



Demonstration of Efficient Electron- Radiation Coupling in a 7th Harmonic IFEL Interaction Experiment

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High-order Harmonic FELs For UV and X-ray Production

Coherent X-Ray Production in a single-pass FELs with a fixed e-beam energy
SLAC LCLS (USA), DESY European XFEL (Germany), and SCSS (Japan)

14 GeV e-beam

Undulator
 $L \sim 100 \text{ m}; \lambda_u = 3.3 \text{ cm}; K = 3.7$

0.1 nm X-ray Self-Amplified Spontaneous Emission

$$\lambda_{Xray} = \frac{\lambda_u}{2\gamma^2 n} \left(1 + \frac{K^2}{2} \right)$$

$n=1$ fundamental frequency

When $K > 1$

$n=3,5,7 \dots$ high-order FEL resonances

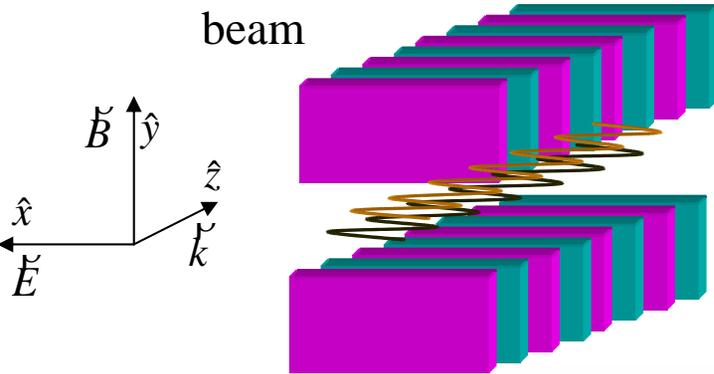
High-Order FEL Interactions are considered both for SASE and seeded cascade FELs

- +) $n\lambda$ choice for the seed
- ++) γ can be \sqrt{n} smaller
- +++) λ_u can be larger and K

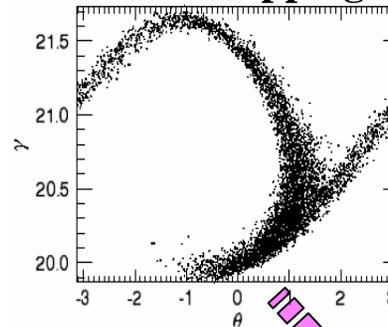


Seeded FEL/IFEL interactions

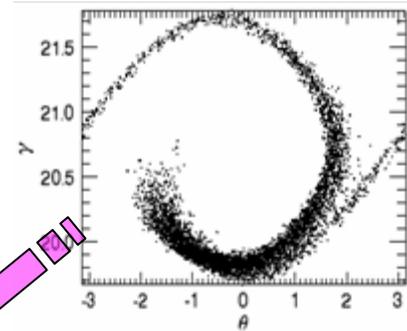
Laser + electron beam



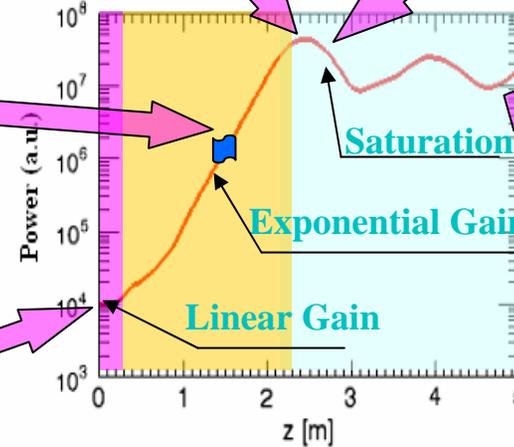
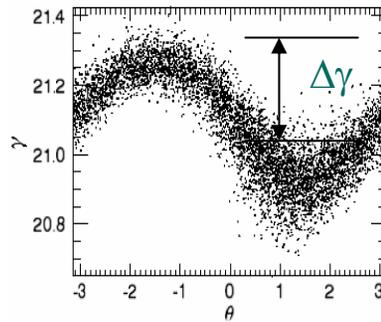
Trapping



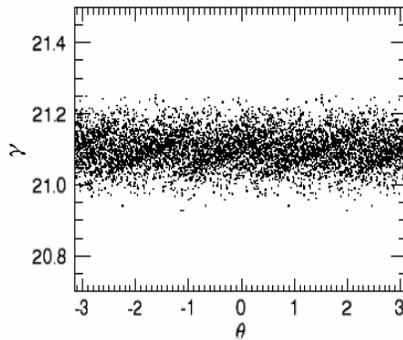
Saturation (Out of resonance)



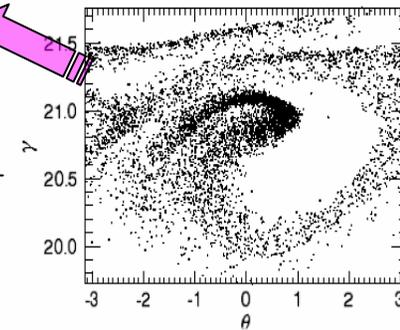
 Sinusoidal Modulation



Initial state



Typical radiation power plot



Totally trapped in the ponderomotive "bucket"



Harmonic coupling in an IFEL undulator

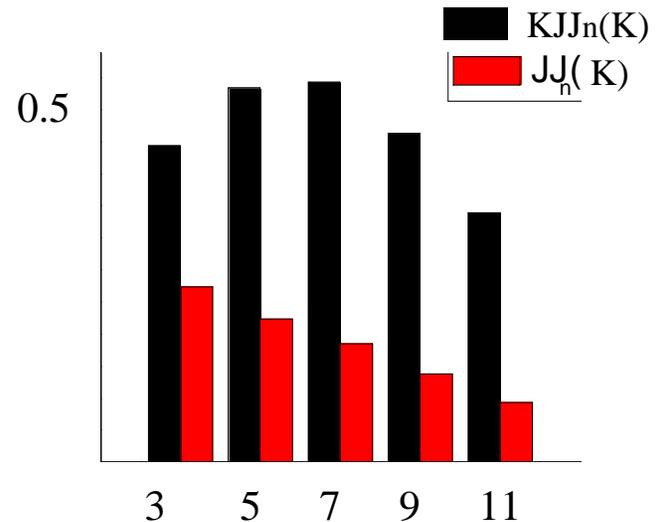
If $K \geq 1$, transverse motion is relativistic and spectrum of the undulator radiation gains odd harmonics $n=3,5,7 \dots$

$$\lambda_{seed} = \frac{\lambda_u}{2\gamma^2 n} \left(1 + \frac{K^2}{2} \right)$$

Lorentz Force IFEL equations

$$\frac{\partial \gamma}{\partial z} = \frac{ka_0 K}{2\gamma} \sum_n J J_n \sin(\psi + k_u z(n-1))$$

$$\frac{\partial \psi}{\partial z} = k_u - k \frac{1 + K^2 / 2 + \gamma^2 \theta^2}{2\gamma^2}$$

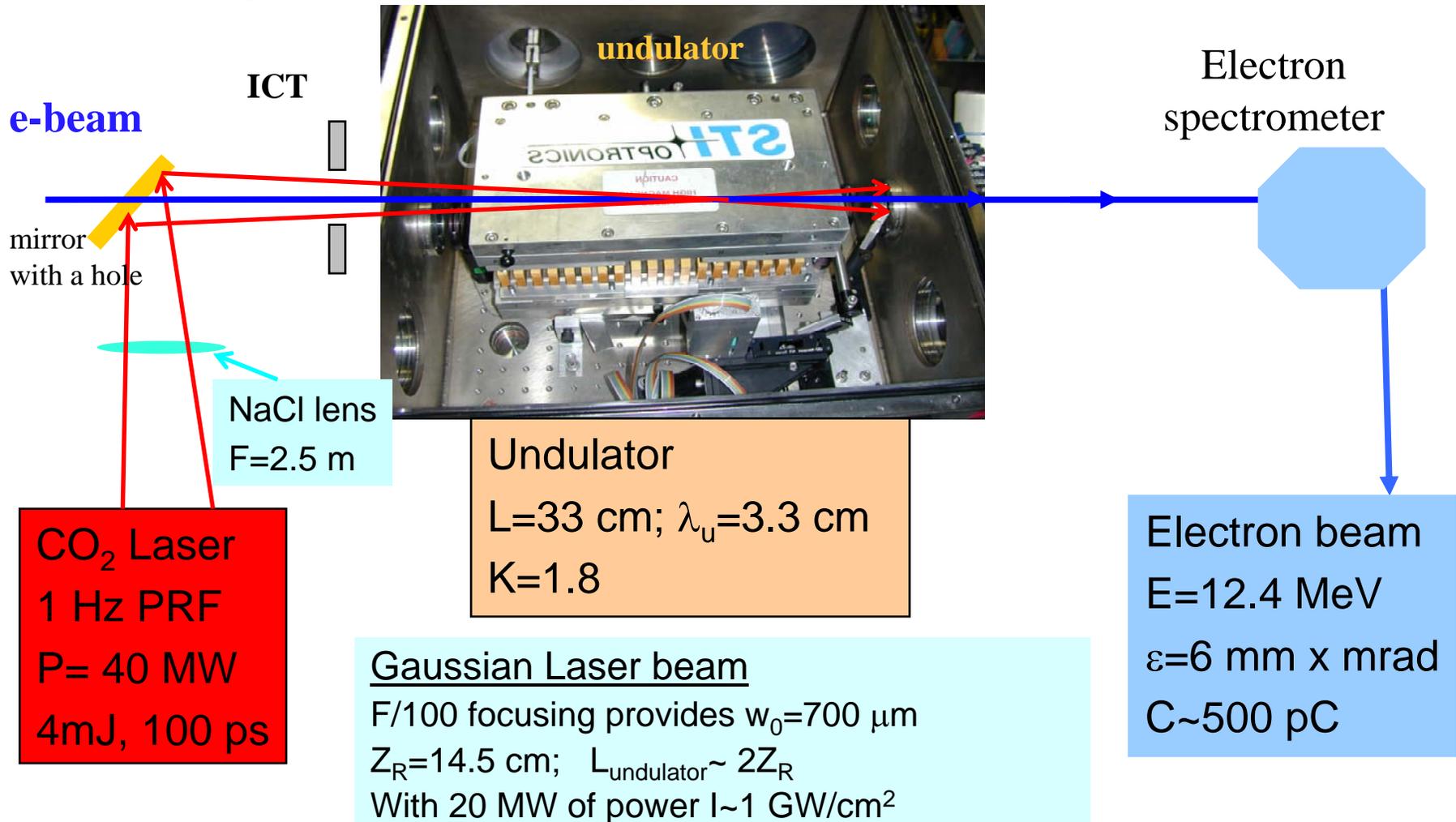


$$\lambda_u = 3.3 \text{ cm}, K = 1.8$$



7th order IFEL experiment at the UCLA Neptune Laboratory

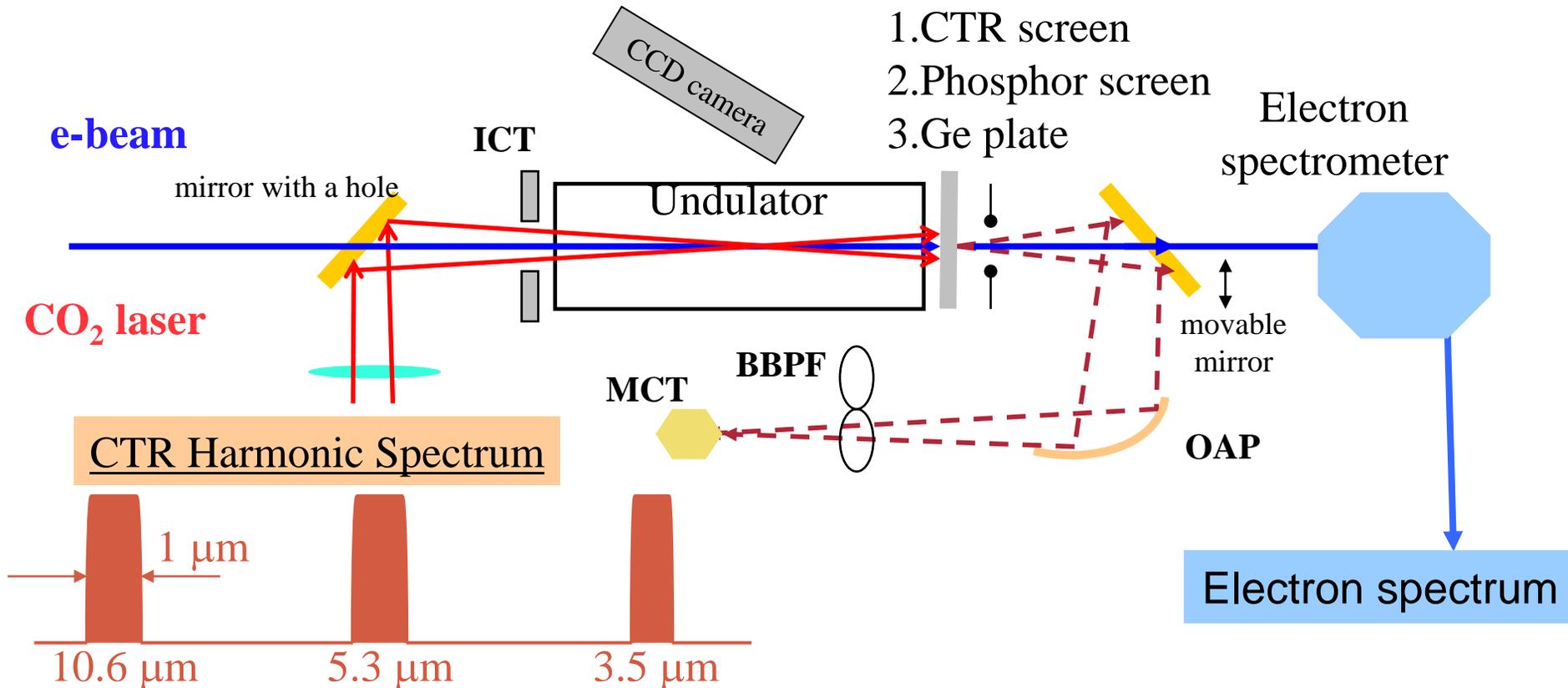
Microbunching in the undulator using 7th order IFEL interactions $10.6 \mu\text{m} \times 7 = 74.2 \mu\text{m}$





CTR Diagnostic for Bunched Beam

Microbunching on fundamental $\lambda_{mb} \sim 10.6 \mu\text{m}$, 2nd- $\lambda_{mb} \sim 5.3 \mu\text{m}$ and 3rd- $\lambda_{mb} \sim 3.5 \mu\text{m}$ harmonics

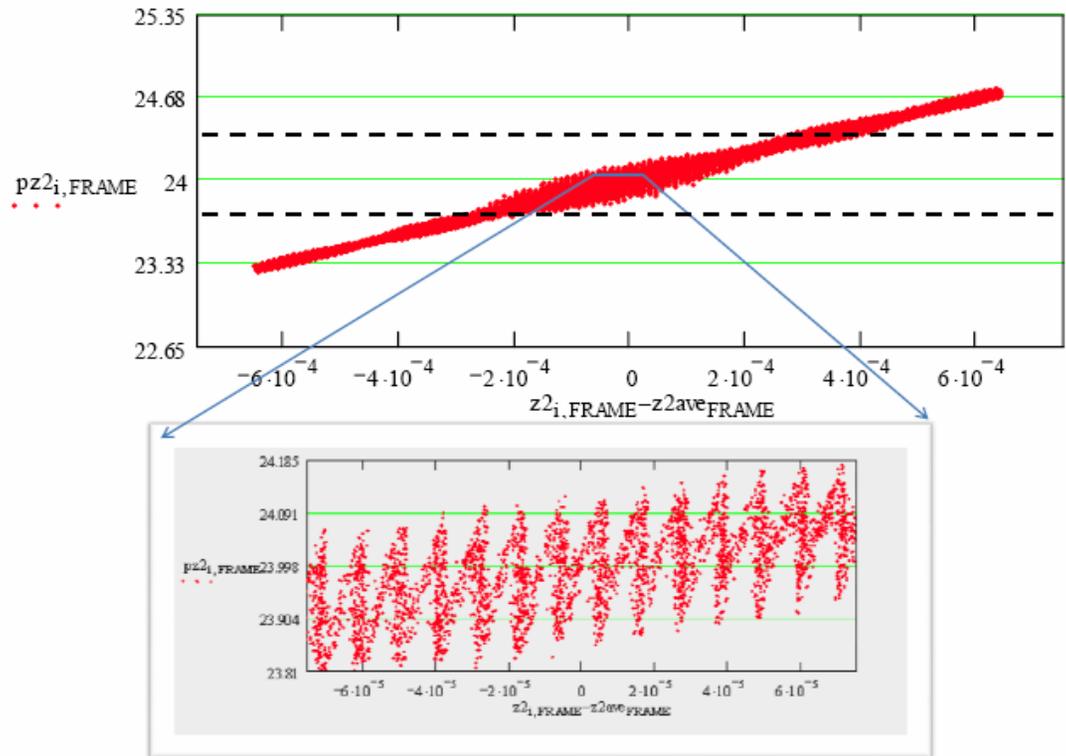
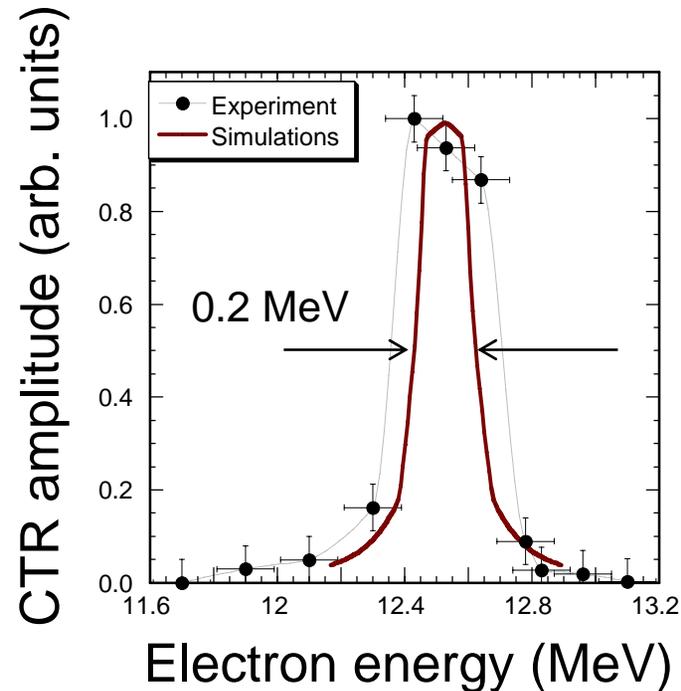


A set of BBPF filters provides an adequate determination of harmonic content. Background is down to $\sim 0.5 \mu\text{J}$, the S/N ratio is 200-2.



Resonant Condition for 7th order IFEL

A correlated rms energy spread is 0.7% measured with and without the undulator

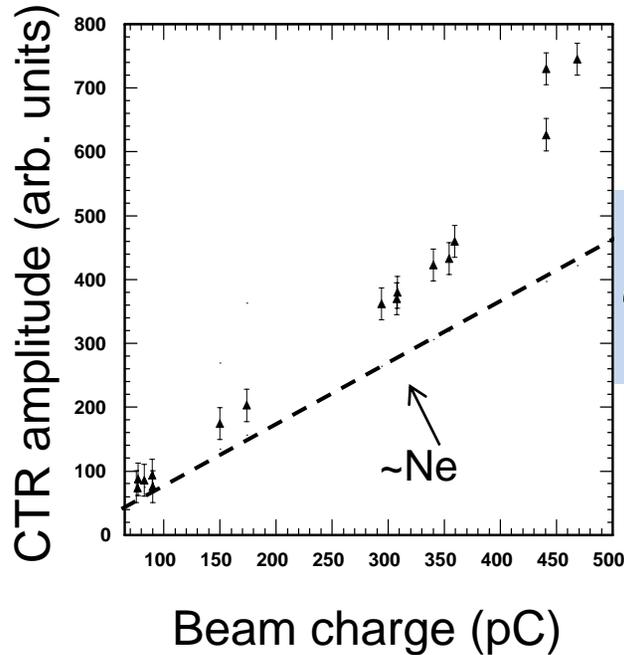


A slice of the beam over which the IFEL interactions take place is $100\mu\text{m}$ (~ 300 fs), results in effective energy spread of 0.02% and provides microbunching of almost the whole beam or part of the beam at a detuned energy.



CTR scaling

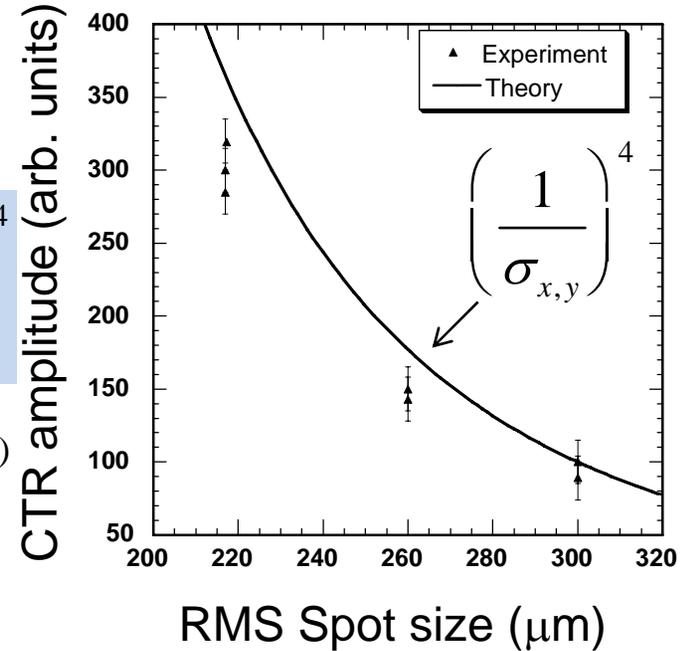
The CTR signal on fundamental versus the charge and the spot size on the screen.



Normal incidence
Forward CTR:

$$U_h \approx \frac{N^2 e^2 b_h^2}{4\sqrt{\pi}\sigma_z} \left(\frac{\gamma}{hk_r}\right)^4 \left(\frac{1}{\sigma_{x,y}}\right)^4$$

A. Tremaine, PRL 81,5816(1998)



Clear nonlinear CTR signal increase versus charge was observed.

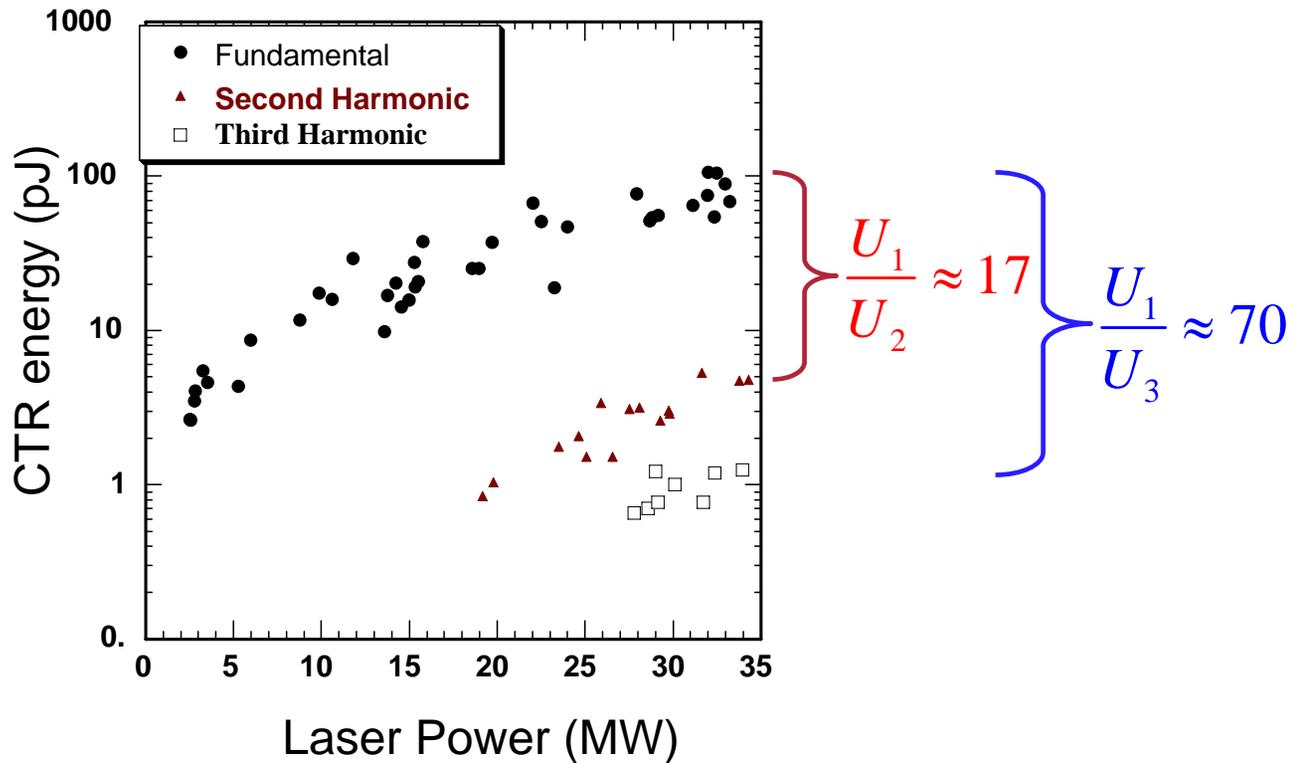
Strong $(1/\sigma_{x,y})^4$ scaling is very close to one observed in the experiment.



Harmonics of the Bunched Beam

Microbunching on fundamental $\lambda_{mb} \sim 10.6 \mu\text{m}$, 2nd- $\lambda_{mb} \sim 5.3 \mu\text{m}$ and 3rd- $\lambda_{mb} \sim 3.5 \mu\text{m}$ harmonics.

$$\frac{U_1}{U_h} \approx \frac{N_1^2 b_1^2}{N_h^2 b_h^2} (h)^4$$

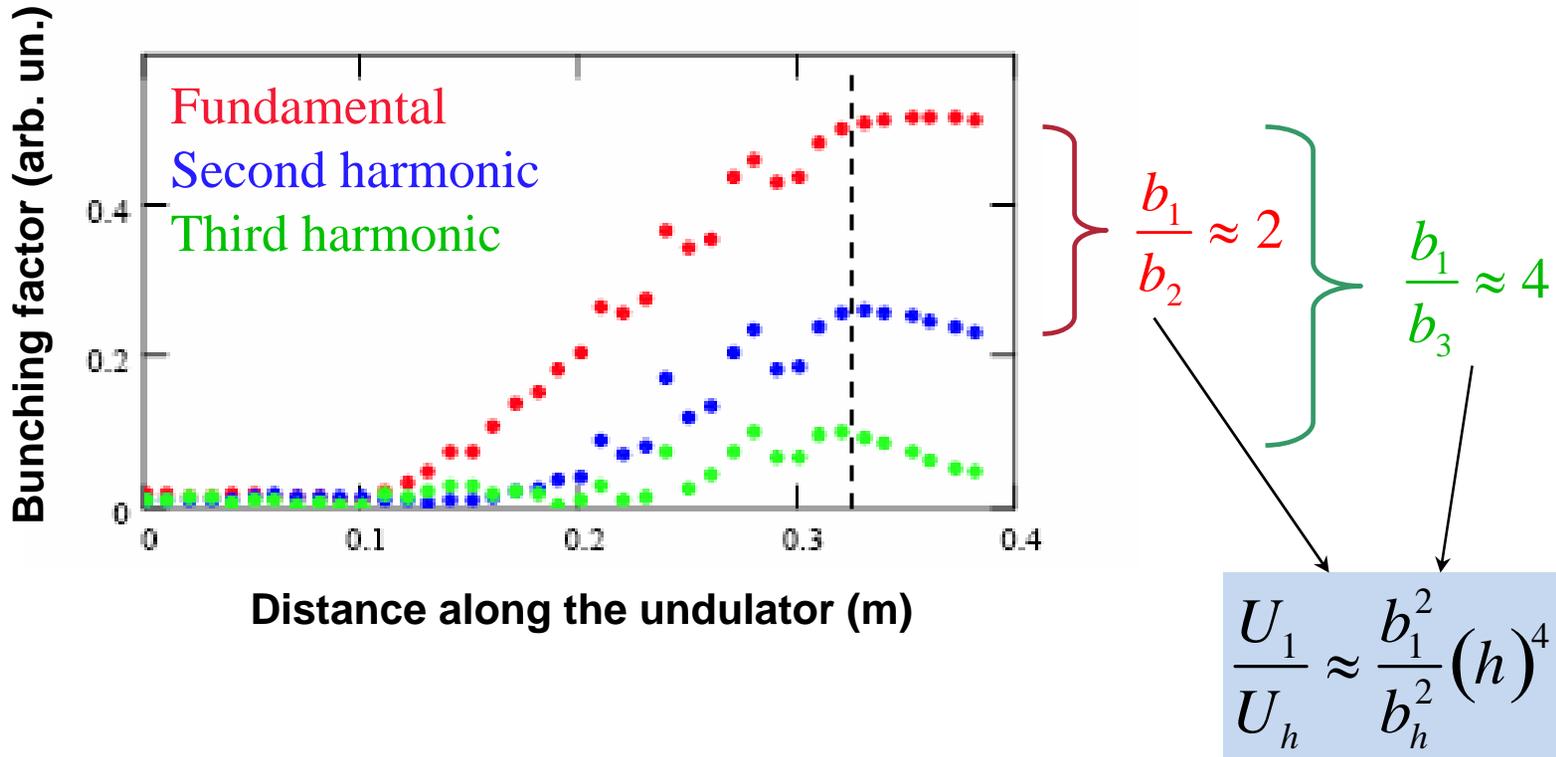


Experimentally achieved coupling efficiency is comparable to that for n=1 case!



3D Simulations of a Bunched Beam

TREDI simulations for laser power 35 MW, $w_0=600 \mu\text{m}$ and $\sigma_{\text{rms}}=400 \mu\text{m}$

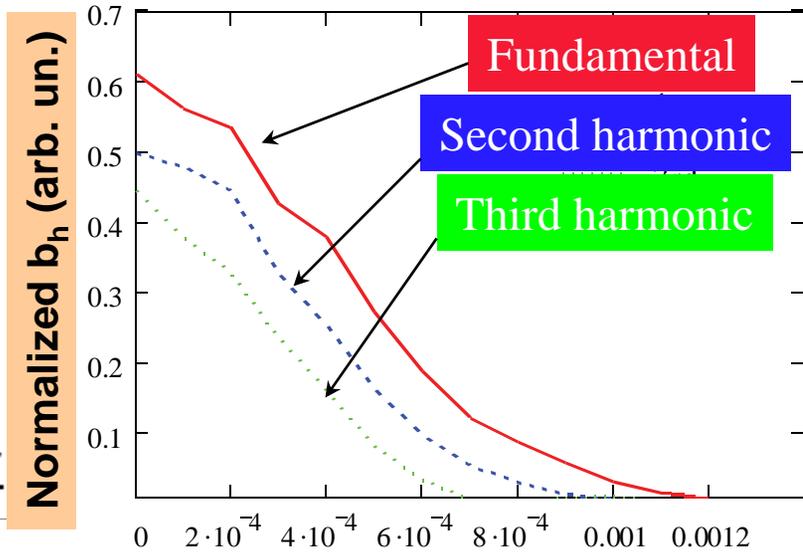
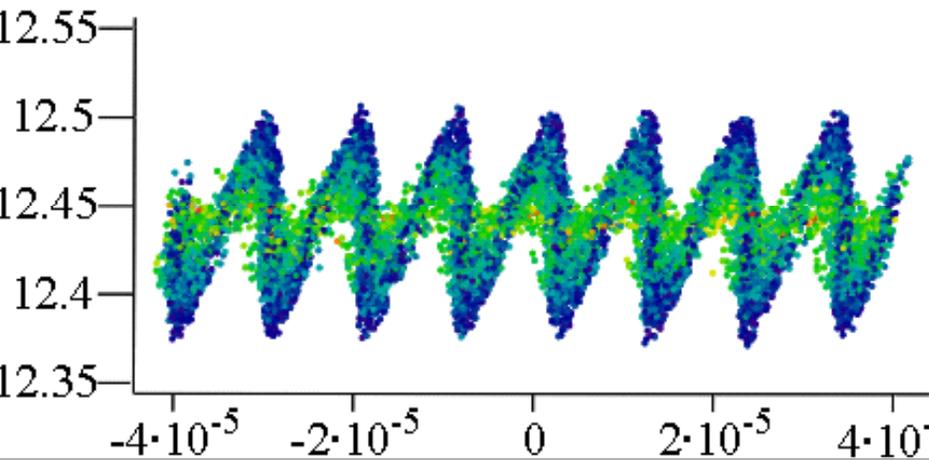


The harmonic ratios extracted from simulations $U_1/U_2=64$ and $U_1/U_3=2025$ are grossly off the measured values.



Transverse effects in bunched beam

TREDI simulations for laser power 35 MW, $w_0=600 \mu\text{m}$ and $\sigma_{\text{rms}}=400 \mu\text{m}$



$$\frac{U_1}{U_h} \approx \frac{N_1^2 b_1^2}{N_h^2 b_h^2} (h)^4$$

$$\frac{b_1}{b_2} \approx 1.2$$

Radius (m)

$$\frac{b_1}{b_3} \approx 1.33$$

The e-beam is bunched stronger on axis and the effective beam size are smaller for higher harmonics $\sigma_{x,y}=380 \mu\text{m}$; 2nd $\sigma_{x,y}=335 \mu\text{m}$; 3rd $\sigma_{x,y}=295 \mu\text{m}$, then for this effective beams harmonic ratios $U1/U2=14$ and $U1/U3=53$.



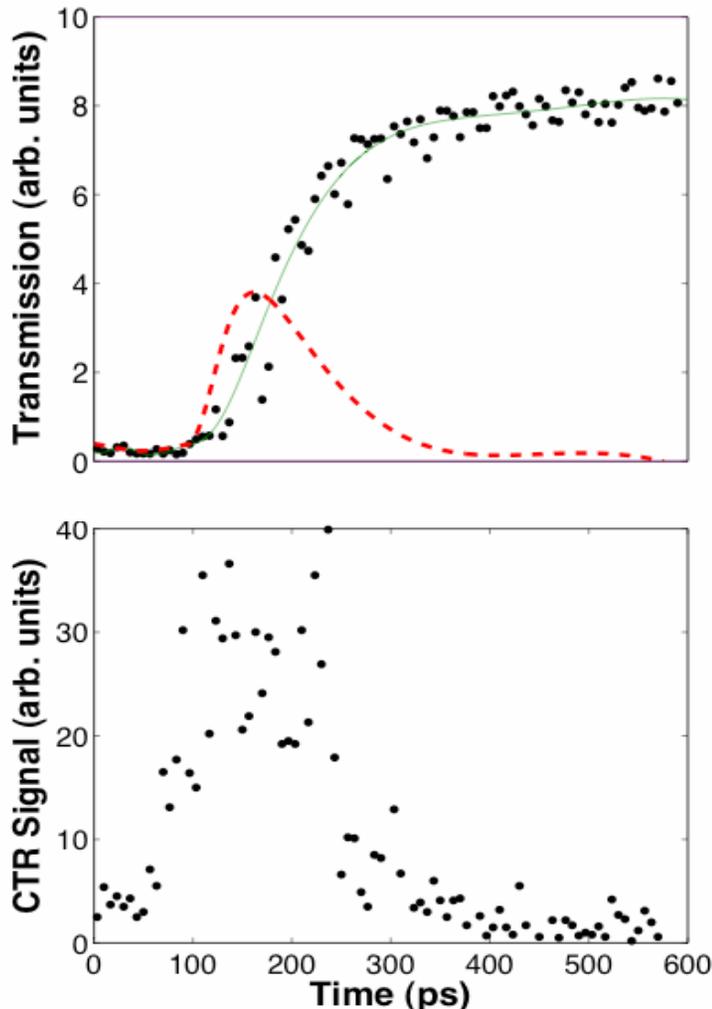
Summary

- 1) We report efficient coupling between the relativistic electrons and seed radiation in a 7th harmonic IFEL interaction.
- 2) We experimentally characterized the strength of this high-order IFEL interactions by analyzing a fundamental, the second and the third harmonics of a microbunched beam in CTR spectrum.
- 3) Comparison between the measurements and 3D simulations revealed that for a seeded IFEL/FELs there is a difference in transverse bunching on different harmonics which may play an important role on the CTR spectrum.
- 4) Inclusion of the high-order IFEL/FEL interactions ($n \geq 3$) on equal footage with the regular ones adds flexibility in designing undulator based systems.



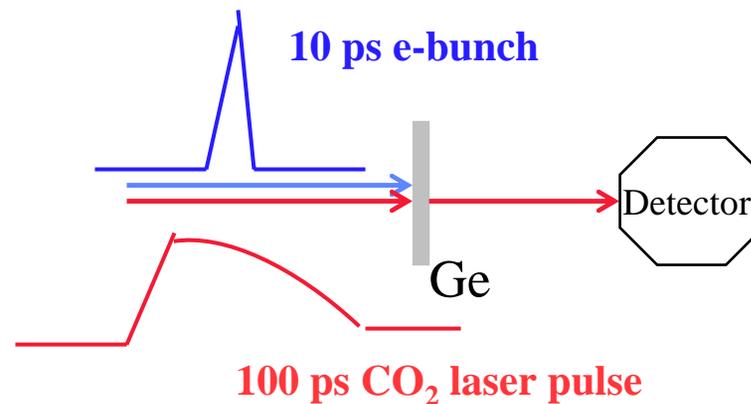
Synchronization of e-beam and 10 μm pulse on a picosecond scale

Cross-correlation between 10 μm laser pulse and electrons in Ge slab and Al foil



E-beam induced carrier generation in Ge

$$\frac{dN}{dt} = -\alpha N + \frac{\beta J(t)}{e}, \beta \text{ is cross section}$$

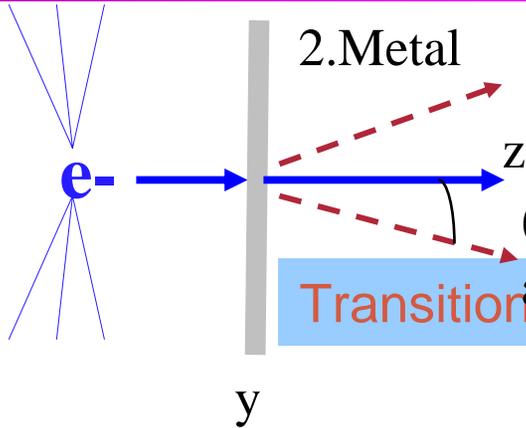


Accuracy of synchronization is limited by
10 ps bunch length e-beam duration



Transition Radiation as a Diagnostic for Bunched Beam

1. Vacuum



2. Metal

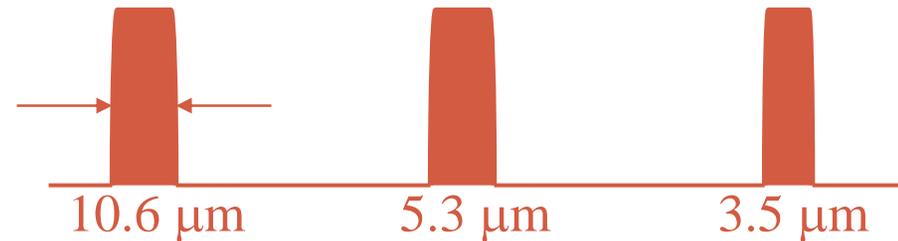
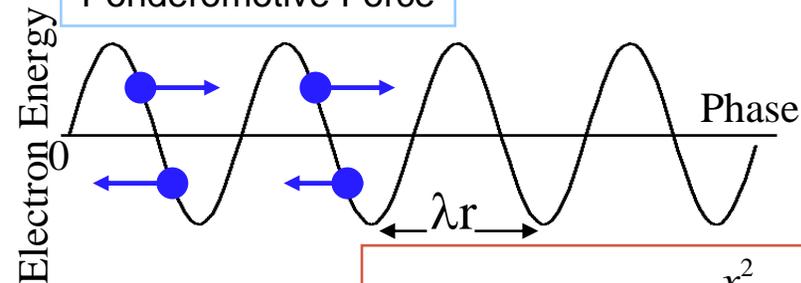
$$\frac{d^2U}{d\omega d\Omega} \cong \left[N + N^2 F_{Long}(\omega) F_{Trans}(\omega) \right] \frac{d^2U}{d\omega d\Omega} \Big|_{1e}$$

$\theta = 1/\gamma$ observation angle

Fourier transform of the e-beam profiles

CTR Spectrum of a Microbunched beam

Ponderomotive Force



E-beam charge

$$\rho(x, y, z) = \frac{eN \exp\left(-\frac{x^2}{2\sigma_x^2} - \frac{y^2}{2\sigma_y^2} - \frac{z^2}{2\sigma_z^2}\right)}{(2\pi)^{3/2} \sigma_x \sigma_y \sigma_z} \times \left[1 + \sum_{n=1}^{\infty} b_n \cos(nk_r z) \right]$$

h- Harmonics in CTR spectrum

Since the beam has has Fourier components at k_r and its harmonics, the CTR spectrum