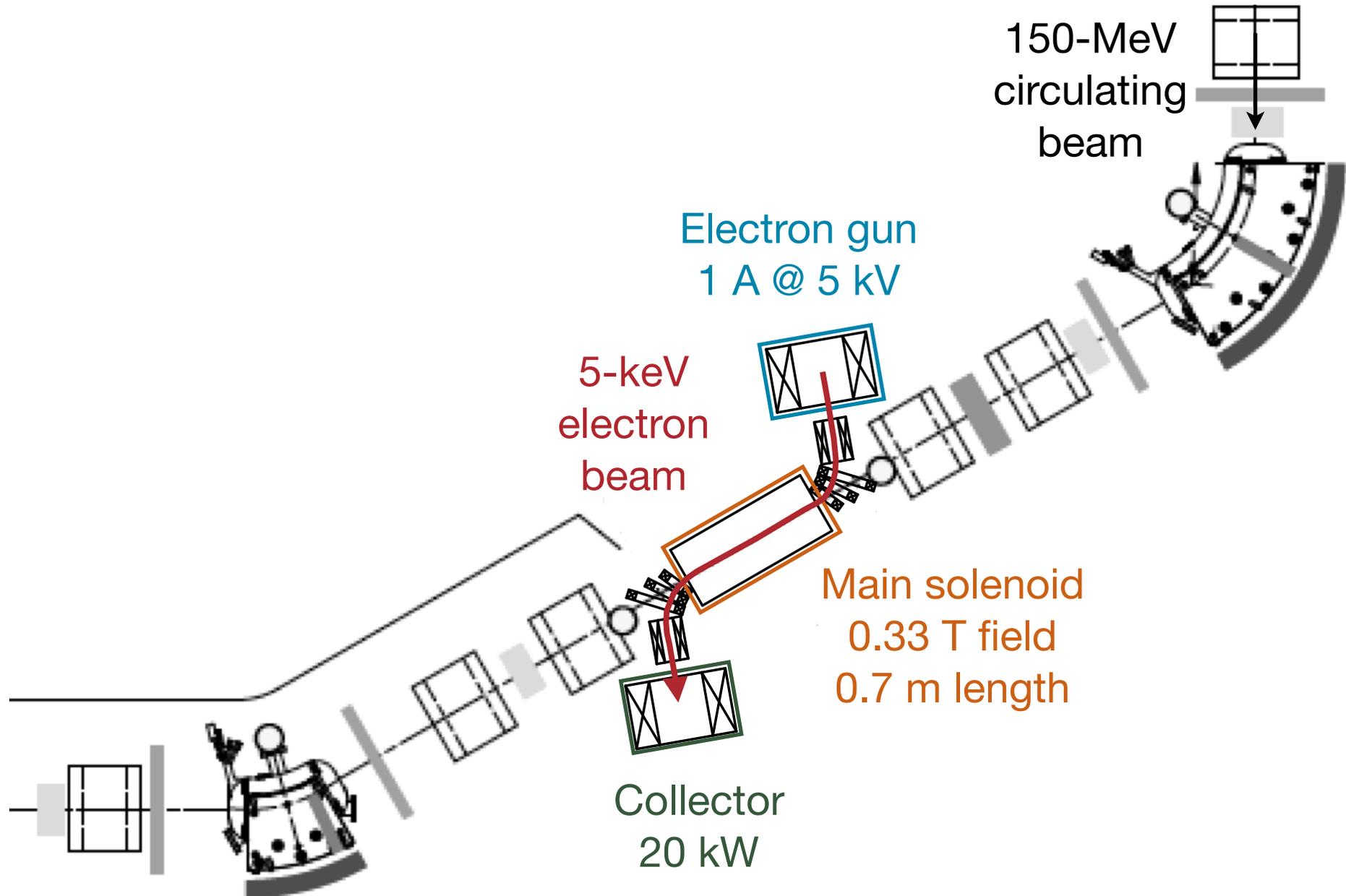
$$\sim \frac{L}{2\pi\beta} = \frac{LB_z}{4\pi(B\rho)}$$

**Smaller tune spreads in IOTA**  
**More robust**

# IOTA lattice with electron lens



# Electron-lens layout in IOTA

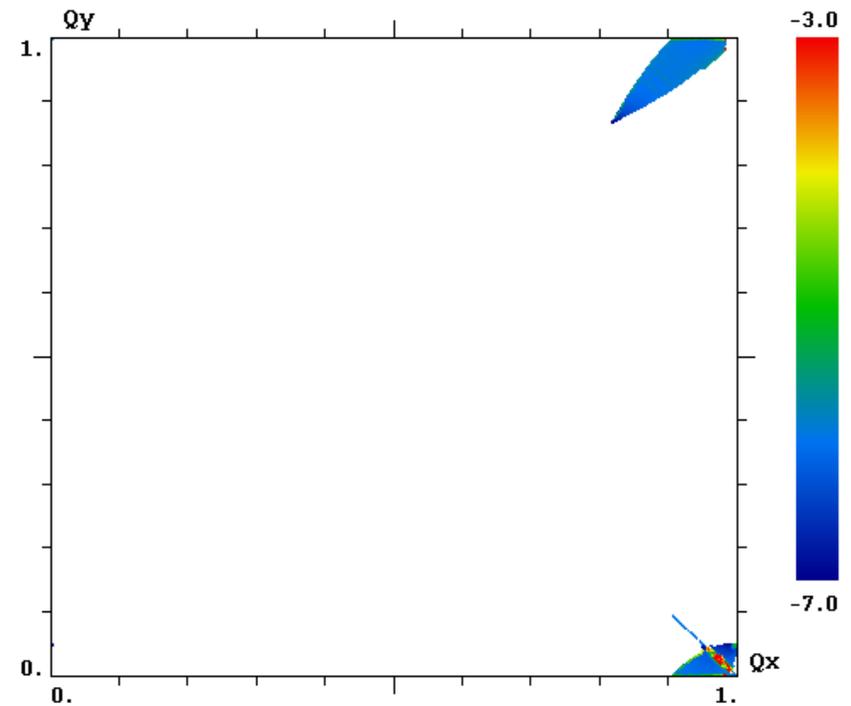
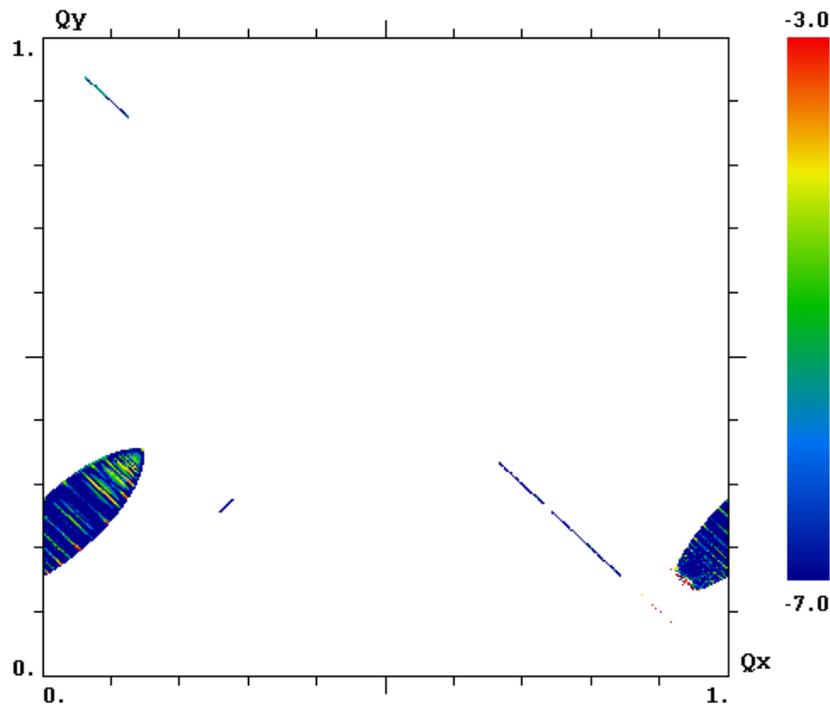


# First feasibility studies: tracking and stability

## 1. Axially symmetric thin-lens kick (extended McMillan case)

## 2. Axially symmetric time-independent Hamiltonian with thick lens

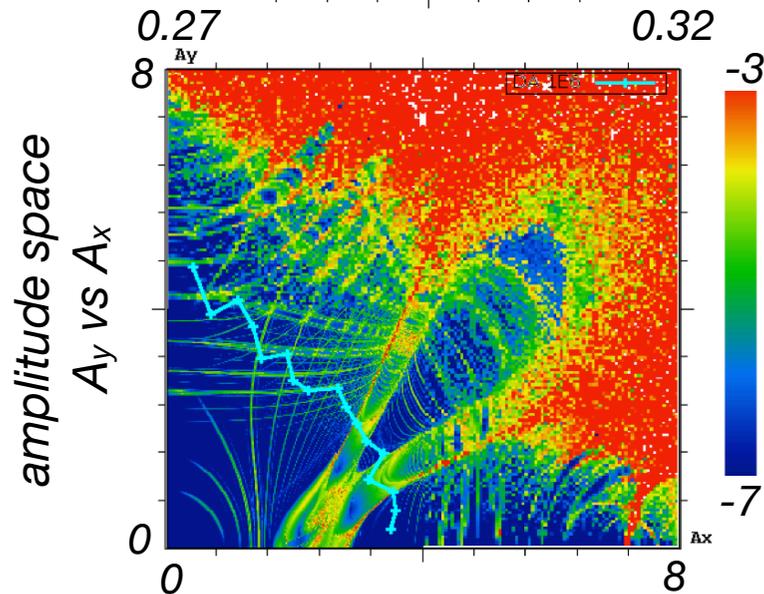
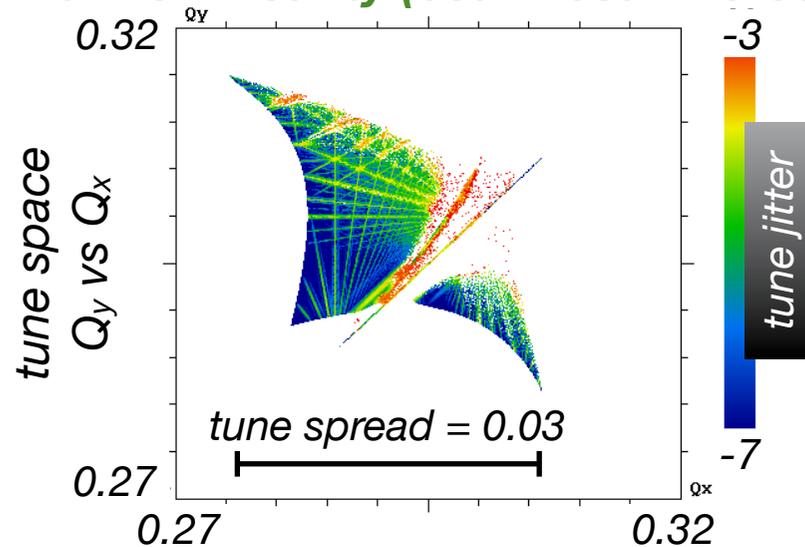
*Frequency-map analysis: tune jitter in tune space*



In both cases  
there are 2 transverse invariants  
the beam can cross integer resonances without particle loss

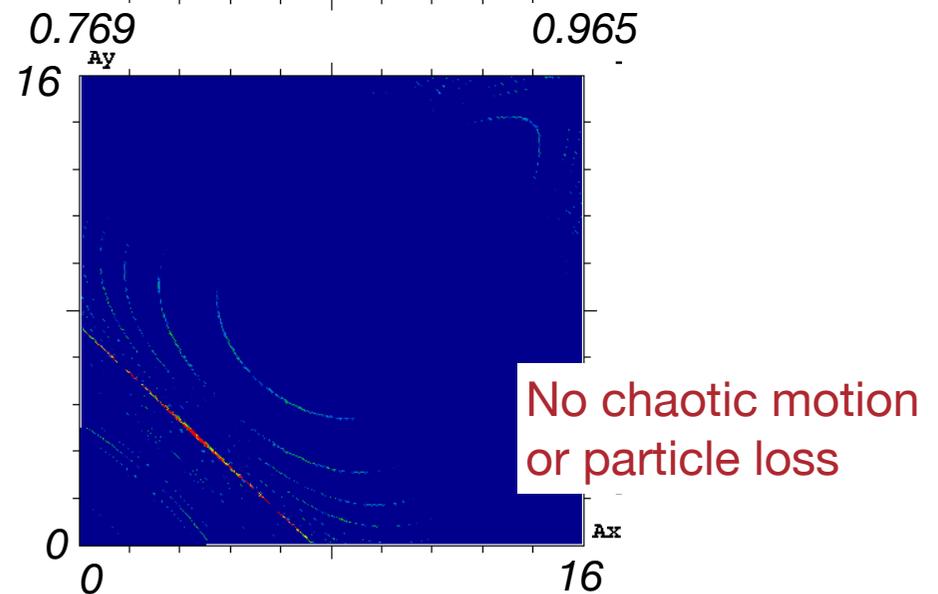
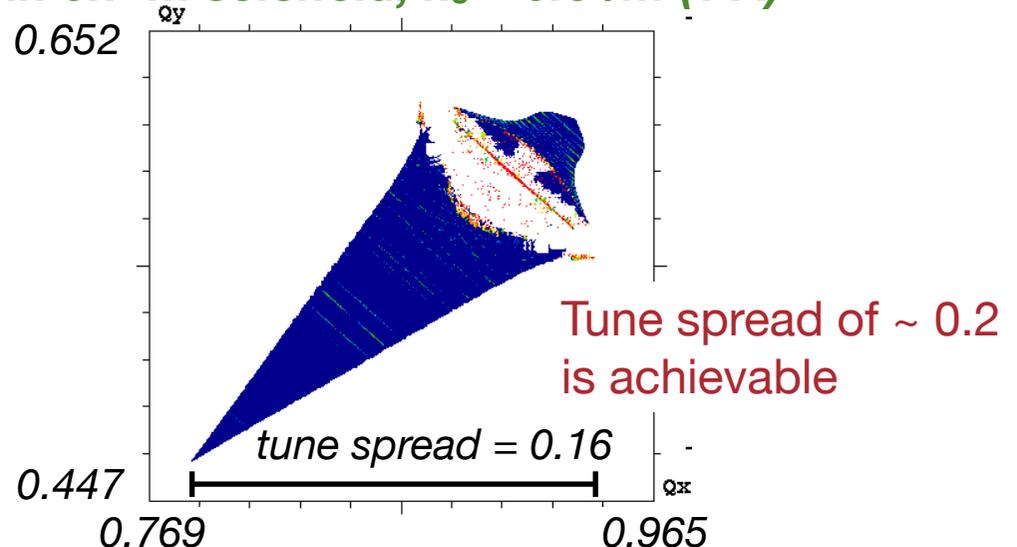
# Frequency maps: conventional vs. nonlinear integrable

*example of conventional machine with nonlinearity (beam-beam force)*

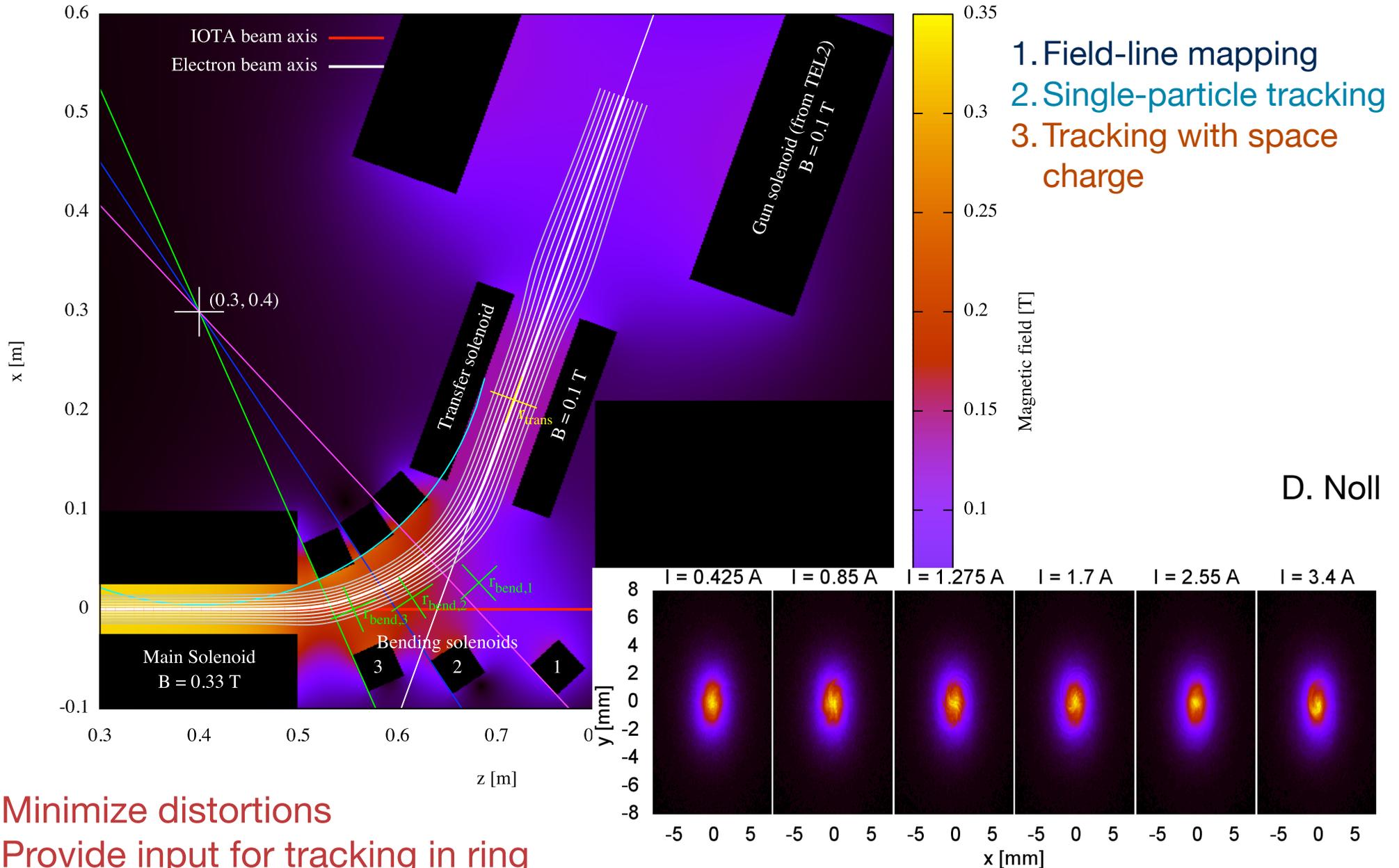


Resonance overlap, restricted dynamic aperture

*IOTA with nonlinear electron lens in 0.7-m solenoid,  $k_e = 0.6$  /m (1 A)*

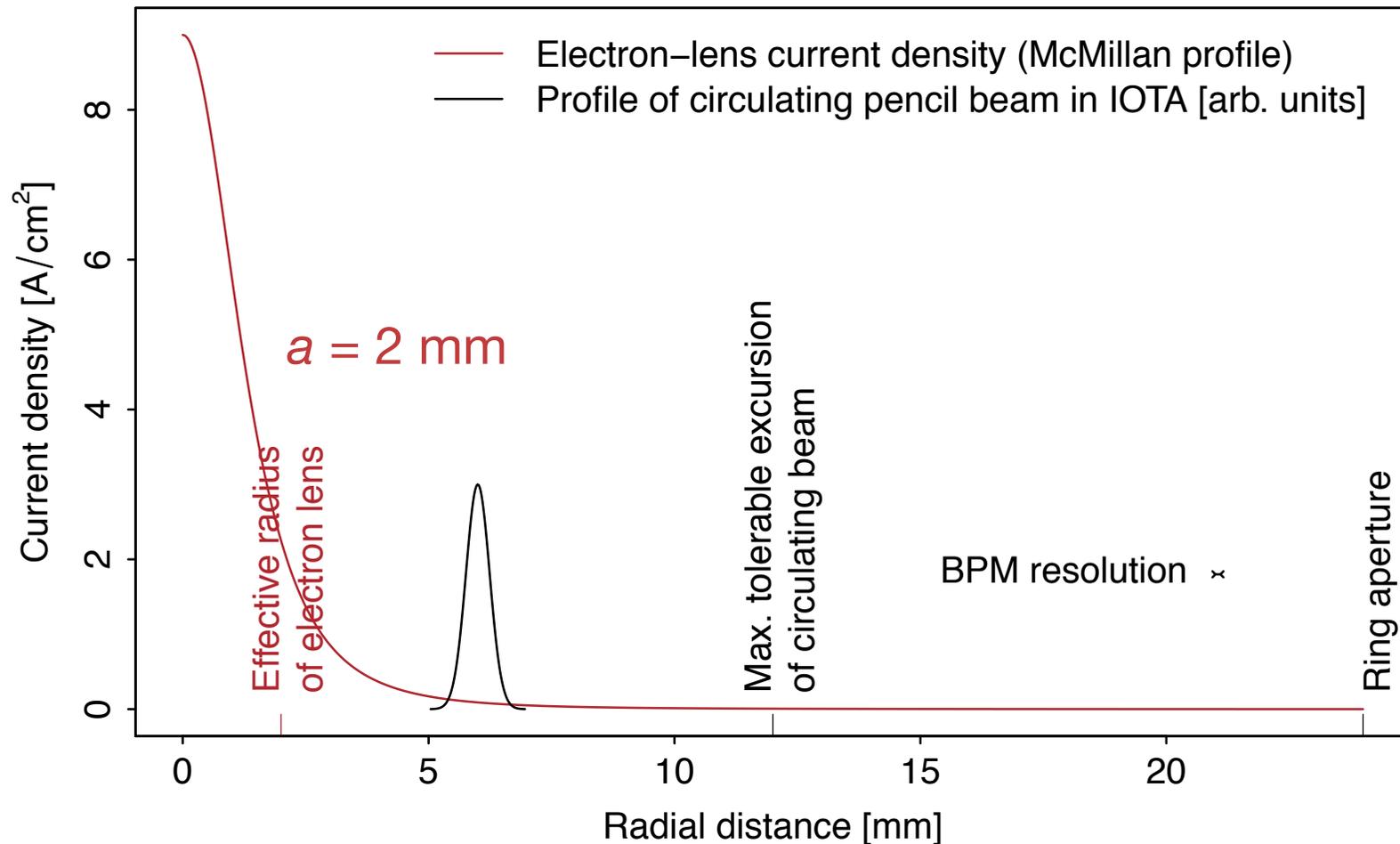


# Design of beam transport in electron lens



# Choice of electron-lens beam size for IOTA

Beam size in electron lens should allow the circulating pencil beam to sample a wide range of tunes, taking aperture and BPM resolution into account



small betatron amplitude: maximum detuning  
large betatron amplitude: negligible detuning

# Typical IOTA electron-lens parameters

Amplitude function	3 m
Circulating beam size (rms)	0.24 mm
Main solenoid length	0.7 m
Main solenoid field	0.33 T
Gun/collector solenoids	0.1 T
Cathode-anode voltage	5 kV
Beam current	1.1 A
Max. current density in overlap region	9 A/cm <sup>2</sup>
Effective radius in overlap region	2 mm
Max. radius in overlap region	12 mm
Effective radius at cathode	3.6 mm
Max. radius at cathode	22 mm

# Next steps

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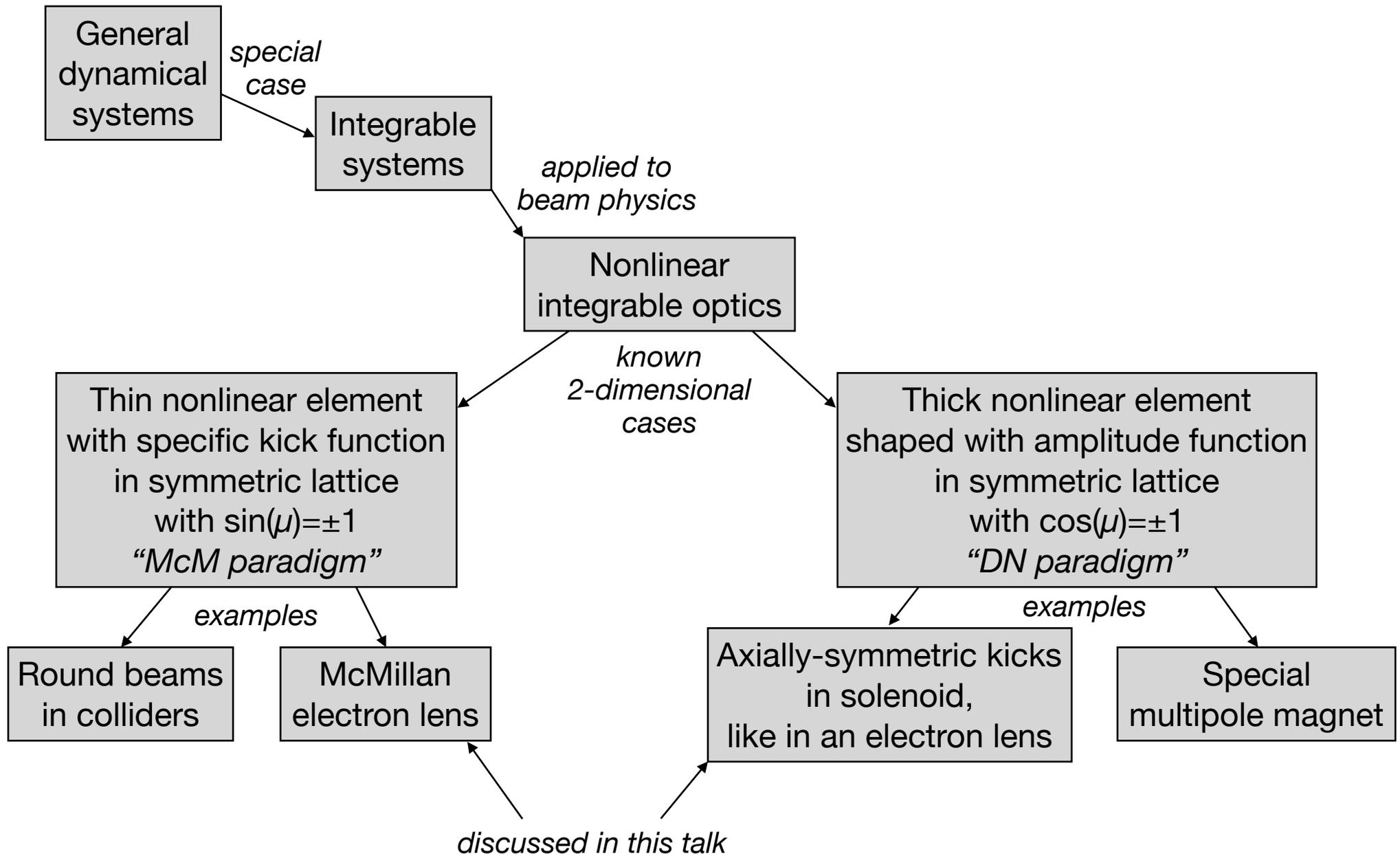
Several effects need to be accurately studied, for instance:

- lattice deviations from ideal case
- impact of chromaticity-correction sextupoles on integrability
- azimuthal asymmetries in electron-lens kicks
- effect of fringe fields on ring optics
- perveance of electron gun and accuracy of beam profile
- chromatic effects of the electron lens
- misalignments

These studies will be based on numerical simulations and on experiments at the Fermilab electron-lens test stand

see also  
S. Webb, IPAC15  
K. Ruisard, IPAC15

# Summary: a concept map



# Conclusions

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- ▶ An **exciting program of general physics and accelerator science** is planned for the Fermilab IOTA/ASTA facility [recent workshop: [indico.fnal.gov/event/9734](http://indico.fnal.gov/event/9734)]
  - ▶ nonlinear integrable lattices
  - ▶ space-charge dynamics
  - ▶ optical stochastic cooling
  - ▶ single-electron quantum optics
  - ▶ high-brightness beams and radiation
- ▶ Experiments and theory of **nonlinear integrable dynamics**
  - ▶ advance the knowledge of dynamical systems in many fields of science
  - ▶ in accelerator physics, they provide a path towards the next generation of high-power machines
- ▶ Research on **electron lenses**
  - ▶ provides a flexible way to implement nonlinear integrable lattices in accelerators
  - ▶ is connected to other applications in beam physics (collimation, beam-beam compensation)
- ▶ New **collaborators** and **ideas** are always welcome. Also, Fermilab currently has a few **job openings** in accelerator physics.

Backup slides

# IOTA experimental program

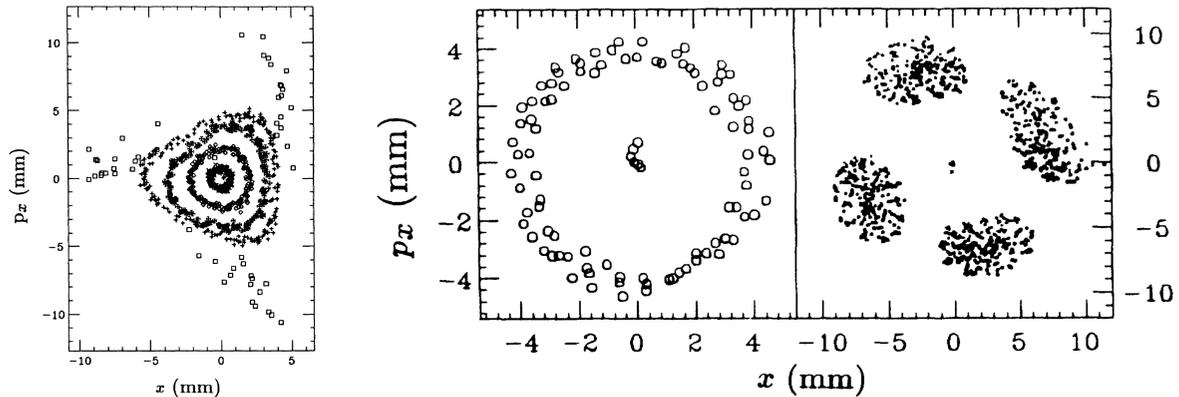
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- **Single-particle motion with electron beams (Phase I)**
  - measure and control **closed orbit and lattice** with required precision
  - implement
    - quasi-integrable optics with **octupoles** and
    - integrable optics with **nonlinear magnets** and **electron lens**
  - **kick electron bunch transversely** and **record turn-by-turn intensities, beam positions, and sync-light profiles**
  - paint aperture to measure **detuning vs. amplitude** and **dynamic aperture** (synchrotron damping helps to cover available phase space)
  - **cross resonances** without loss of intensity
  - **test robustness** of nonlinear system against perturbations and imperfections
- Main goal: achieve 0.25 tune shift without loss of dynamic aperture

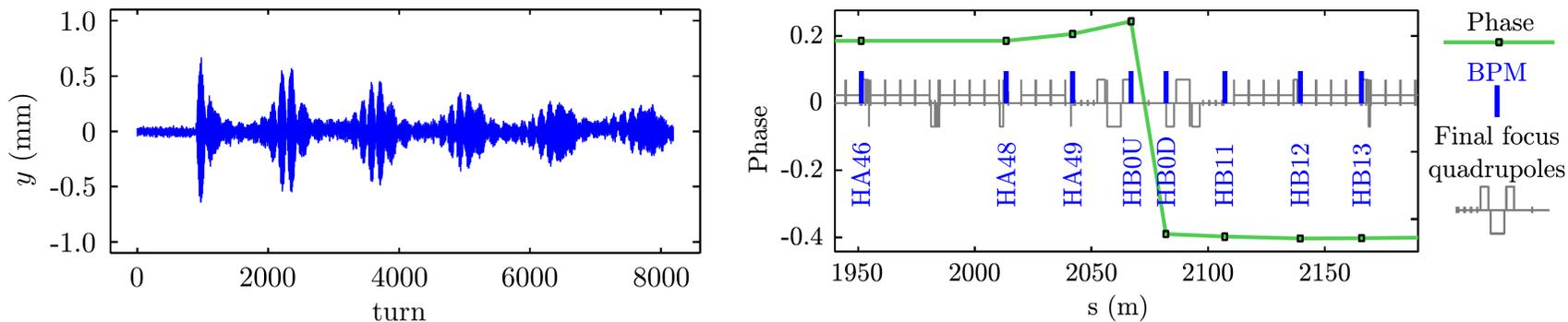
# From linear lattice to nonlinear dynamics

After establishing precise linear lattice, main goal is to observe detuning and lifetime vs. amplitude. Some measurements will be based on experimental techniques used at IUCF Cooler Ring and Fermilab Tevatron

Experimental Poincaré maps at IUCF [e.g., Caussyn et al., PRA **46**, 7942, (1992)]



Model-independent analysis of Tevatron turn-by-turn data, including coupling and shifted-BPM constraints [Petrenko et al., PRSTAB **14**, 092801 (2011)]



# IOTA experimental program

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- Proton injection (Phase II)
  - inject **2.5-MeV protons** from RFQ
  - achieve **0.6 space charge tune shift**
  - investigate **integrable optics with protons and space charge**
  - study **space-charge dynamics**
  - **space-charge compensation** experiments with **electron columns**
- Other experiments under consideration
  - optical stochastic cooling demonstration
  - single-electron radiation emission

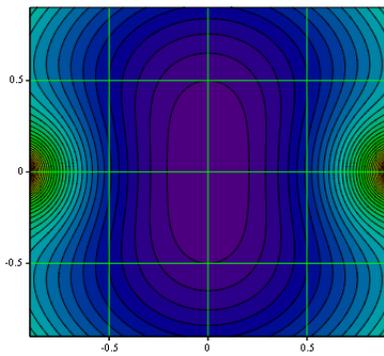
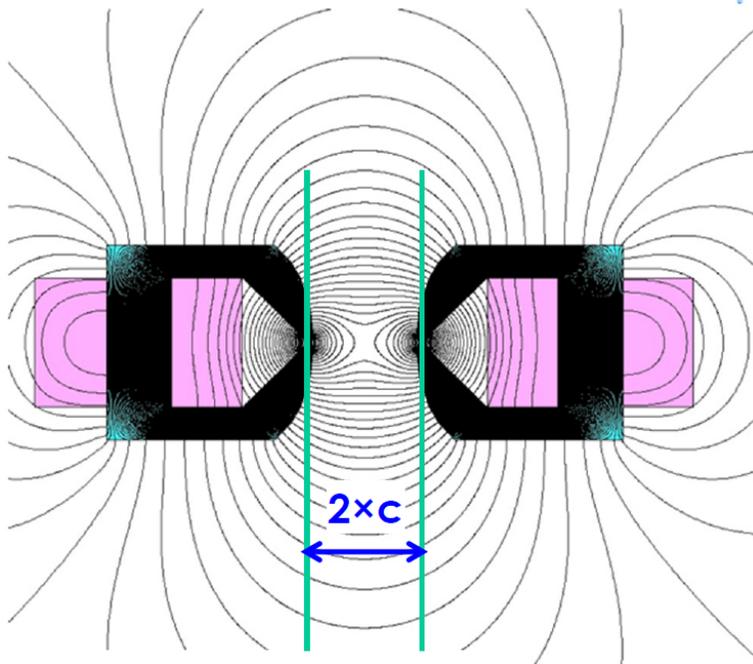
# Schedule and plans

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- 2015–2017
  - complete ASTA injector
  - start research program with injector
  - build IOTA
  - commission proton injector
  - commission IOTA with electrons
  - single-particle dynamics experiments with electrons
- 2018–2020
  - commission IOTA with protons
  - first space-charge experiments
- 2021 —
  - apply results to next generation of high-intensity machines
  - expand program to serve accelerator and particle physics communities

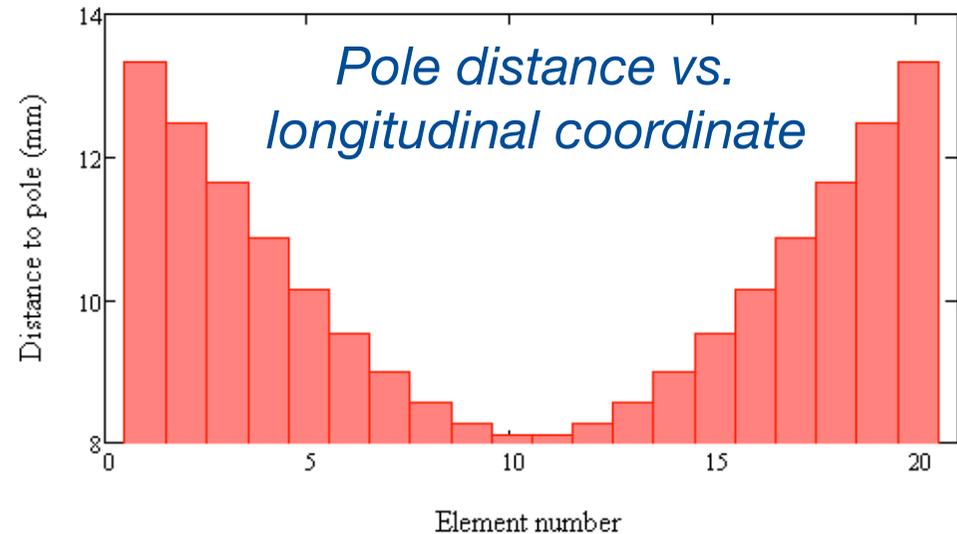
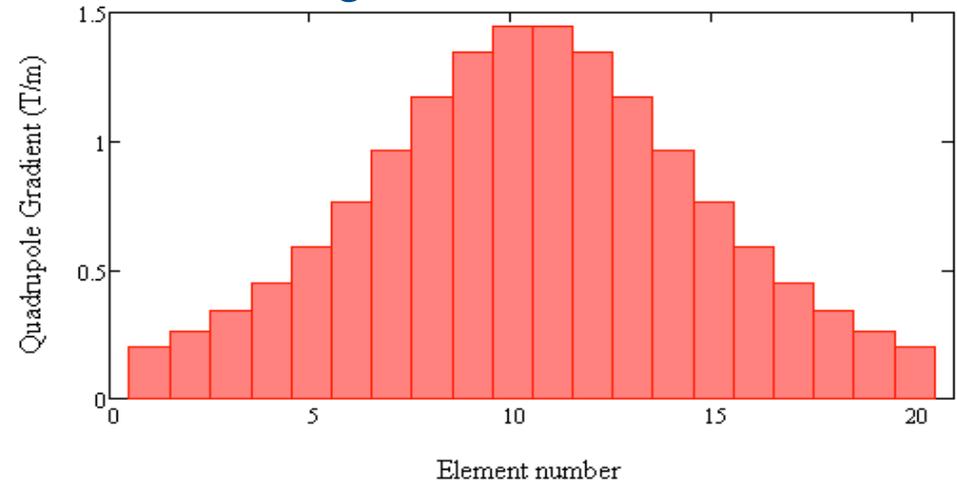
# The nonlinear magnet

The nonlinear element is a special multipole with longitudinally dependent strength and geometry



*Magnetic field and potential*

*Quadrupole component vs. longitudinal coordinate*



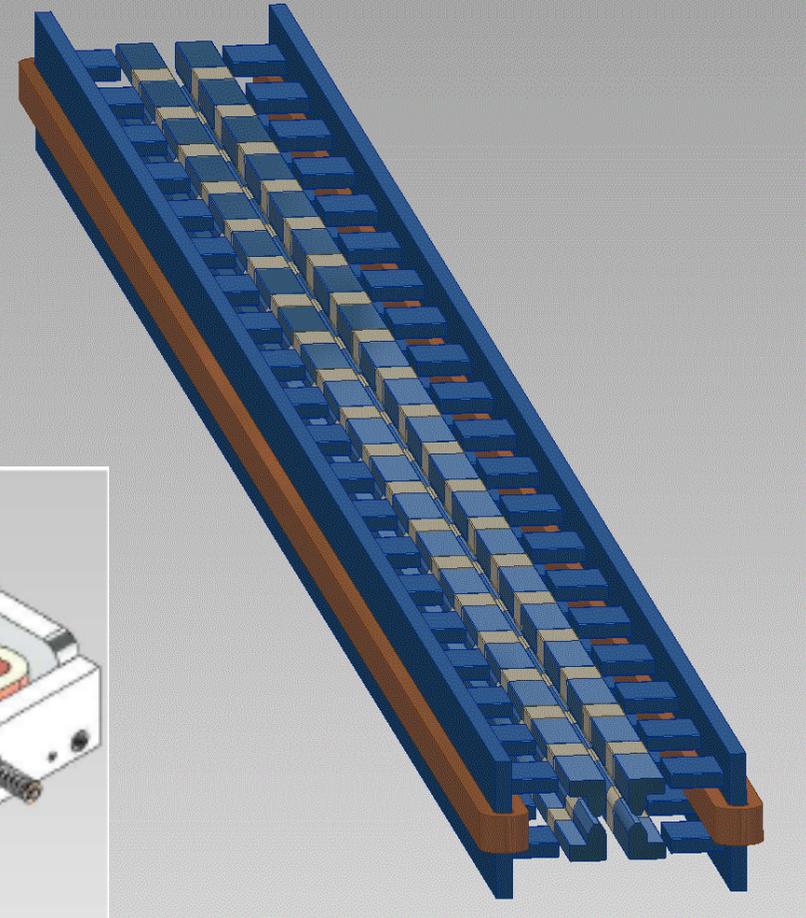
# The nonlinear magnet

*Fermilab design  
with 20 segments*

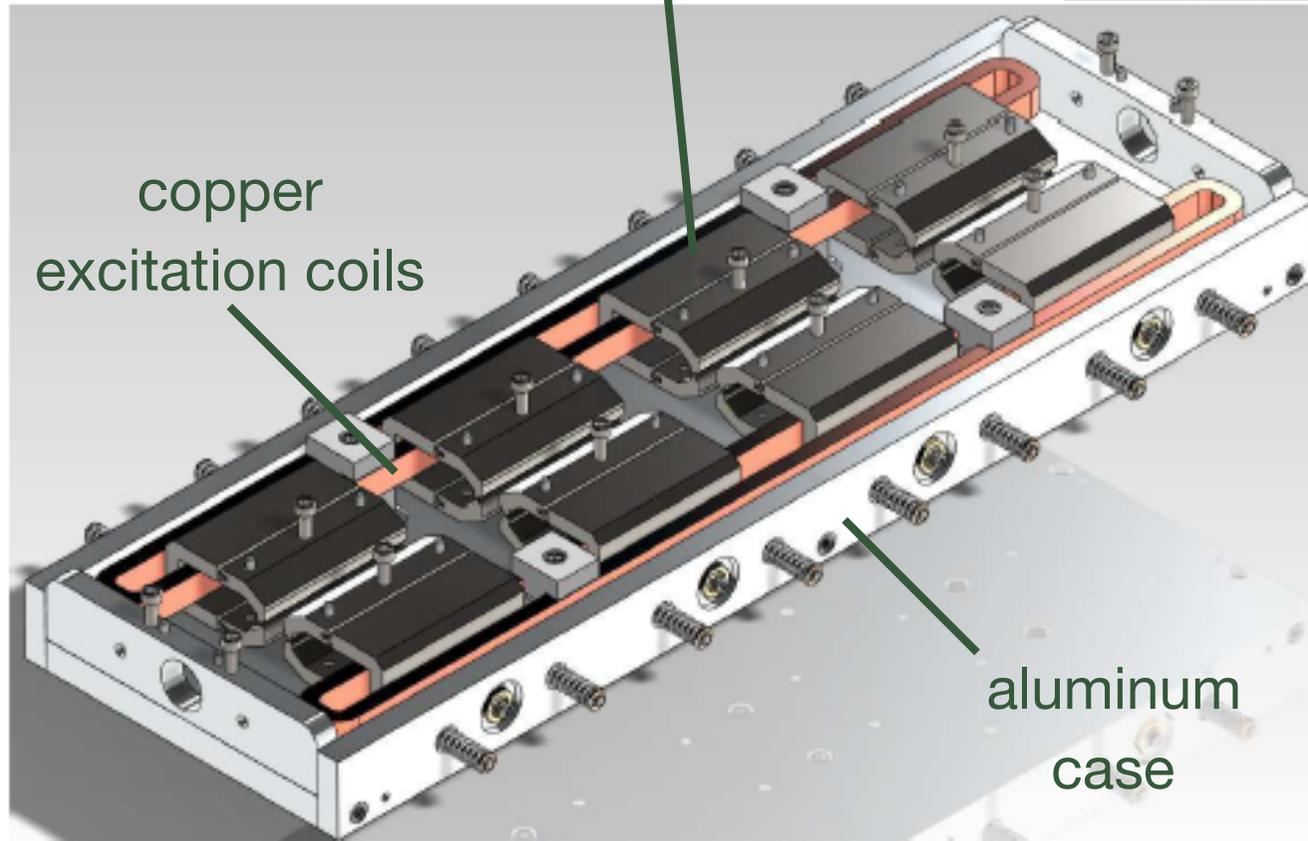
stainless-steel poles  
and return yokes

copper  
excitation coils

aluminum  
case



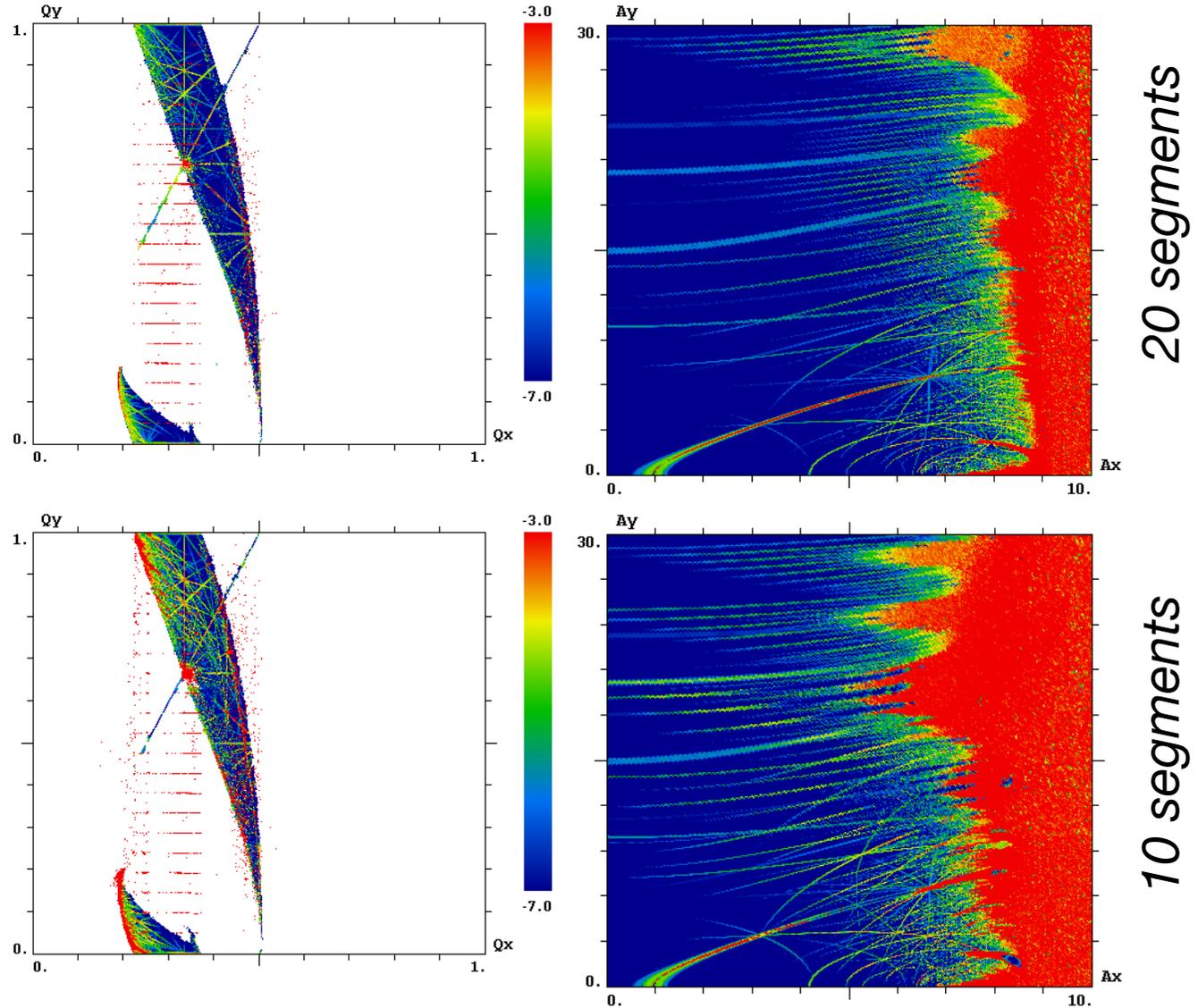
*Radiabeam prototype  
with 4 segments*



# Tracking simulations with nonlinear magnets

Frequency-map analysis in tune and amplitude spaces (Lifetrac code)

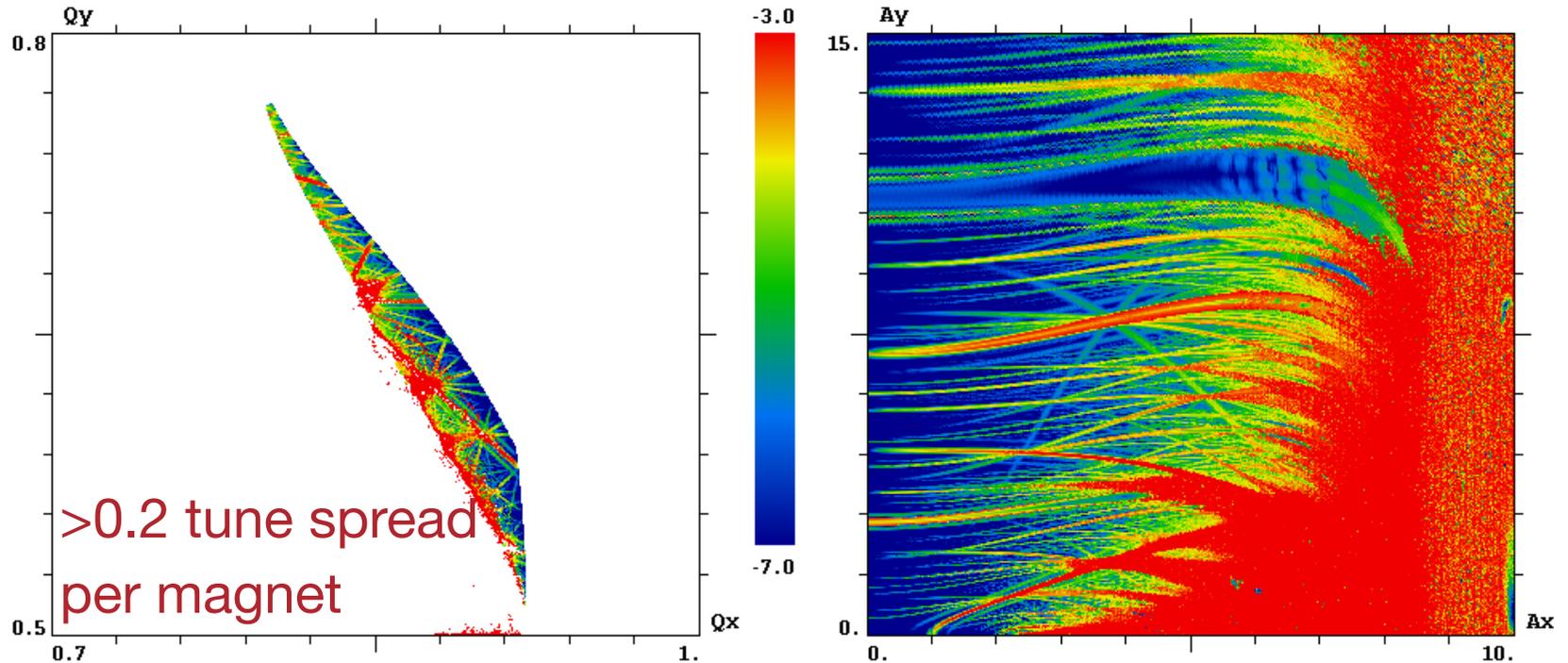
Very large tune spread,  
crossing integer  
resonance, with no  
lifetime degradation



No resonance overlap, stochastic layers, or diffusion

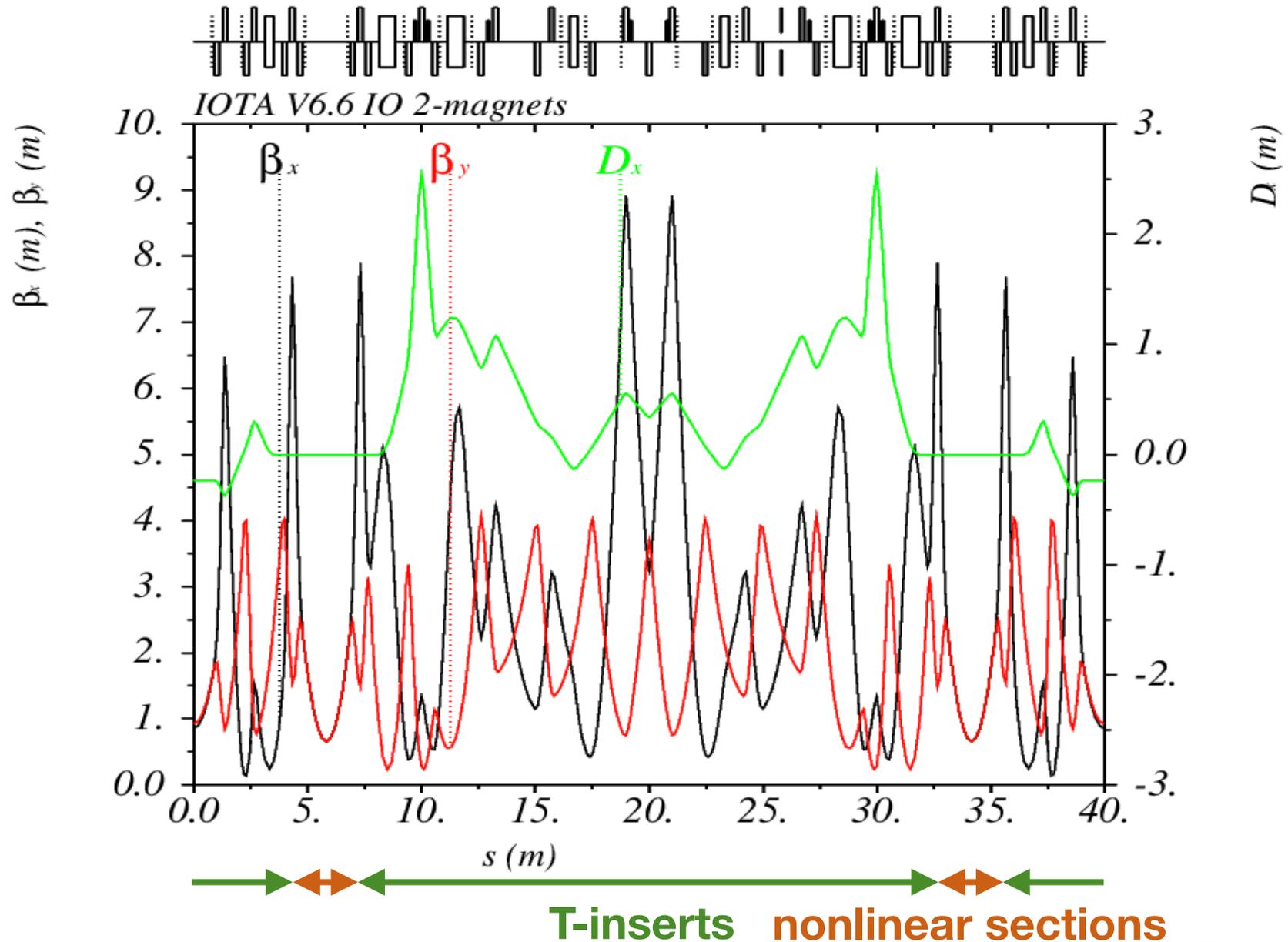
# Tracking with imperfections

Including misalignments, tilts, gradient errors, lattice imperfections

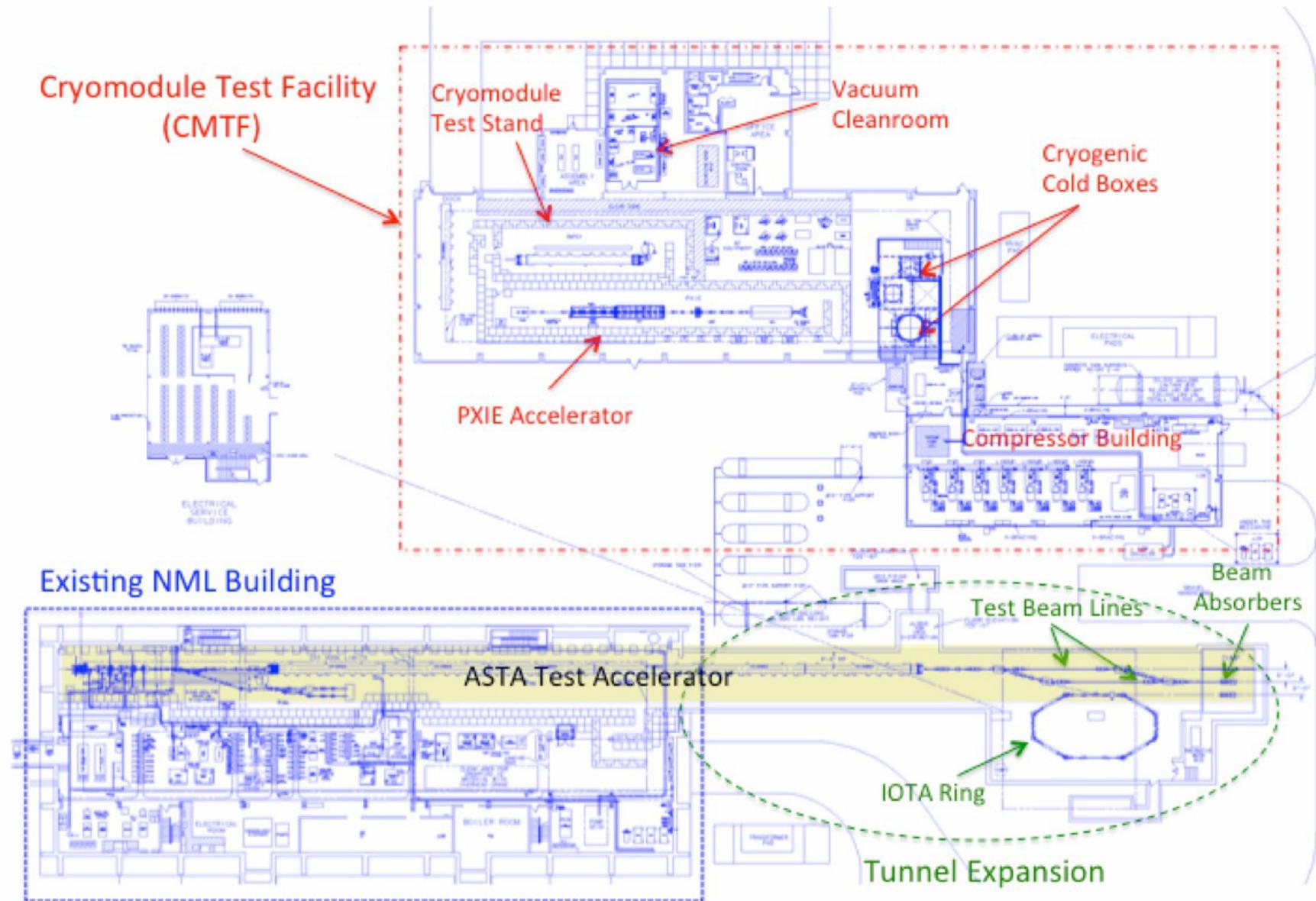


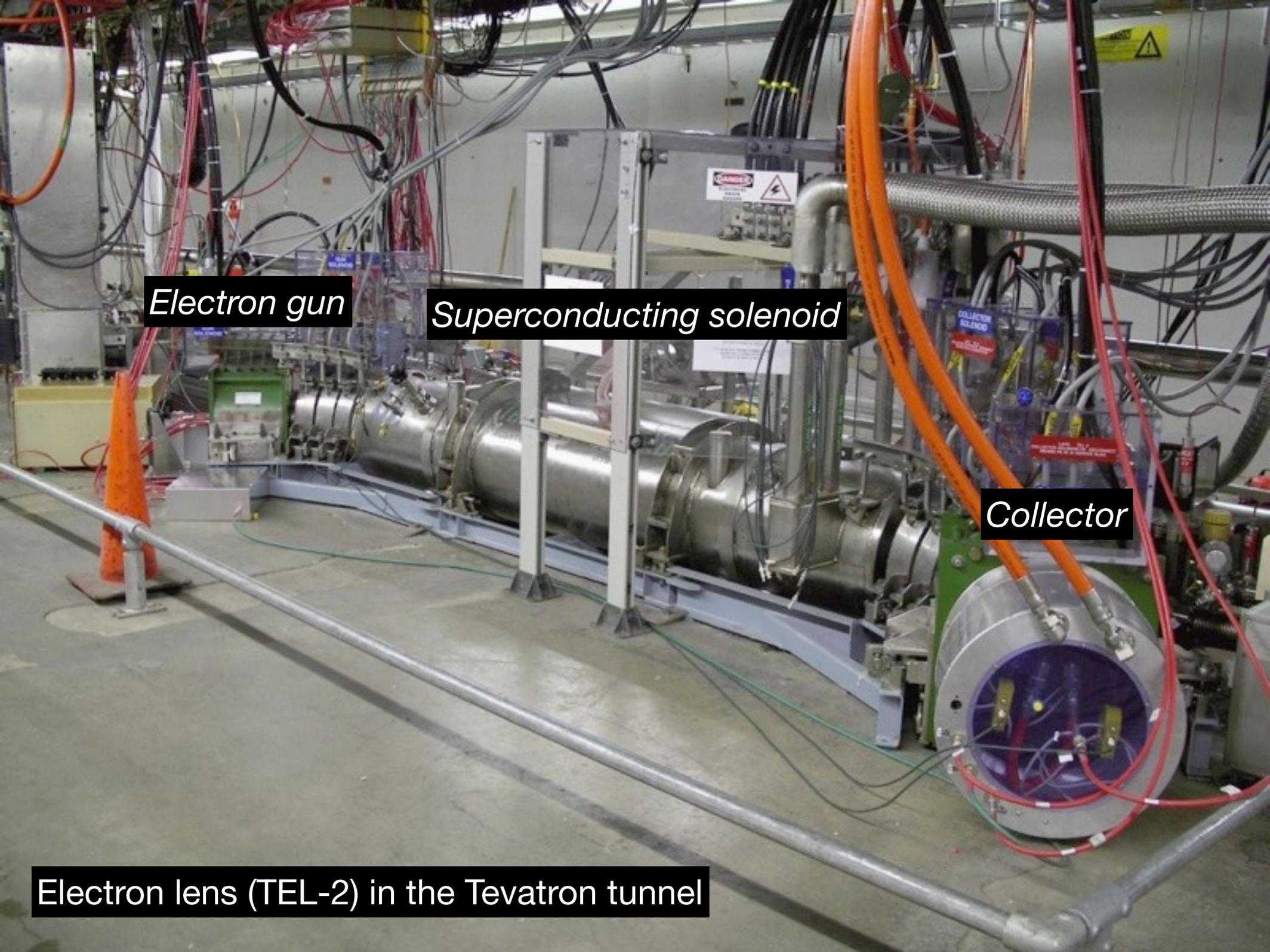
Simulations suggest that a proof-of-principle experiment to demonstrate large tune spreads with acceptable lifetimes is feasible

# IOTA lattice with 2 nonlinear magnets



# Floor plan of the IOTA/ASTA facility





*Electron gun*

*Superconducting solenoid*

*Collector*

Electron lens (TEL-2) in the Tevatron tunnel

# IOTA components

