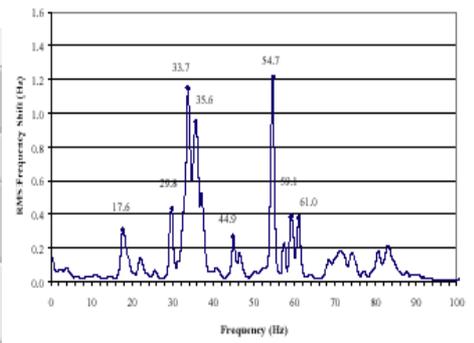
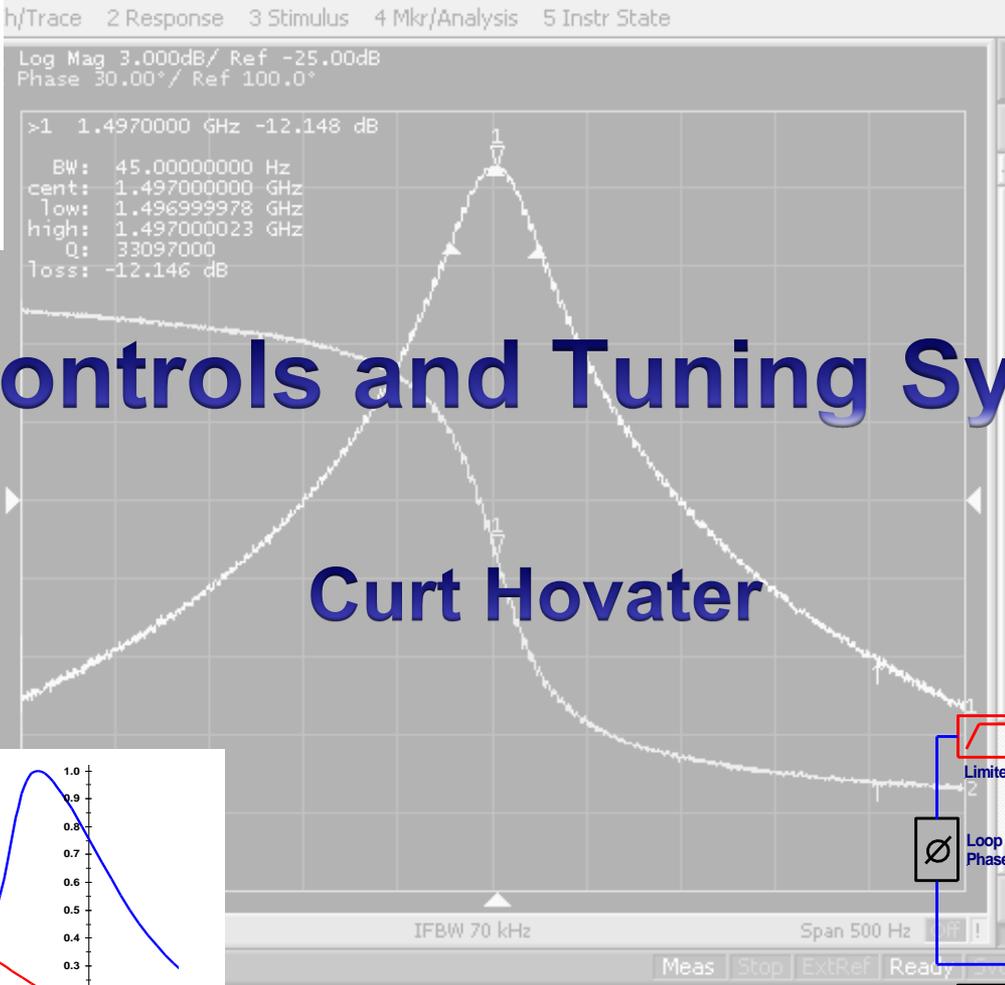
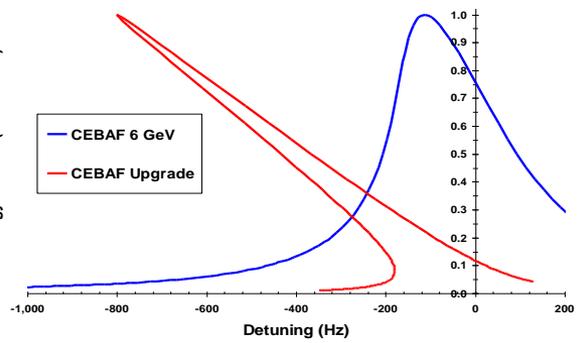


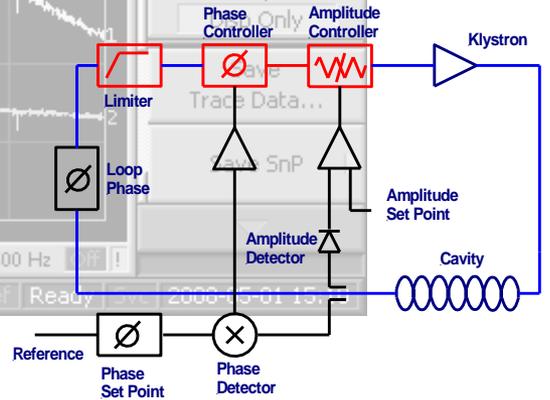
$$\beta_{opt} = \sqrt{(b+1)^2 + \left[\frac{2\delta f}{\Delta f_o} \right]^2}$$

where $b = \frac{I_o(R/Q)Q_o}{V} \cos \phi$



RF Controls and Tuning Systems

Curt Hovater



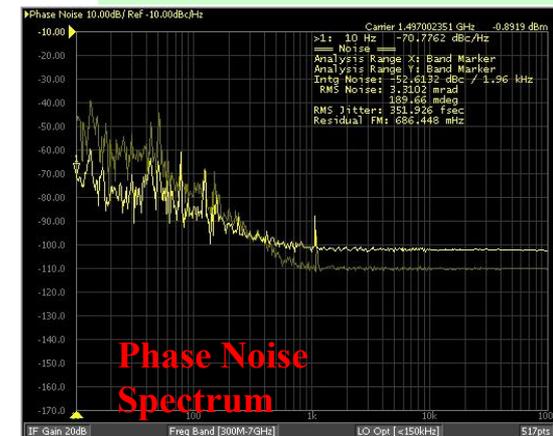
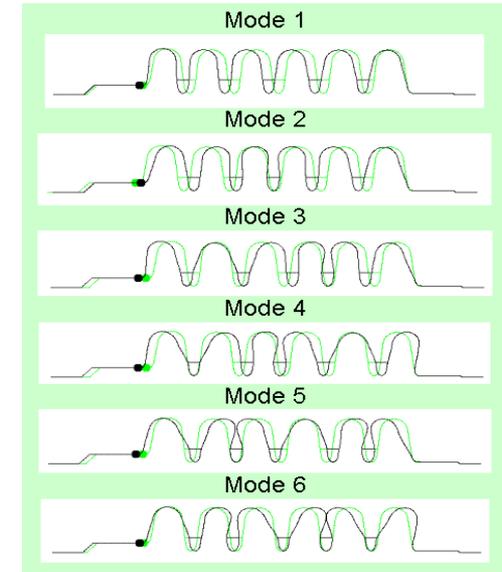
Outline

- **Why Control?**
- **Cavity Equations**
- **Control Systems**
 - **Cavity Models**
- **Algorithms**
 - **Generator Driven Resonator (GDR)**
 - **Self Excited Loop (SEL)**
- **Hardware**
 - **Receiver**
 - **ADC/Jitter**
 - **Transmitter**
 - **Digital Signal Processing**
- **Cavity Tuning & Resonance Control**
 - **Stepper Motor**
 - **Piezo**

Understand What You Are Controlling

- Cavity: what's the frequency and Q_{ext}
- Pulsed, CW, both
- Cavity Gradient
- Lorentz detuning
- Field regulation
- Residual microphonic background
- Beam current
- Klystron/IOT/amplifier effects
- Other cavity pass bands
- He pressure drifts
- Fault Recovery

**SNS Cavity
Mechanical
Modes**

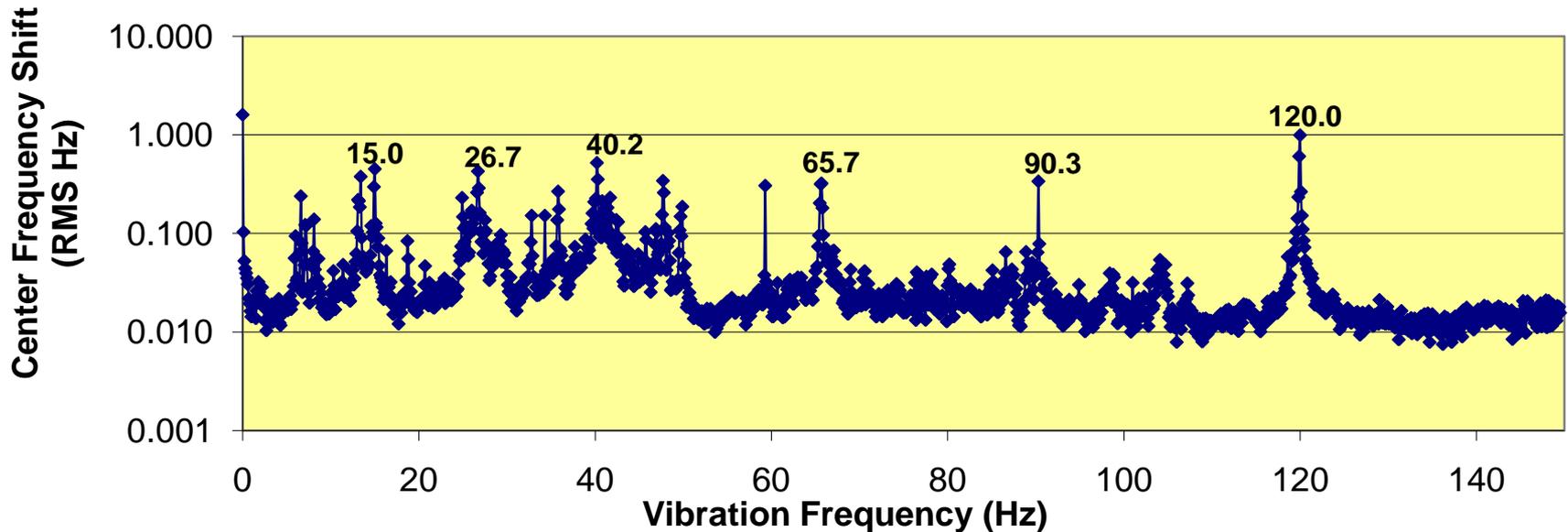


Don't Over Build the Control SystemKISS

Cavity Microphonics

- Determines the feedback gain needed for operation
- Determines the Q_L and the klystron power for lightly loaded cavities

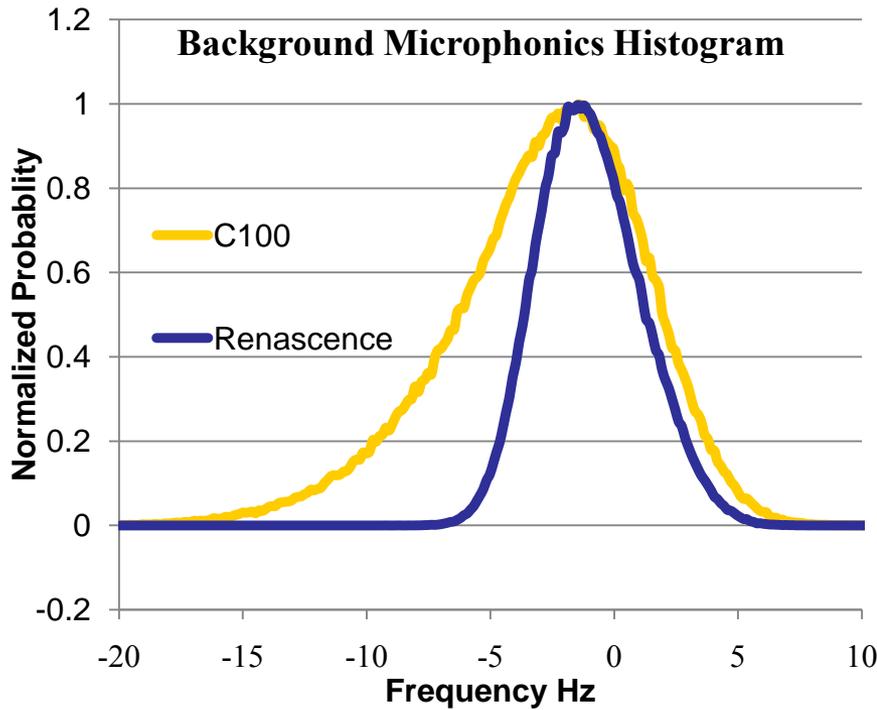
C100 HTB Cavity 7



References: 3

Cavity Microphonics Cont.

Microphonic Detuning*	Renascence (stiffened)	C100
RMS Amplitude (Hz)	1.98	3.65
6σ (Hz) ~ Peak	11.9	21.9



*Data Taken in Same Environment

Microphonic Impact on cavity power operating at 20 MV/m (100 μ A of beam)

- C100 = 5.3 kW
- REN = 3.3 kW

Potential for cost reduction

- Utility
- Power amplifier

Cryomodule design should incorporate features to reduce microphonics.

References: 3

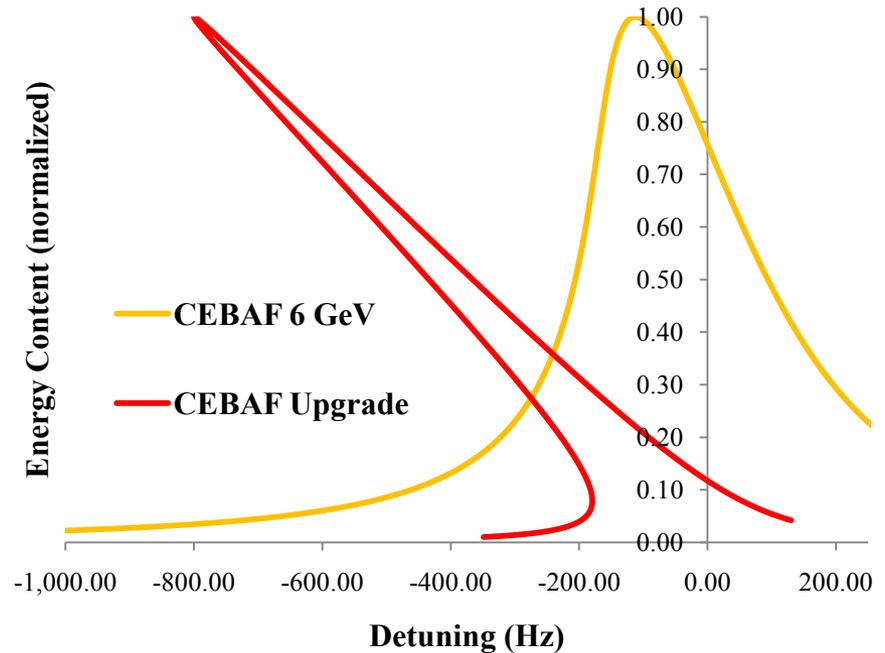
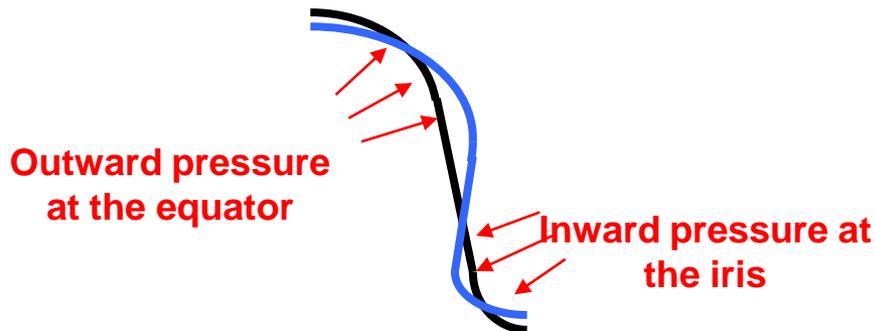
Lorentz Detuning

- RF power produces radiation

pressures : $P = (\mu_0 H^2 - \epsilon_0 E^2)/4$

- Pressure deformations produce a frequency shift :

$$\Delta f = K_L E_{acc}^2$$



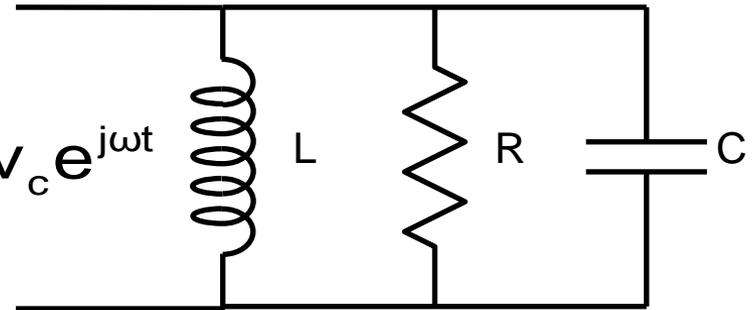
The Quadratic relationship with Gradient becomes an issue at the high gradients (15+ MV/m) needed for new accelerators

References: 4,5

Cavity Equivalent Circuit

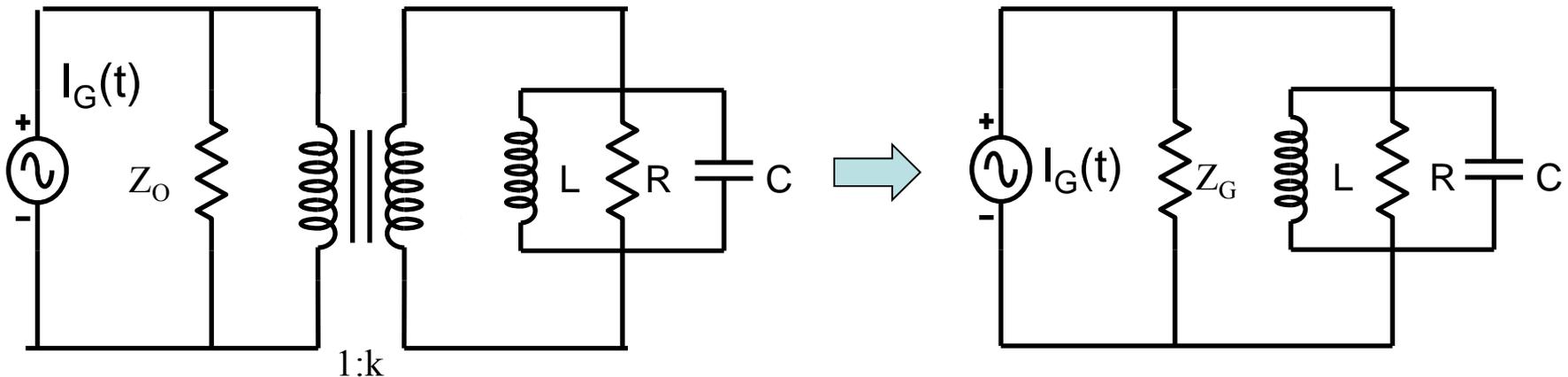
The simplest representation of a cavity is a parallel LRC circuit

$$V_c(t) = v_c e^{j\omega t}$$



Coupling to the cavity can be represented by a transformer and then reduced to the following circuit

$$Z = \left(\frac{1}{R} + \frac{1}{j\omega L} + j\omega C \right)^{-1}$$



where $Z_G = k^2 Z_0$

And the coupling β is defined

$$\beta \equiv \frac{1}{k^2} \frac{R}{Z_0}$$

References: 1

SC Cavity Equivalent Circuit Terms

R_{sh}	Shunt Impedance	Ω		R_L	Loaded Shunt impedance	Ω
r/Q	Geometry Factor	Ω		Q_o	Intrinsic Quality Factor	
E	Electric Field	V/m		Q_L	Loaded Quality Factor	
l	Electrical Length	m		P_g	Generator Power	W
f_o	Cavity Frequency	Hz		P_c	Cavity Dissipated Power	W
W	Stored Energy	J		Ψ_b	Beam Phase	
β	Coupling Coefficient			I_b	Beam Current	A
Ψ	Tuning Angle			V_c	Cavity Voltage	V
δf	Cavity Detuning	Hz		Δf_o	Cavity Bandwidth	Hz
δf_o	Static Detuning	Hz		δf_m	Microphonic Detuning	Hz

Basic Cavity Formulas

Substitutions for L & C

$$\omega_o = \frac{1}{\sqrt{LC}} \quad C = \frac{Q_o}{\omega_o R}$$

Shunt Impedance

$$R_{sh} = \frac{V_c^2}{P_c} \text{ or from circuit theory } R_{sh} = \frac{V_c^2}{2P_c}$$

Loaded Q and Shunt Impedance

$$Q_L = \frac{Q_o}{1 + \beta} \quad R_L = (r / Q) Q_L$$

Generator Power

$$P_g = \frac{V_c^2}{R_L} \frac{(1 + \beta)}{4\beta} \left\{ \left[1 + \frac{I_o R_L}{V_c} \cos \Psi_b \right]^2 + \left[\tan \Psi - \frac{I_o R_L}{V_c} \sin \Psi_b \right]^2 \right\}$$

Detuning Angle

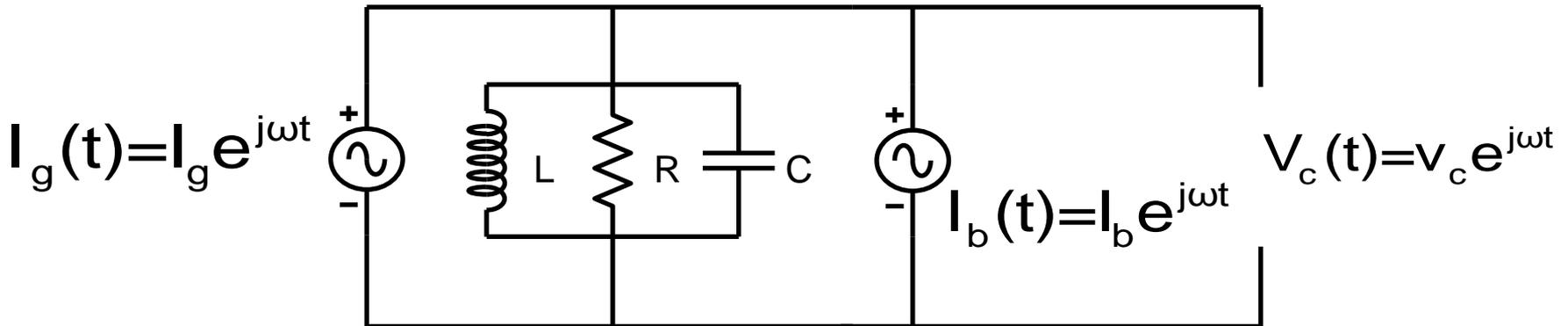
$$\tan \Psi = -2Q_L \frac{\Delta \omega}{\omega_o} = -2Q_L \frac{\delta f}{f_o}$$

Total Detuning

$$\delta f = \delta f_o + \delta f_m$$

References: 1, 27

Equivalent Circuit: Cavity + Klystron + Beam



- **Beam and RF generator are represented by a current source**

I_b produces V_b with phase Ψ which is the detuning angle
 I_g produces V_g with phase Ψ

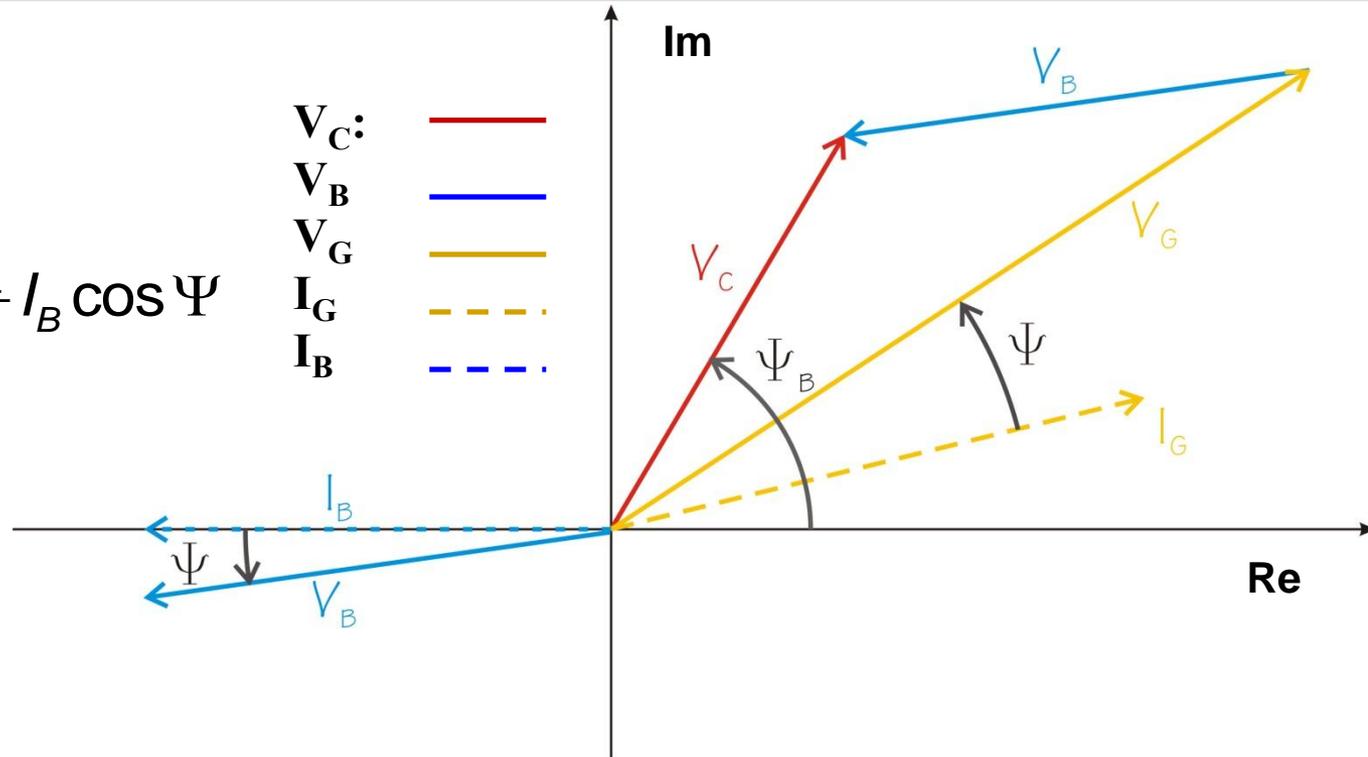
Cavity Voltage $V_c = V_g - V_b$

$$V_c = \frac{R_L}{2} I_G \cos \Psi - \frac{R_L}{2} I_B \cos \Psi$$

Phasor Diagram

$$V_C = \frac{R_L}{2} I_G \cos \Psi - \frac{R_L}{2} I_B \cos \Psi$$

V_C :	— (red)
V_B :	— (blue)
V_G :	— (yellow)
I_G :	- - - (yellow)
I_B :	- - - (blue)



$$V_B = \frac{R_L}{2} I_B \cos \Psi$$

$$P_G = \frac{1}{16\beta} R_{Sh} I_G^2$$



$$V_G = \frac{2\beta^{1/2}}{(1+\beta)^{1/2}} (P_G R_L)^{1/2} \cos \Psi$$

References: 1, 2, 19, 20

Q_L Optimization for Minimum Power

From generator power
We can determine the
Minimum power needed

$$P_g = \frac{V_c^2}{4 \frac{r}{Q} Q_L} \left\{ \left[1 + b Q_L \cos \Psi_b \right]^2 + \left[2 Q_L \frac{\delta f}{f_o} + b Q_L \sin \Psi_b \right]^2 \right\}$$

Substituting in for b where

$$b = \frac{I_o}{V_c} \frac{r}{Q}$$

Some assumptions

$$Q_o \gg Q_L \text{ therefore } \beta \approx \frac{Q_o}{Q_L}$$

Differentiating P_g with
respect to Q_L and setting it
to zero leads to optimum
Coupling Q

$$Q_{Lopt} = \left[b^2 + 4 \left(\frac{\delta f}{f_o} \right)^2 + 4 \left(\frac{\delta f}{f_o} \right) b \sin \Psi_b \right]^{-1/2}$$

For beam on crest $\Psi_b = 0$

$$Q_{Lopt} = \left[\left(\frac{I_o}{V_c} \frac{r}{Q} \right)^2 + 4 \left(\frac{\delta f}{f_o} \right)^2 \right]^{-1/2}$$

And if $I_o = 0$

$$Q_{Lopt} = \frac{f_o}{2 \delta f}$$

And if $I_o \gg 0$

$$Q_{Lopt} \cong V / I_o (r / Q)$$

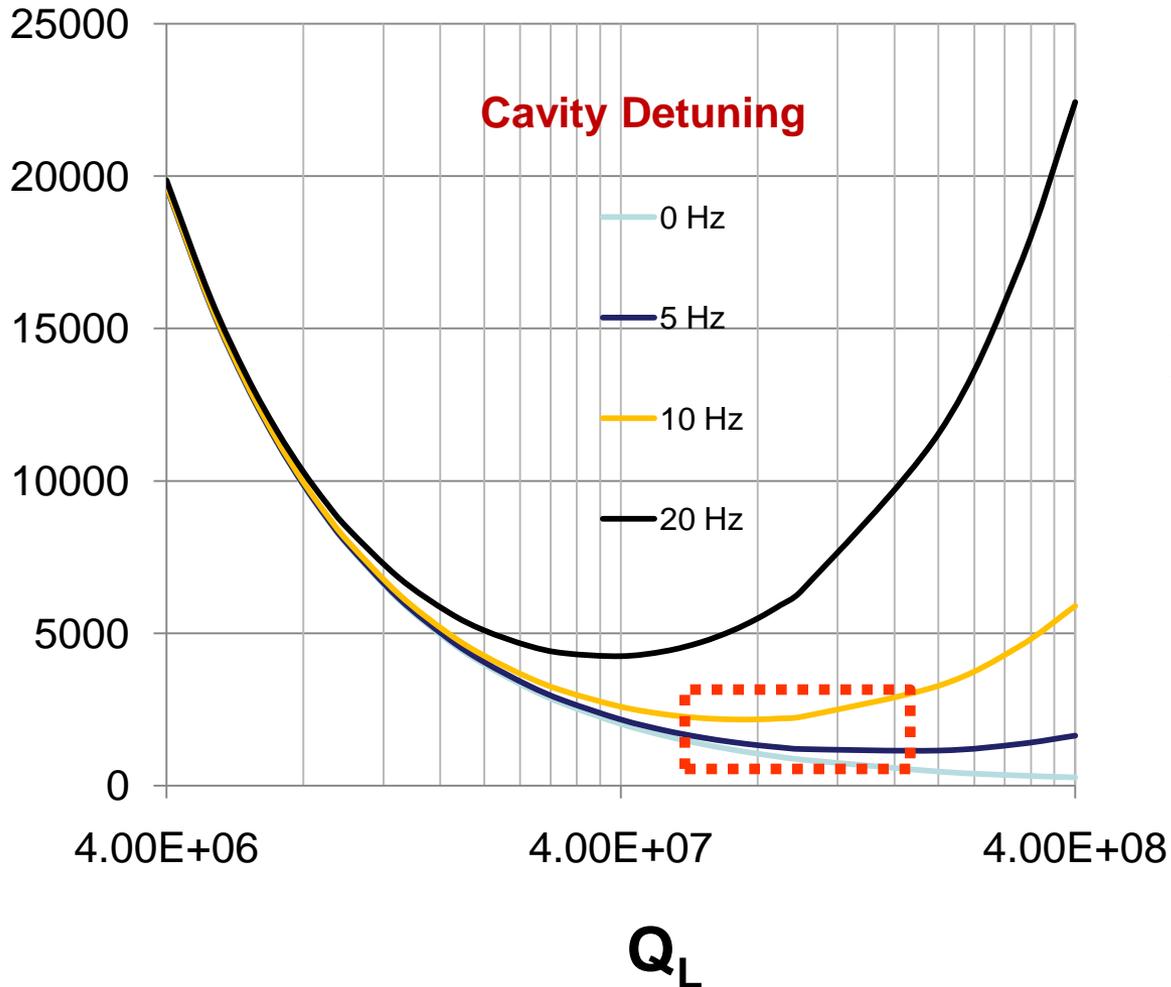
References: 1, 20

Q_L Optimization: Lightly/non Beam Loaded Cavity

Beam on Crest

$$Q_{Lopt} \cong f_o / 2\delta f$$

Power



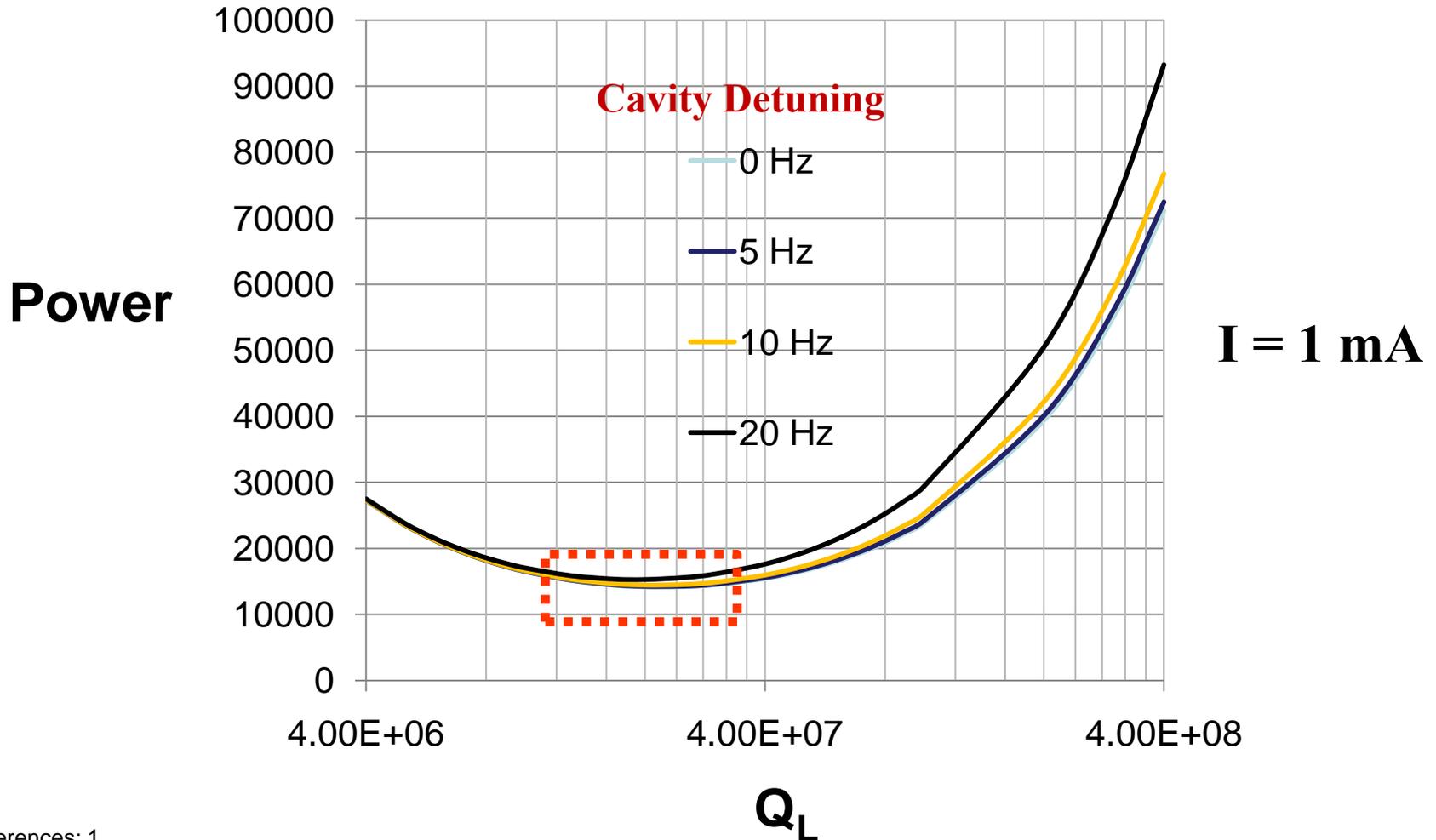
I = 10 μ A

References: 1

Q_L Optimization: Beam Loaded Cavity

Beam on Crest

$$Q_{Lopt} \cong V / I_o (r / Q)$$



References: 1

Electronic and Mechanical Control

When to apply

$$\delta f = \delta f_o + \delta f_m$$

δf_o is the static detuning or slow detuning< 1 Hz

- Use active mechanical tuning to control cavity frequency

δf_m is the fast detuning do to microphonics>10 Hz

- Use active electronic feedback for field control

Gray area between 1 and 10 Hz

Control Systems

Classic “Plant-Controller” can be used to model the RF control system

Cavity

- Can be modeled a variety of ways.
- Lorentz force can be added as a non-linear element
- Mechanical modes can also be included

Power Amplifier (Klystron, IOT etc.)

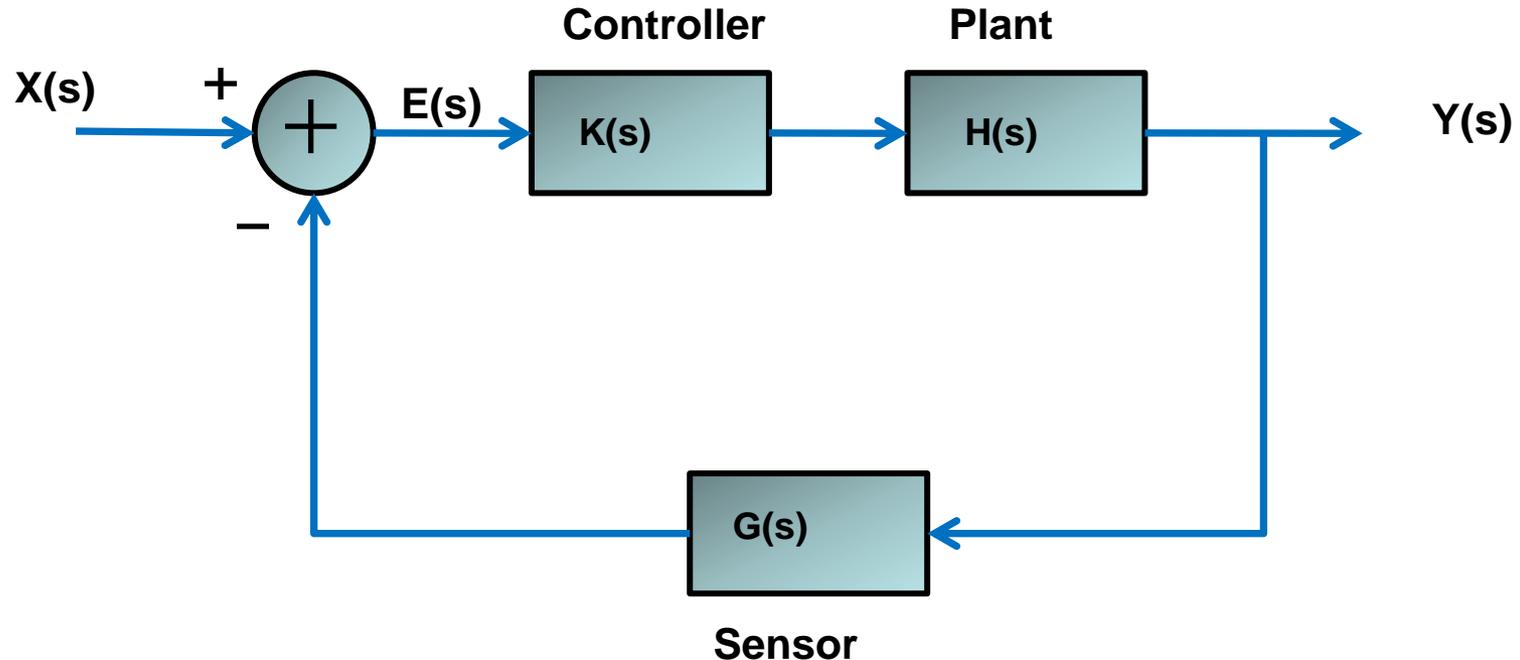
- Saturation effects

Hardware

- Group delay (line delay, processing latency etc.)

Modeling software such as Matlab/Simulink has made this rather easy.

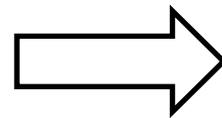
Controller – Plant System Representation



**Need to solve for close loop
transfer function: Y/X**

$$E(s) = X(s) - G(s)Y(s)$$

$$Y(s) = K(s)H(s)E(s)$$



$$\frac{Y(s)}{X(s)} = \frac{H(s)K(s)}{1 + H(s)K(s)G(s)}$$

Plant (Cavity) Transfer Function

Want Output/Input (V/I) assume Parallel RLC circuit with current source

$$I = \frac{V}{R} + \frac{V}{j\omega L} + j\omega CV$$

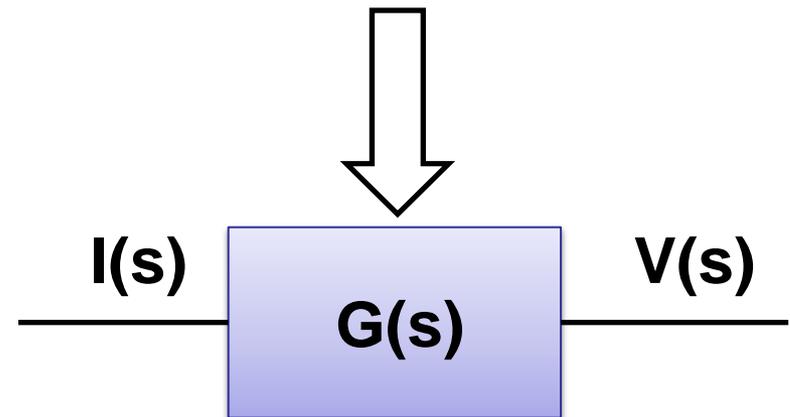
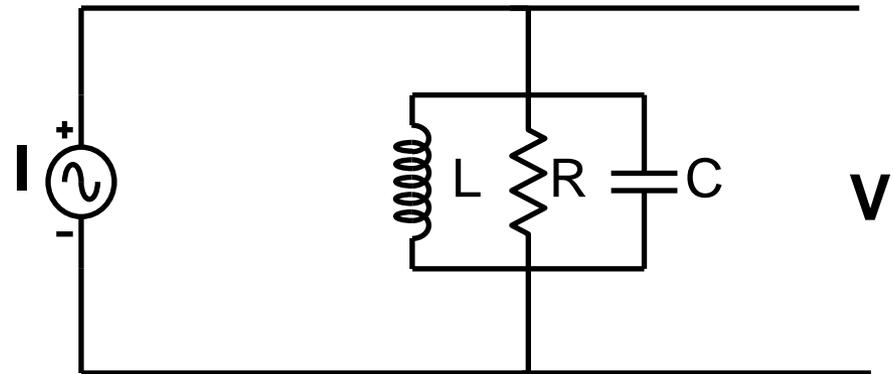
$$\frac{V}{I} = \frac{j\omega RL}{\omega^2 RLC + j\omega L + R}$$

Convert to s domain

$$\frac{V(s)}{I(s)} = G(s) = \frac{sRL}{s^2 RLC + sL + R}$$

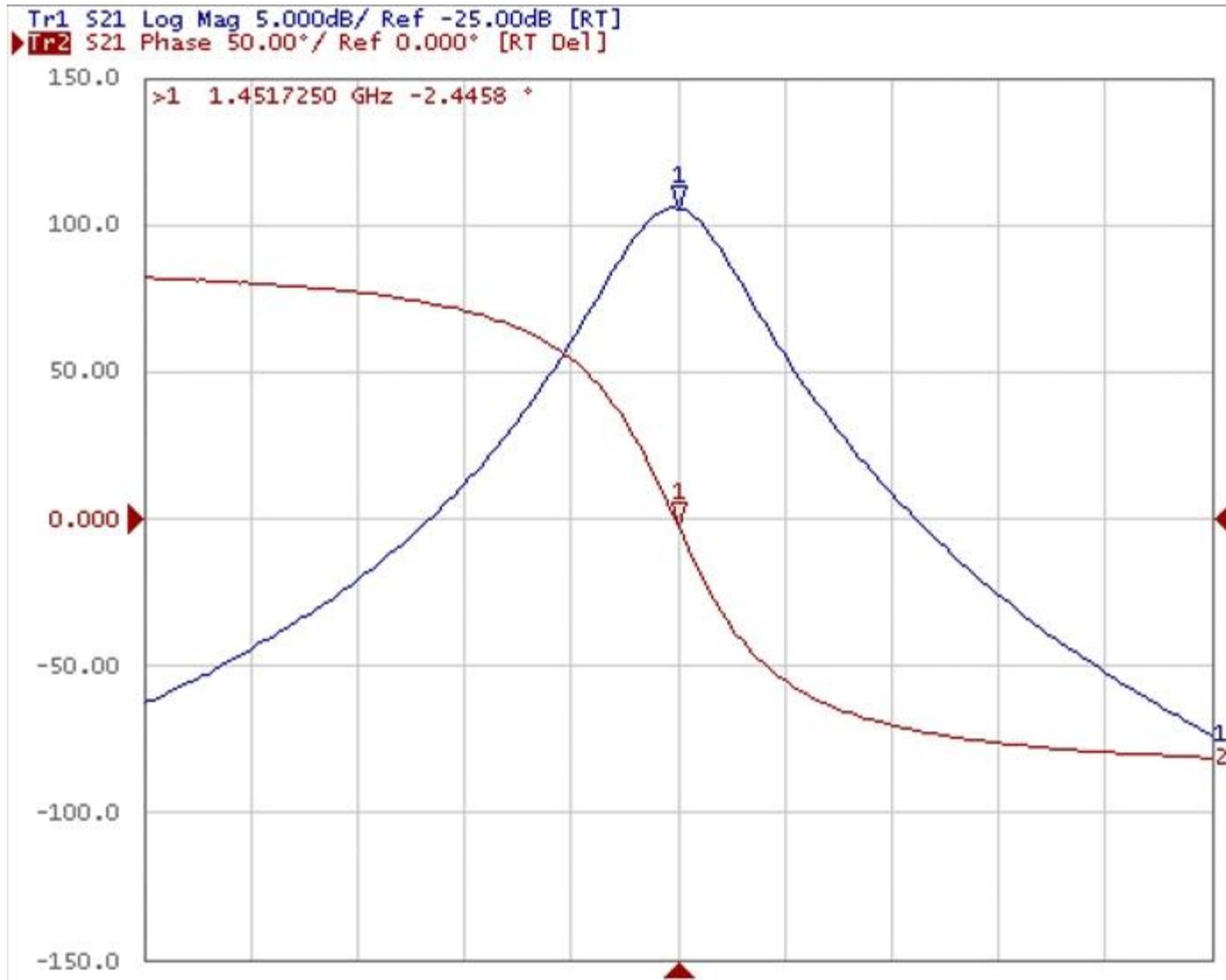
Sub for L&C

$$G(s) = \frac{\frac{\omega_0 R_L}{Q_L} s}{s^2 + \frac{\omega_0}{Q_L} s + \omega_0^2}$$



$$V(s) = G(s) \cdot I(s)$$

Cavity Transfer Function



State Space Representation for a Cavity

We are only interested in the time scale of the detuning microphonics. Therefore we can model the cavity at baseband using a complex envelope by separating $V(t)$ and $I(t)$ into I and Q terms .

$$V(t) = [V_R(t) + jV_I(t)] \cdot e^{j\omega t} \quad I(t) = [I_R(t) + jI_I(t)] \cdot e^{j\omega t}$$

From the 2nd ODE for a driven oscillator $\ddot{V}(t) + \frac{\omega_0}{Q_L} \dot{V}(t) + \omega^2 V(t) = \frac{\omega_0}{Q_L} R_L I(t)$

Want the state form $\dot{x} = Ax + Bu$ where A and B are state Matrixes

Ignoring 2nd derivative terms (small compared to lower order terms), assume that $\omega/\omega_0 \sim 1$ and $\Delta\omega = \omega_0 - \omega$ is the cavity detuning

$$\dot{V}_R + \frac{\omega_0}{2Q_L} V_R + \Delta\omega V_I = R_L \frac{\omega_0}{2Q_L} I_R$$

$$\dot{V}_I + \frac{\omega_0}{2Q_L} V_I - \Delta\omega V_R = R_L \frac{\omega_0}{2Q_L} I_I$$



$$A = \begin{pmatrix} -\frac{\omega_0}{2Q_L} & -\Delta\omega \\ \Delta\omega & -\frac{\omega_0}{2Q_L} \end{pmatrix}$$

$$B = \begin{pmatrix} R_L \frac{\omega_0}{2Q_L} & 0 \\ 0 & R_L \frac{\omega_0}{2Q_L} \end{pmatrix}$$

$$x = \begin{pmatrix} V_R \\ V_I \end{pmatrix}$$

$$u = \begin{pmatrix} I_R \\ I_I \end{pmatrix}$$

Control System Stability

“Quickest way to build an oscillator is to design a control system.”various authors

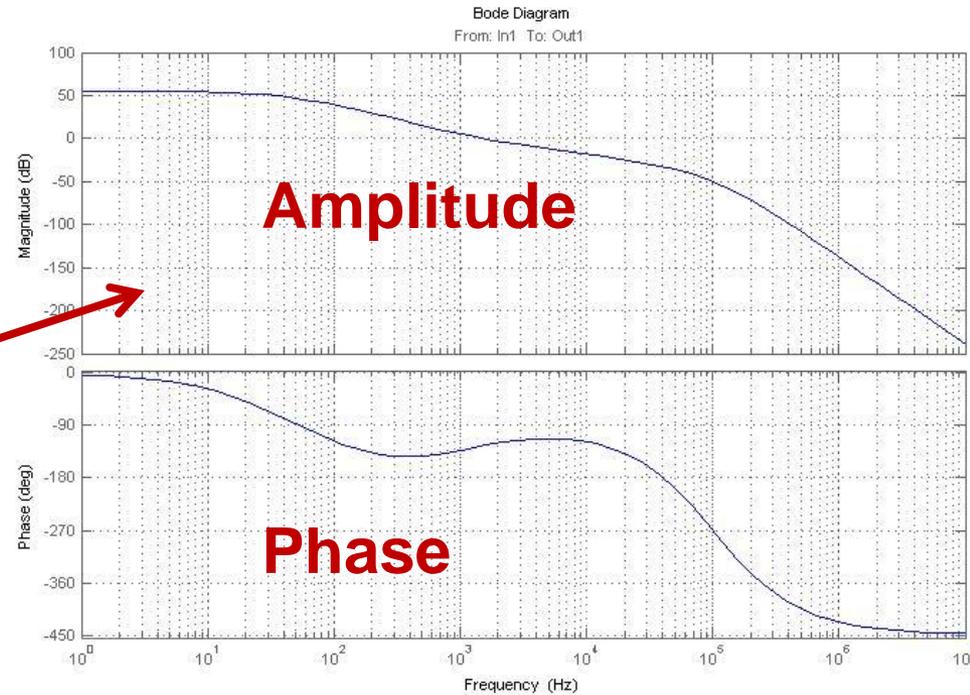
- An unstable condition occurs when $\text{Gain} > 1$ and the phase shift through the system is more than 180 degrees.
- Know your poles! Since we are working with sc cavities the first pole will be the cavity bandwidth (10 – 1000 Hz)
- Each pole contributes 90 degrees starting a decade before the pole and ending a decade after.
- Need to do a phase delay budget all the way around the system, RF Controls-Klystron-waveguide-cavity-cables etc.

Control System Stability

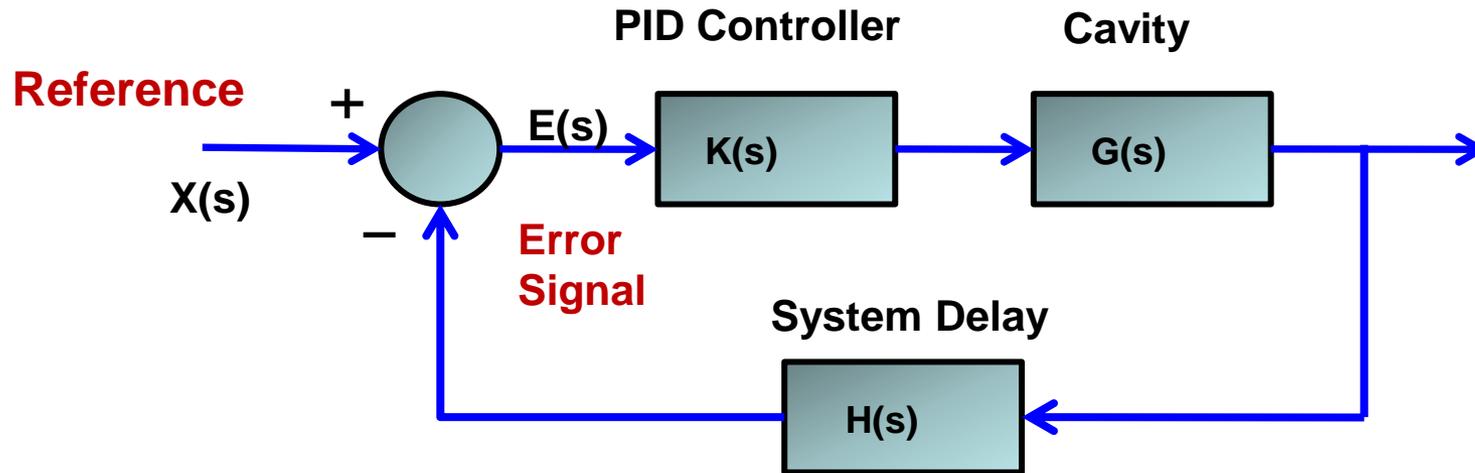
There are many methods (Routh and Nyquist) to determine stability of a control system. Matlab will actually perform this analysis.

Bode Diagrams

- Graphically intuitive
- Give Phase and Gain margin
- Instabilities start as small peaks



Simple PID Cavity Control



PID Function
$$K(s) = K_P + \frac{K_I}{s} + K_D s = \frac{K_D s^2 + K_P s + K_I}{s}$$

System Delay
(Four Poles at 100 kHz)

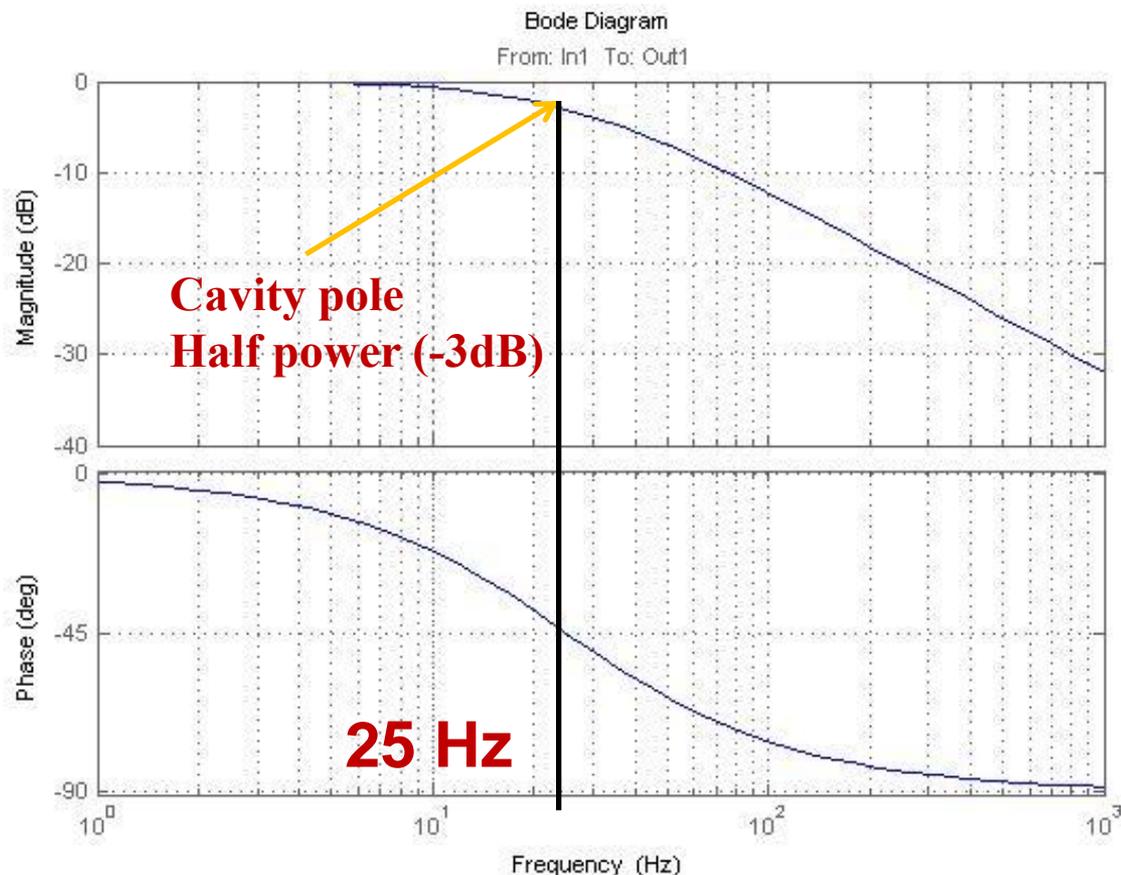
$$H(s) = \left(\frac{6.3 \times 10^5}{s + 6.3 \times 10^5} \right)^4$$

Cavity Bandwidth ~ 25 Hz

$$G(s) = \frac{157}{s + 157}$$

References: 28

Cavity Bode Diagram (First Order Lowpass Filter)



$$G(s) = a/(s+a)$$

$$G(s) = \frac{157}{s + 157}$$

Proportional-Integral-Derivative (PID) Controller

Proportional Term

$$P = K_P e(t) \Rightarrow K_P$$

K_P ~ proportional gain

e ~ error

Integral Term

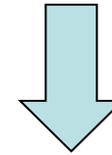
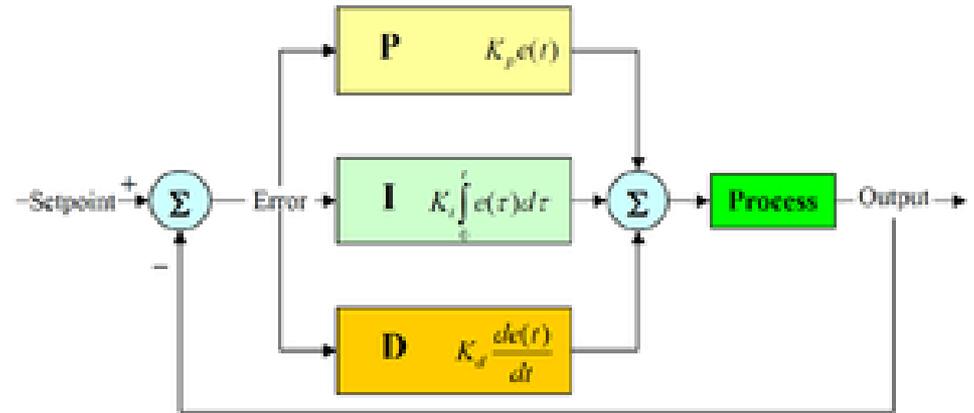
$$I = K_I \int_0^t e(\tau) d\tau \Rightarrow \frac{K_I}{s}$$

K_I ~ integral gain

Derivative Term

$$D = K_D \frac{de(t)}{dt} \Rightarrow K_D s$$

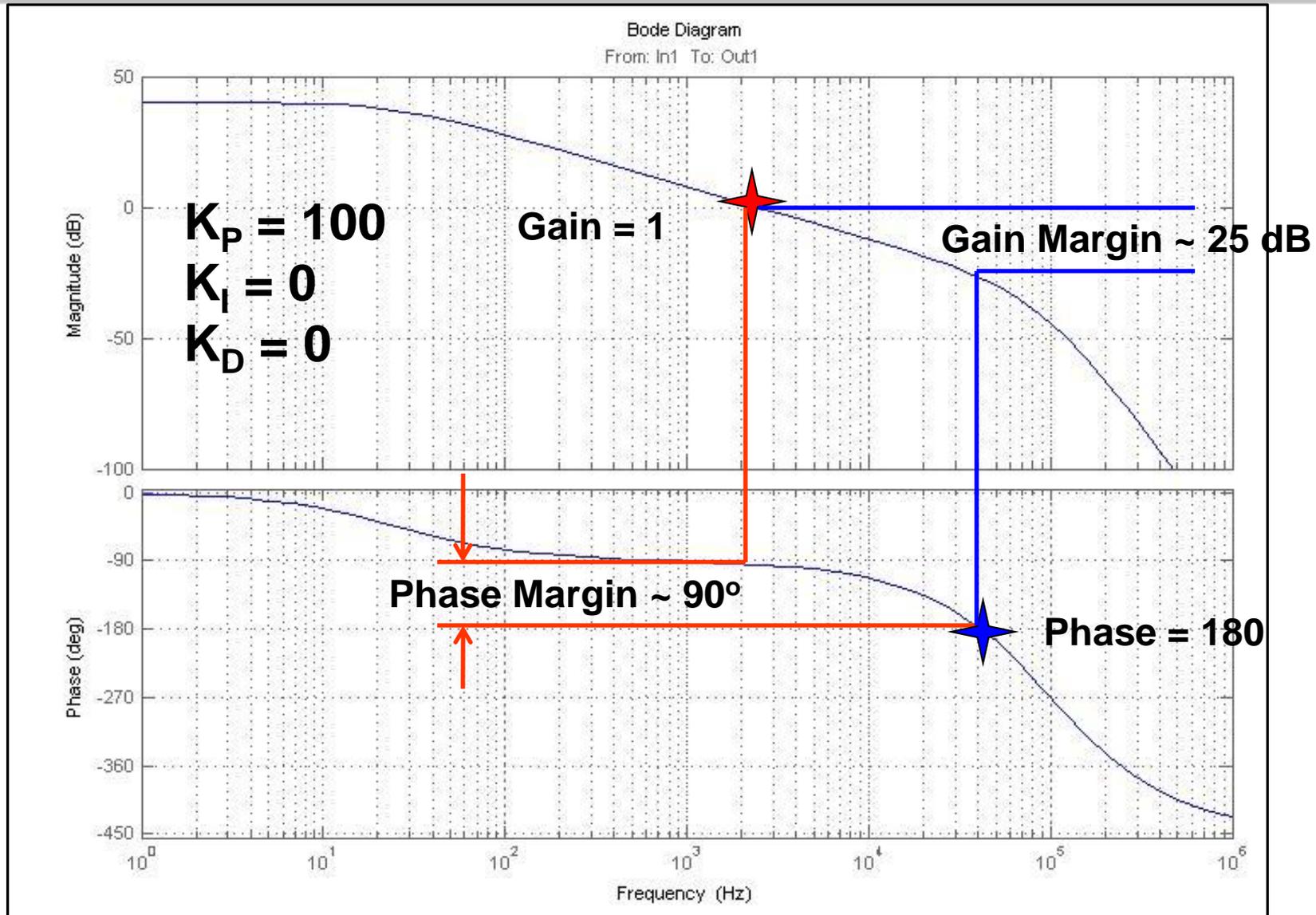
K_D ~ derivative gain



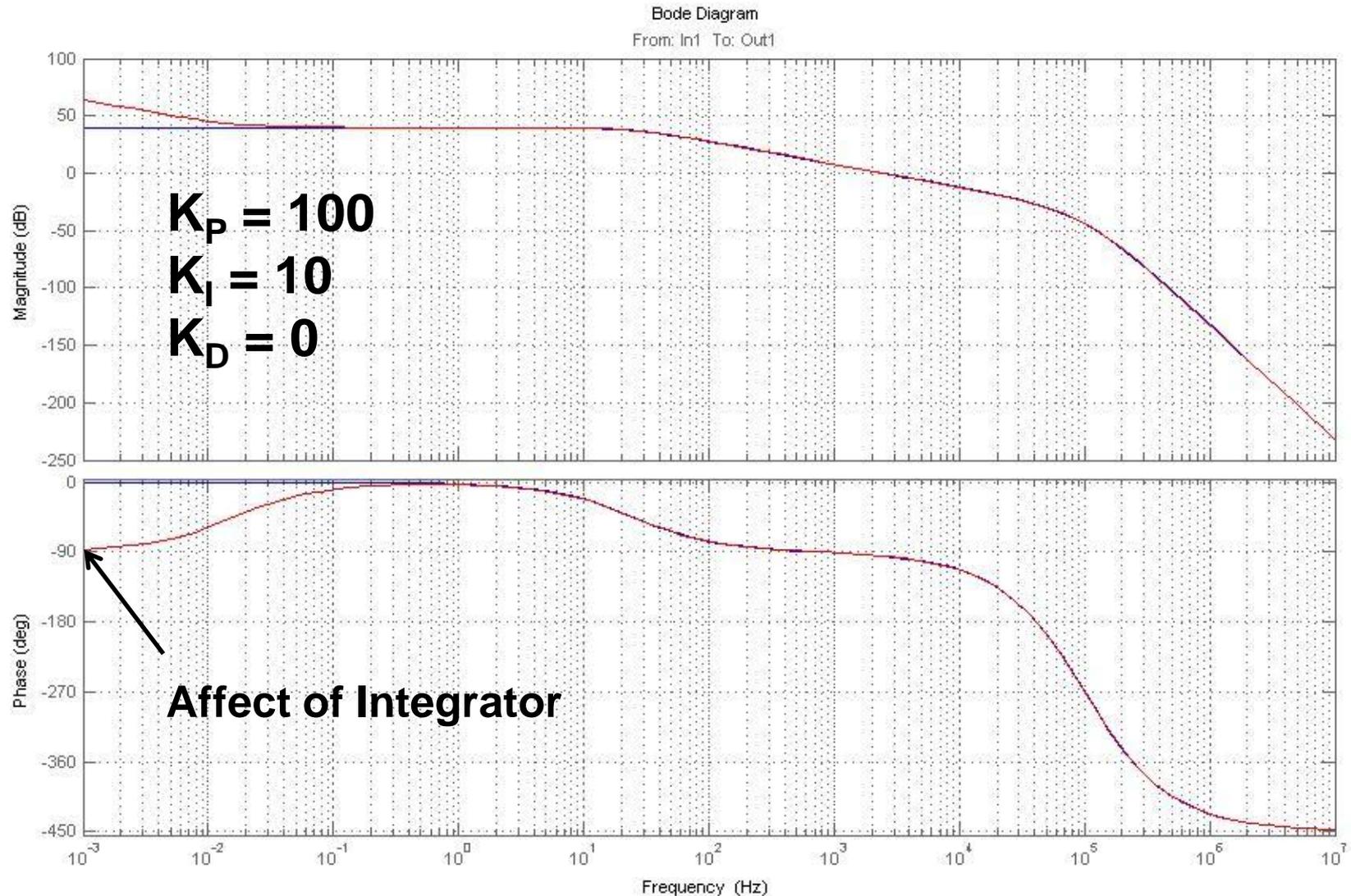
$$K(s) = K_P + \frac{K_I}{s} + K_D s = \frac{K_D s^2 + K_P s + K_I}{s}$$

References: 28

Cavity + Proportional Control

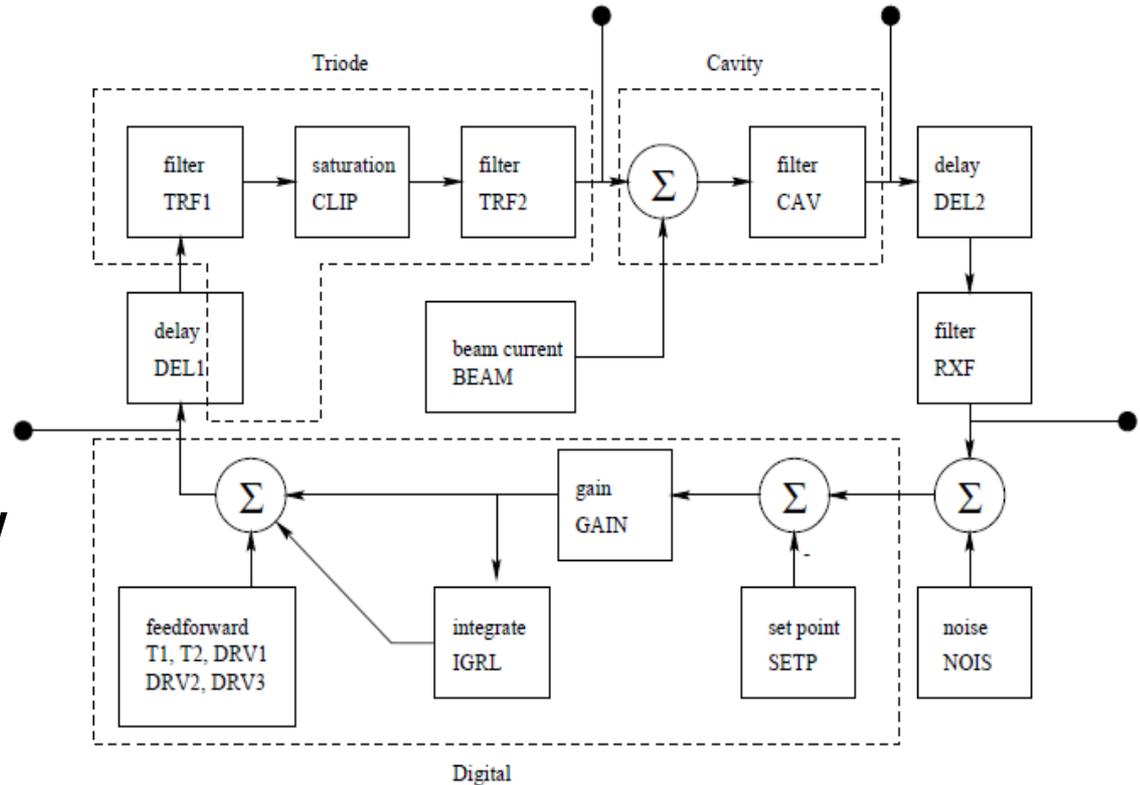


Proportional + Integral Control



RF System Models: LBL/SNS

- Numerical based model, coded in C
- Incorporates feedback and feed forward
- Cavity modeled at baseband as a low pass filter



References: <http://recycle.lbl.gov/~ldoolitt/lrf-model/>

RF System Models: DESY

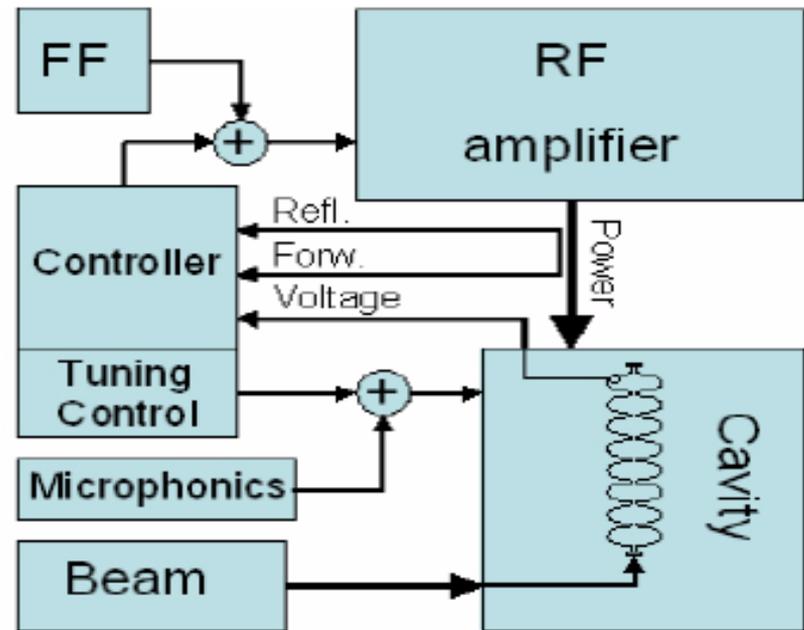
- Matlab/Simulink based
- Cavity represented in state space
- A library of model blocks is available

Feedback/Feedforward

Lorentz Force

GDR and SEL

Various other algorithms
(Kalman, Smith Predictor)



$$\begin{bmatrix} \dot{v}_r \\ \dot{v}_i \end{bmatrix} = \begin{bmatrix} -\omega_{12} & -\Delta\omega \\ \Delta\omega & -\omega_{12} \end{bmatrix} \cdot \begin{bmatrix} v_r \\ v_i \end{bmatrix} + R \cdot \omega_{12} \cdot \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} I_r \\ I_i \end{bmatrix}$$

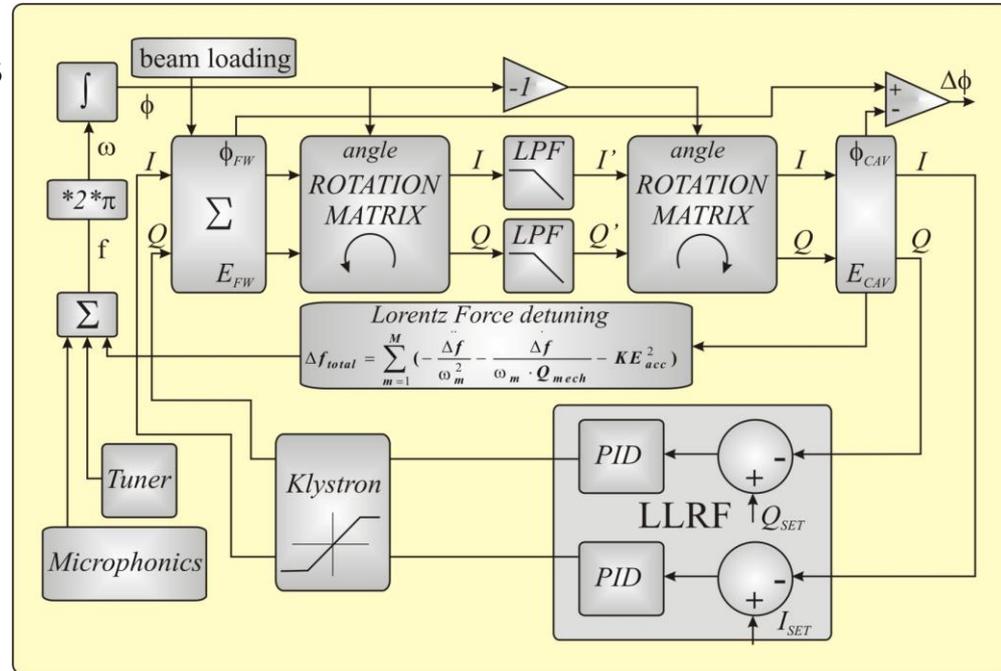
RF System Models: JLAB

Cavity representation is simplified to quadrature components using low pass filter (cavity bandwidth/2).

- Lorentz Force detuning, microphonics and tuners function are incorporated as a frequency modulators.

Baseband simulation, means sampling time for processing can be large (1usec) thus simulation speed is high.

- Rotation matrix for quadrature components to reflect detuning frequency
- Microphonics: External noise generator



Cavity Control Algorithms

Generator Driven Resonator (GDR)

- Vector Sum (FlashILC)
- Feed forward (for pulsed systems)

Self Excited Loop (SEL)

- Microphonics (detuning) compensator

Other Control Algorithms

- Kalman Filter
- Adaptive Control (LMS)

Generator Driven Resonator

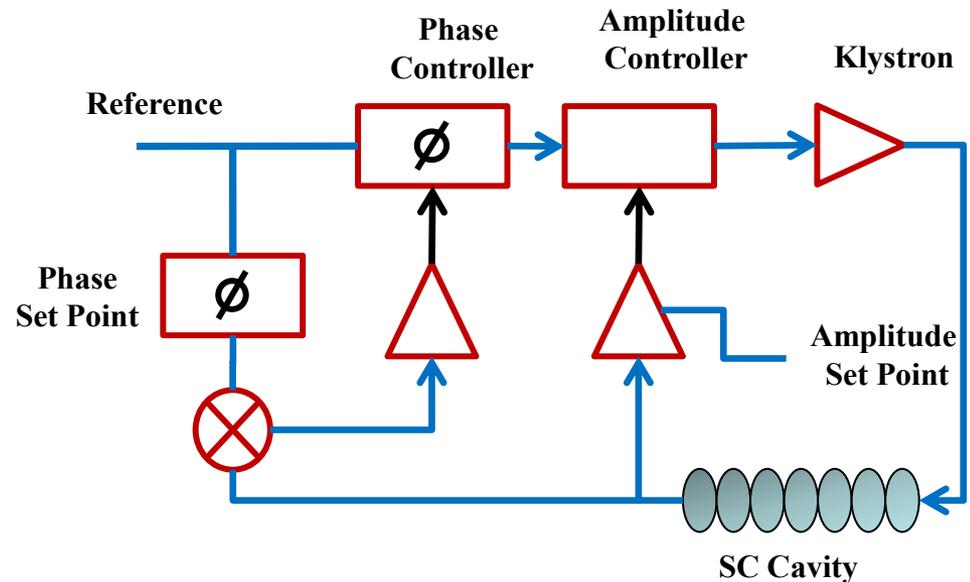
- Essentially an extension of the classic “Controller – Plant” model
- Easily adaptable to I and Q domain for digital control.

Advantages

- Where fast/deterministic lock up times are critical i.e pulsed systems.

Disadvantages

- Not frequency agile needs tuning elements to keep cavity close to reference
- High Q machines with high microphonic content and large Lorentz detuning could go unstable



Self Excited Loop (SEL)

Cavity acts as a “tank” circuit for the feedback. Much like a VCO in a PLL.

By adjusting loop phase, loop is forced to operate at the reference frequency.

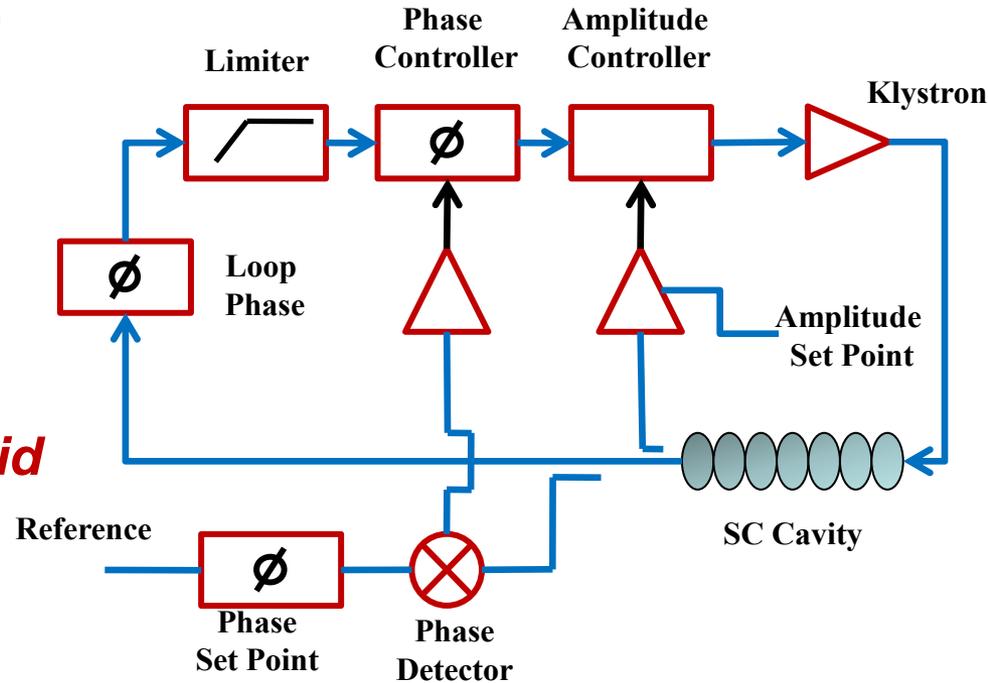
“No free lunch” cavity still must be locked close to the reference to avoid saturating the power amplifier

Advantages

- High Q_L Cavities
- Systems with large Lorentz detuning

Disadvantages

- Slow lock up time



GDR vs. Digital SEL

- When “locked “ the methods are equivalent.
- GDR only operates in the “DC” domain i.e. the converted vector does not spin only has angle and magnitude dependence.
- A digital SEL must be able to handle a spinning vector when the system is not locked i.e. there is an “ ωt ” term that must be accounted for when the SEL is in oscillation mode.
- DSEL capture range only limited by digital filter (~ 100 kHz)
- Easy configuration switch between GDR and SEL

Ultimately some hybrid digital SEL/GDR of the two may be the solution.

Analog RF Systems

- The standard method for RF control up until ~ 1995
- Still have relevance in accelerators that need little adjustment

Advantages

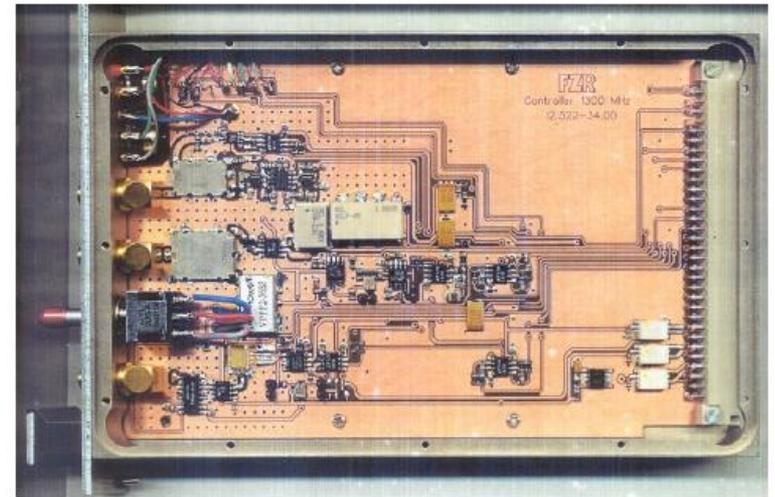
- Economical
- Simple design

Disadvantages

- flexibility
- Pulsed beam loading
- RF/analog signal processing parts harder to find

Recent Installations

Daresbury, ELBE/Rossendorf



Digital RF Systems

- Overwhelmingly the majority of new RF controls employ digital feedback

Advantages

- Flexibility
- Flexibility
-did I mention flexibility??

Disadvantages

- Complexity.....this is relative

Installations too numerous to list

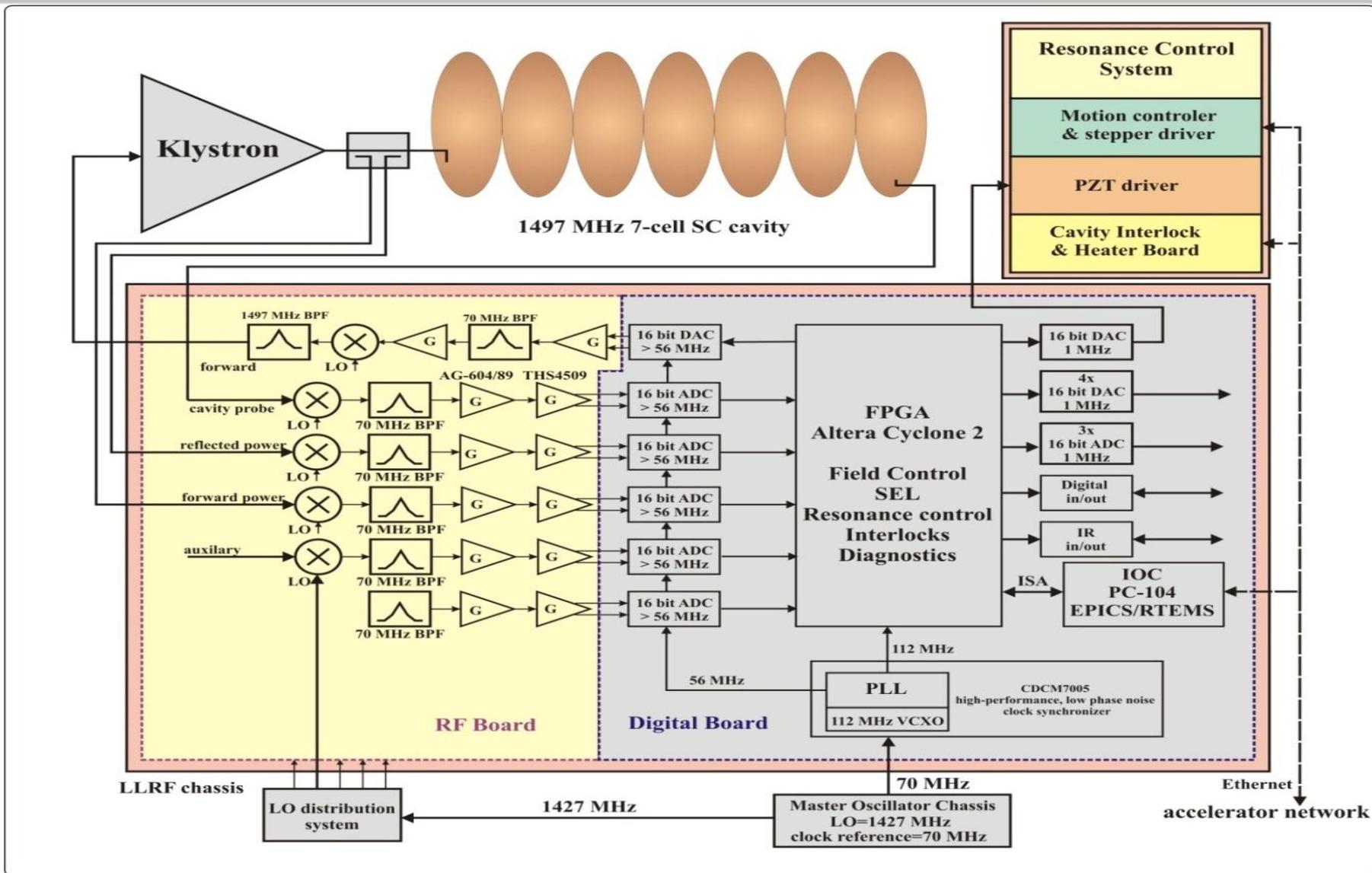


SNS RF Controls

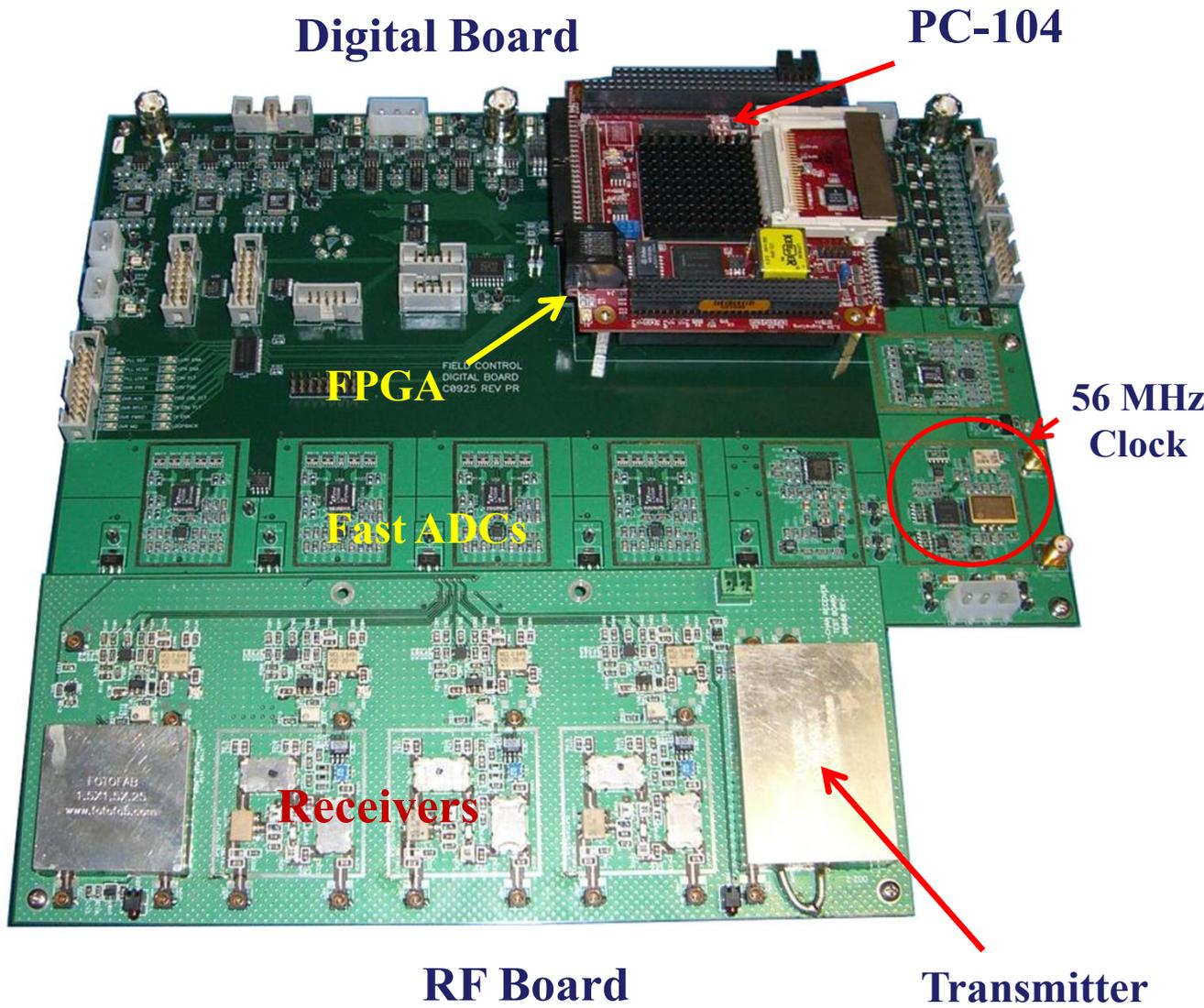


Cornel RF Controls

JLAB Upgrade RF Control System



JLAB LLRF System Architecture



- **RF Board**

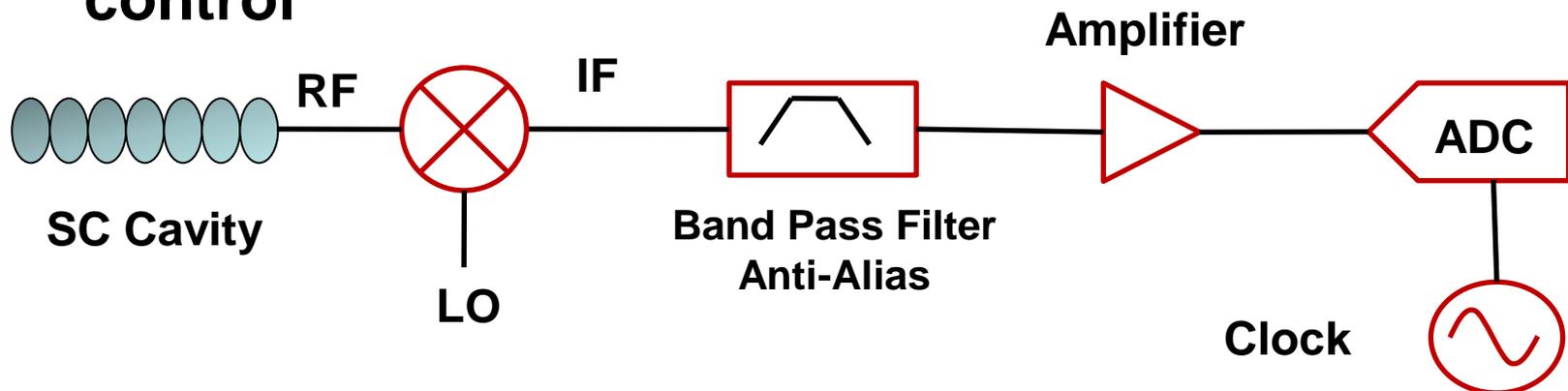
- RF = 1497 MHz, IF = 70 MHz
- 5 Receiver Channels
- One transmitter

- **Digital Board**

- FPGA: Altera Cyclone 2 EP2C35
- 16 bit ADC's & DAC
- Quadrature sampling at 56 MHz
- Ultra low noise 56 MHz clock
- IOC PC104/ RTEMS/EPICS

Receiver Basics

- Heterodyne scheme
- Noise Figure: Typically large cavity signal so not an issue
- Signal to Noise Ratio (S/R, SNR): Ultimately determines field control. Dominated by ADC
- Component linearity effects dynamic range and signal accuracy
- Clock and LO Phase Noise/Jitter can impact control

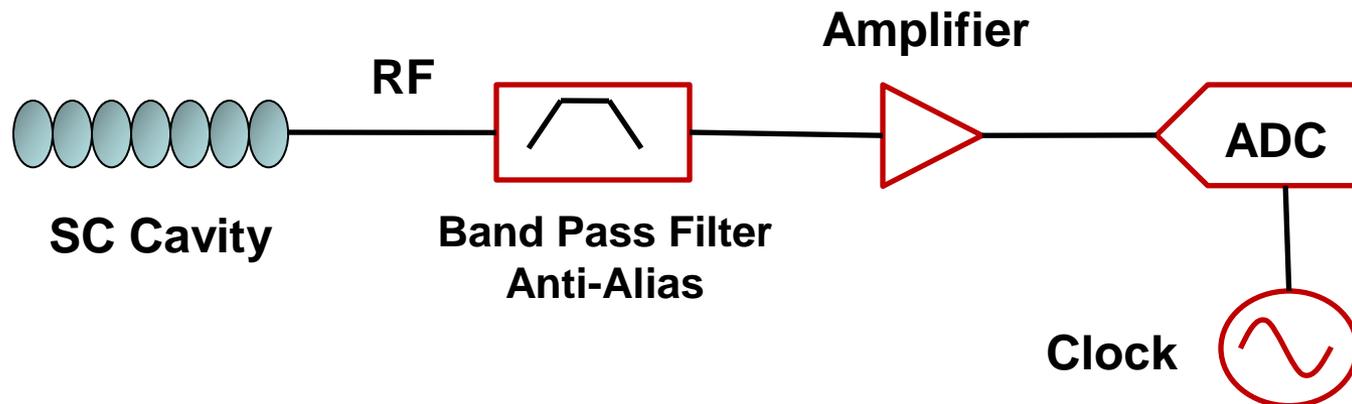


Direct Sampling

- Should be considered for frequencies < 500 MHz
- Clock jitter/phase noise is crucial
- ADC must have small aperture jitter (< 300 fs)

Benefits

- Economy \$\$\$
- Simpler receiver for multiple frequencies (i.e. FRIB)
- Simpler Master Oscillator (MO) distribution



ADC Selection

- Factors in heavily in determining your systems S/N and dynamic range
- Calculate how many bits that you need then add two!
 - Additional Cost will be minimal
- S/N determined by , number of bits, quantization error, sample rate and system jitter.

Parallel Architecture clock speed > 50 MHz

- Advantage: Wide bandwidths > 700 MHz

Serial Architecture clock speeds < 50 MHz

- Advantage: multiple channels, less pins needed, smaller FPGA

ADC Selection cont.

Whether you are down converting to an IF or Direct sampling the systems S/N needs to be determined to meet field control specifications.

The S/N of an ideal ADC is given by the following equation

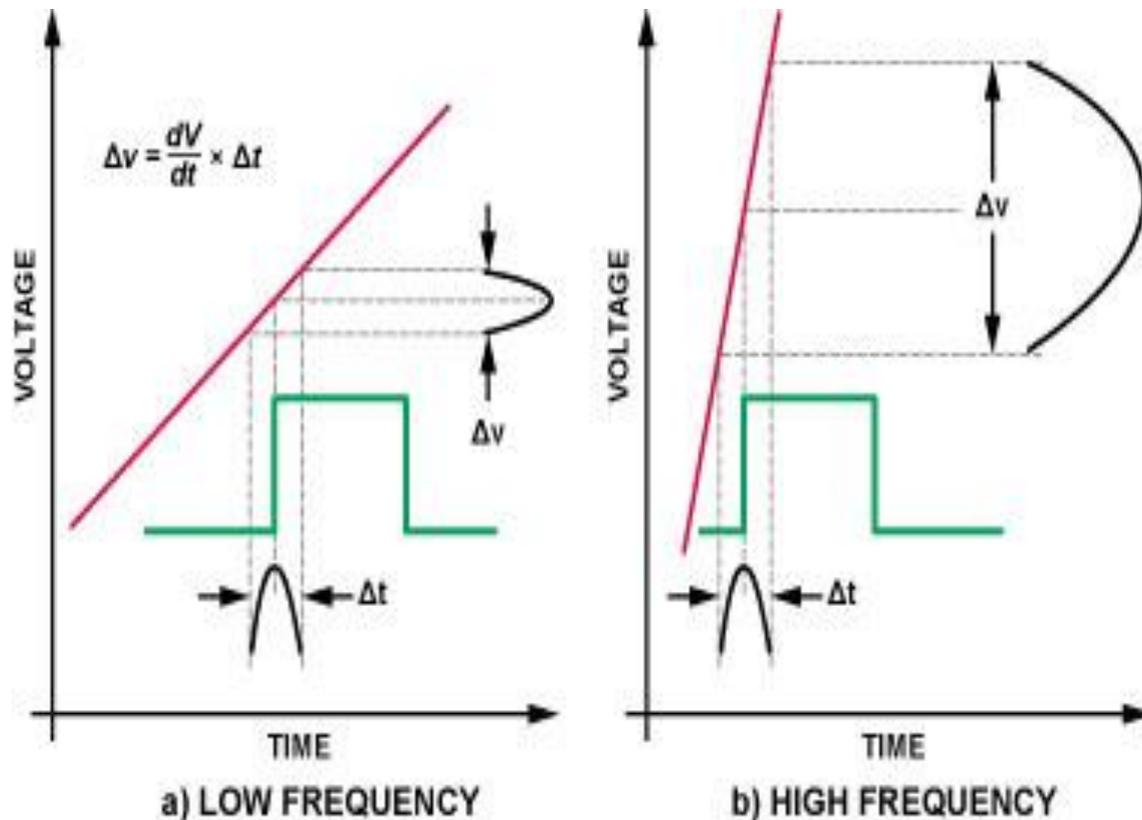
$$S / N = [6.02N + 1.76]$$

Number of bits	12	14	16
S/N (ideal) dB	74	86	98
S/N (real) dB	70	74	78

.....It gets worse

ADC – S/N

When we factor in linearity and clock jitter the S/N decreases even more. In the case of clock jitter, the conversion error can be seen below



ADC – S/N

Real world S/N equation

$$S / N = -20 \log_{10} \sqrt{(\omega_o t_{jrms})^2 + \frac{2}{3} \left(\frac{1 + \varepsilon}{2^N} \right)^2 + \left(\frac{2\sqrt{2} V_{NOISErms}}{2^N} \right)^2}$$

Where ω_o is the analog input frequency ($2\pi f$),

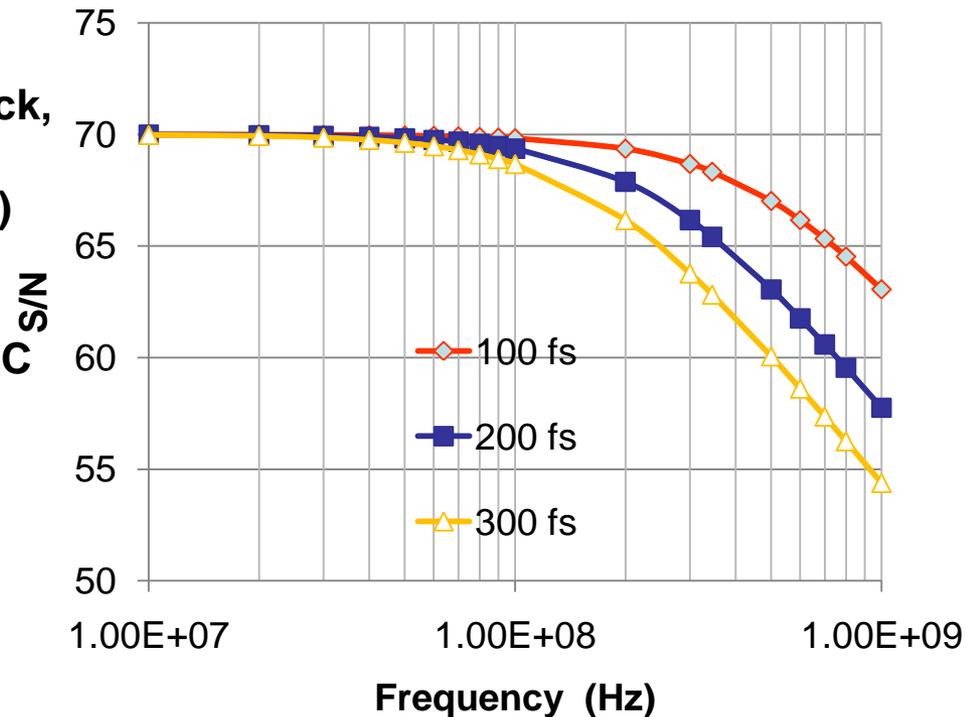
t_{jrms} is the combined jitter of the ADC and clock,

ε is the average differential nonlinearity (DNL) of the ADC in LSBs,

$V_{NOISErms}$ is the effective input noise of the ADC in LSBs and

N is the number of ADC bits.

12 Bit ADC S/N vs Input Frequency



Phase Noise and Timing Jitter

- **Phase Noise** is the parameter used in the communication industry to define an oscillators spectral purity.
- **Timing Jitter** is the parameter most used by accelerator designers in describing beam based specifications and phenomena.
- Phase noise spectrum can be converted to a timing jitter using the formula

$$\tau = \frac{\sqrt{2 \cdot 10^{A/10}}}{2\pi f_o}$$

Where A is the area under the curve

Signal Source Phase Noise

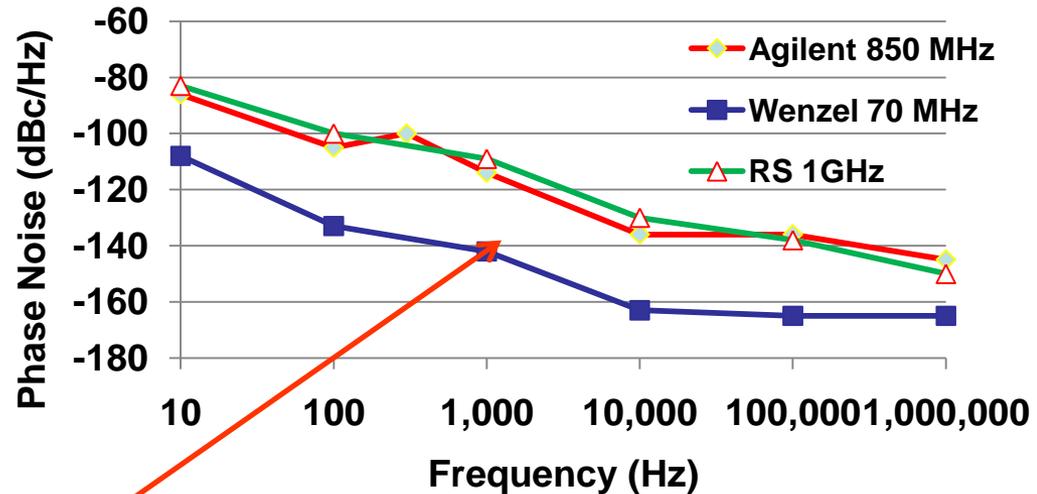
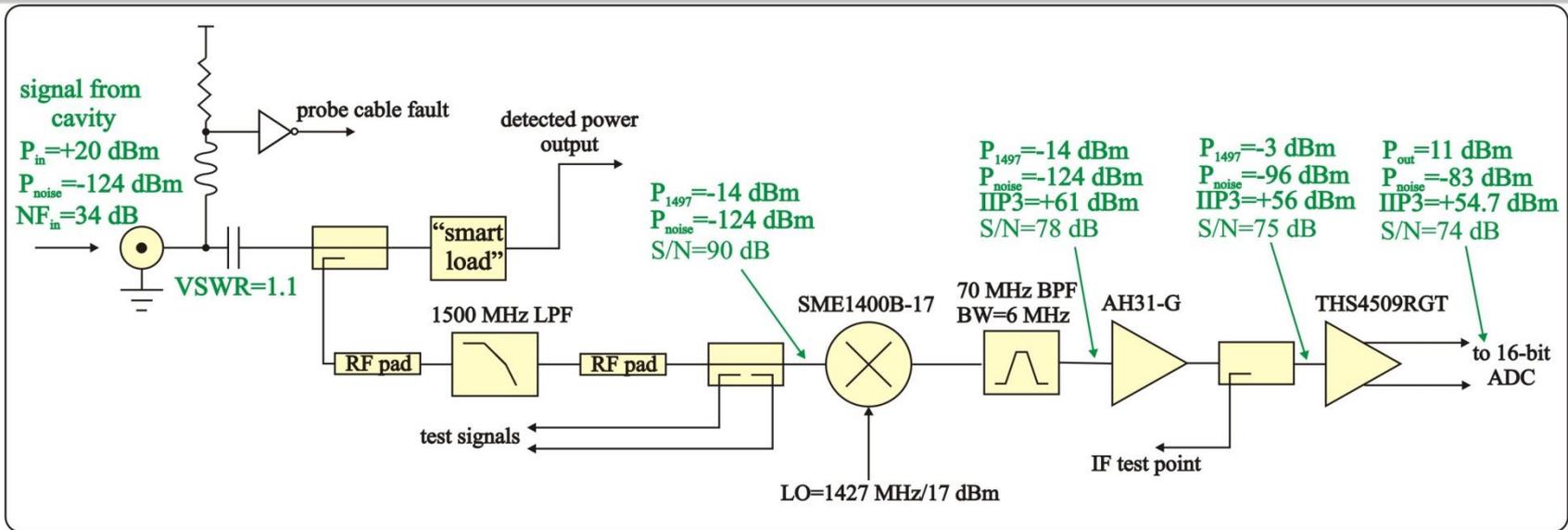


Table: Signal Source Jitter

Signal Source	Integrated Phase Noise (dBc/MHz)	Jitter (RMS)
Agilent(1497 MHz)	-67.5	63 fs
Rhode Schwarz(1497 MHz)	-64.0	76 fs
Wenzel (70 MHz)	-97.1	45 fs

JLAB Upgrade RF Receiver



Parameter	Specification Value	Imposing Quantities
S/N	72 dB	0.1 degree resolution, 0.01% gradient accuracy
Bandwidth	8 MHz	Latency, S/N, temperature stability
Latency	100 ns	Control BW
Noise Figure (NF)	52 dB, BW = 100 kHz	S/N for phase resolution
Linearity	0.01% F.S.	Stability, accuracy
Dynamic Range	+54 dBm IIP3	Gradient range
Channel Isolation	67 dB	Phase, gradient resolution/accuracy
In-band intermodulation distortion (IMD)	67 dBc	THD

Field Control: Amplitude

Receiver S/N determines minimum residual amplitude control

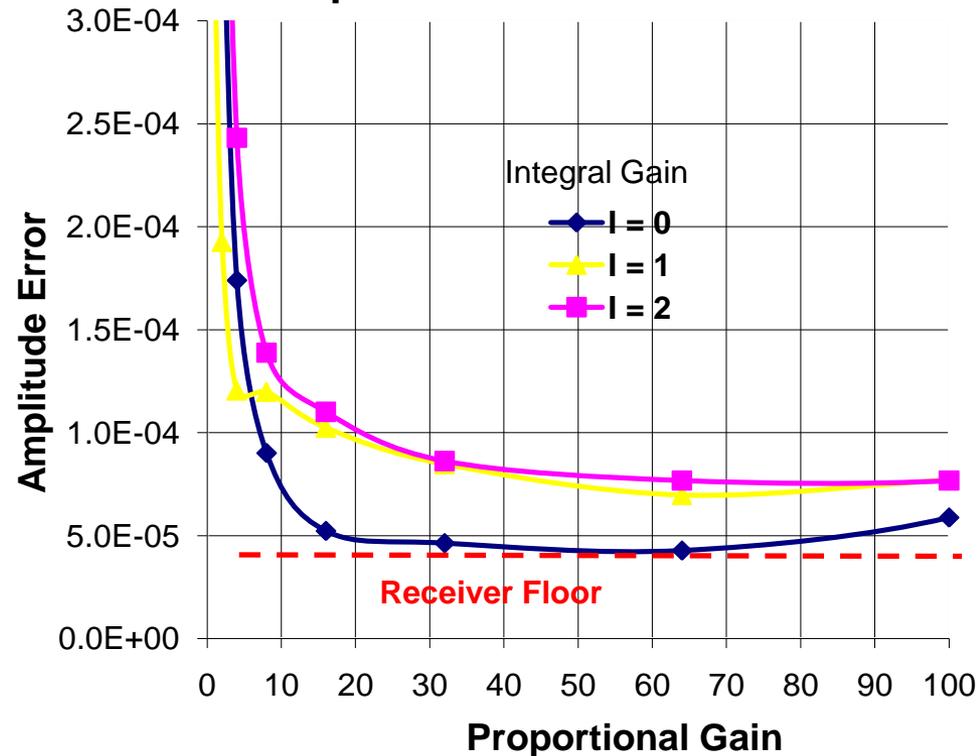
- Amplifiers
- Mixer
- ADC

- Linear components needed for stability and accuracy over large dynamic range

It is possible to improve S/N, through process gain, but at the expense of control bandwidth and ultimately stability (latency).

References: 30

Measured Amplitude Error vs. Proportional Gain



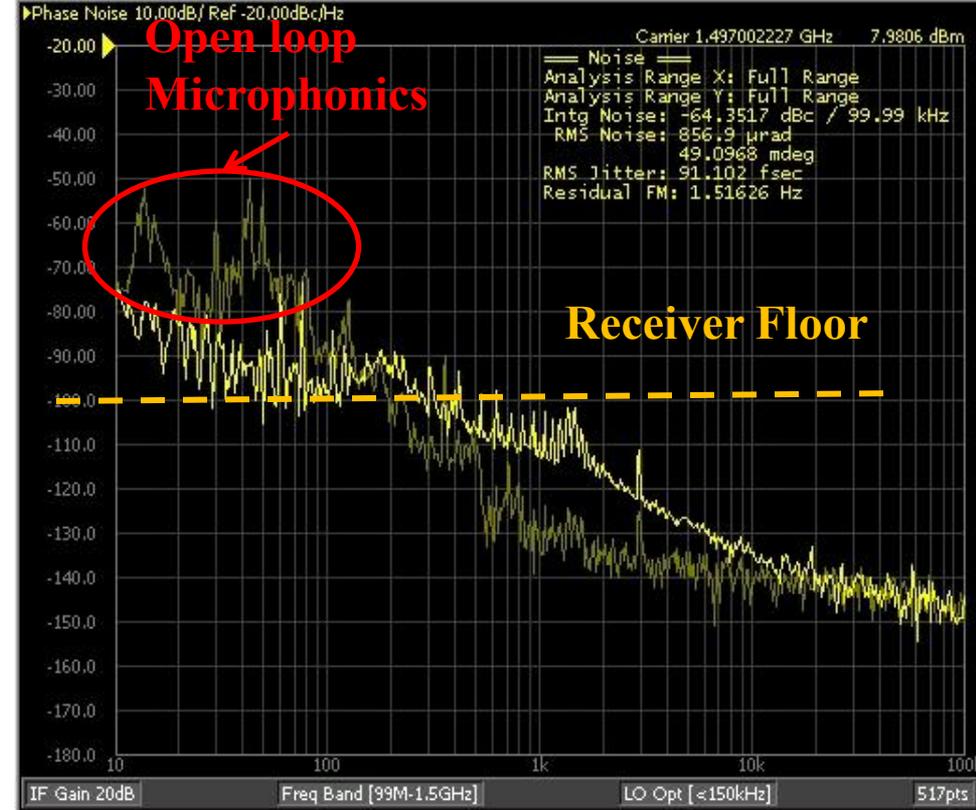
RF=1497 MHz

IF = 70 MHz

ADC = 14 bits

Field Control: Phase

- Highly dependent on the reference (LO/IF) and subsequent board level clock
- Linear components needed to minimize AM to PM contributions
- ADC aperture jitter ~ 100 fs
- Some ADC linearity can be improved with near quadrature sampling



**Phase Noise of Open and Closed Loop.
Bright Yellow is Closed loop.**

Digital Signal Processing

FPGA or DSP?

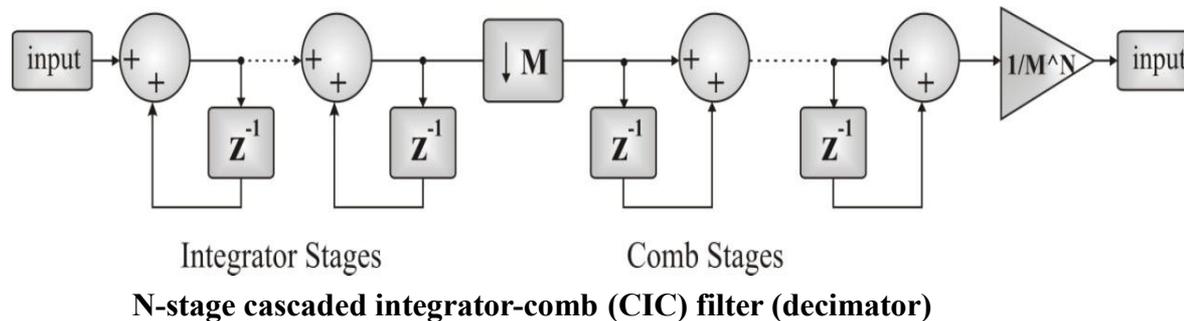
- For fast processing FPGA wins
- DSP a little more flexible but FPGAs not far behind
- Suggest FPGA followed by a small CPU (ColdFire or PC104) of some sort (best of both worlds!)
- For FPGA calculate your gate needs then double or triple the size to be safe. *Cost is a wash.*

FPGA: Xilinx ... Altera Both are used by the accelerator community

DSP: Texas Instruments ...Analog Devices dominate industry

Digital Signal Processing

- I/Q easiest to implement
- Non I/Q sampling eliminates ADC non-linearities
- Frontend processing can be decimation followed by FIRnot efficient
- Better method is to use a Cascaded-Integrated-Comb (CIC).



- PID algorithm simplest for CW applications
- PID can be enhanced with feed-forward or gain scheduling for use in pulsed systems.

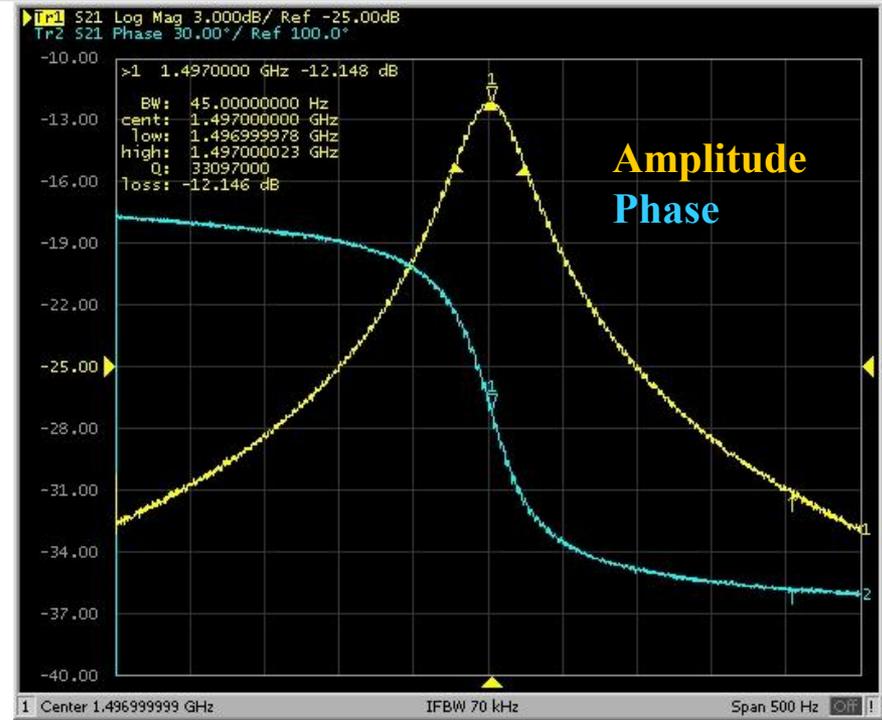
Digital Signal Processing

- **IIR Filter: Best for realizing analog filters**
 - Need to decimate to F_s/F_o of ~ 100 to insure stability
 - Can have high-gain and round off errors
- **Oversampling can improve S/N by $\sim 20\log(N^{1/2})$, but at the expense of control bandwidth**

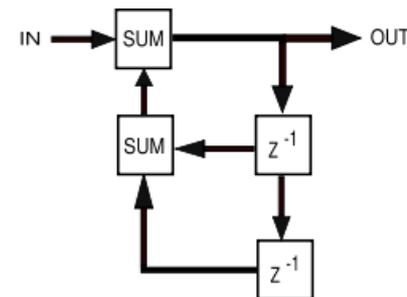
Example:

clock = 50 MHz and bandwidth needed is 1 MHz. The potential S/N improvement would be 17 dB

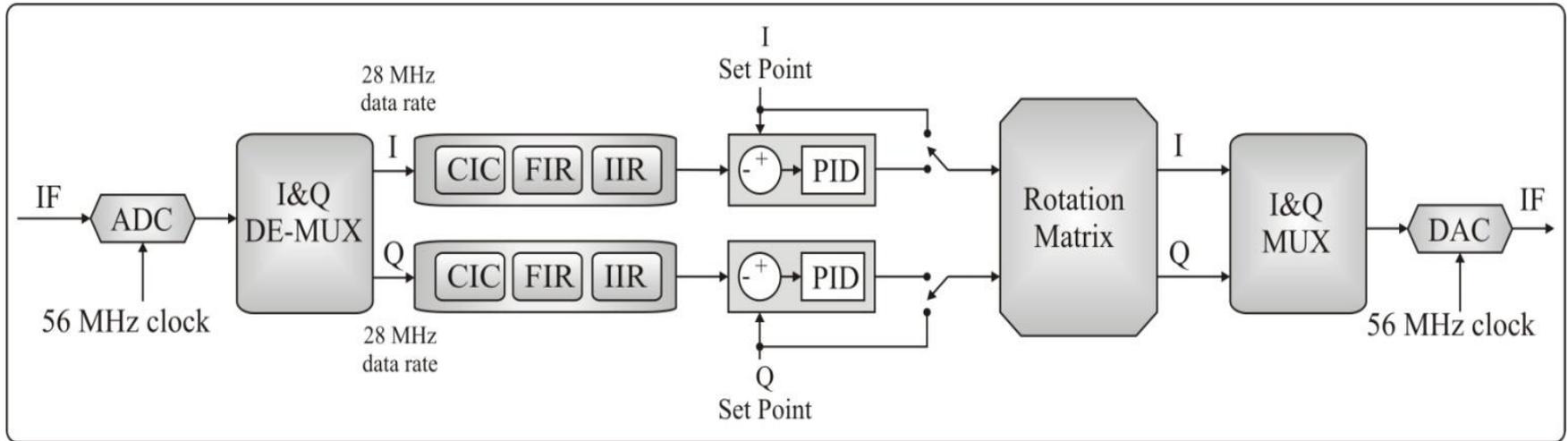
References: 30



Cavity Emulator using IIR Filter



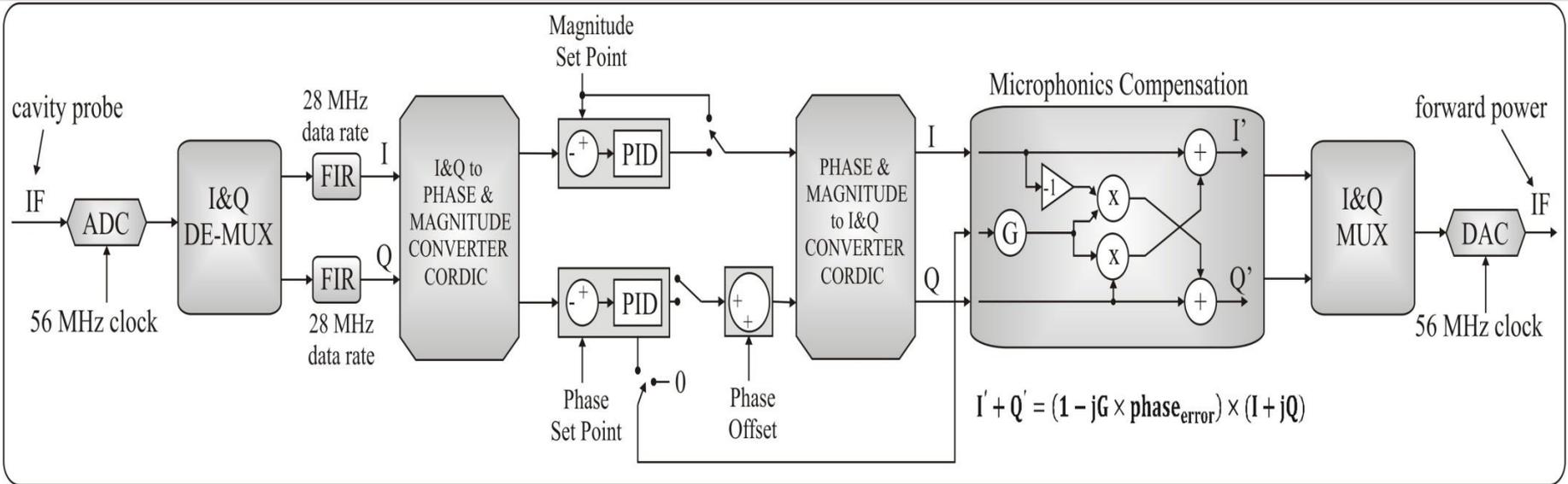
Signal Processing Block Diagram: GDR



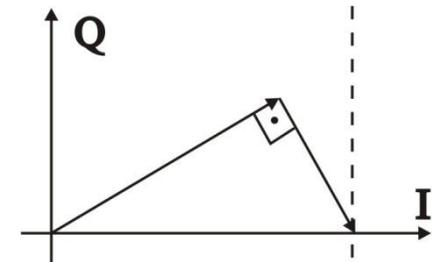
- IF direct I&Q sampling
- Digital filtering
- PID controller for I and Q values
- Rotation matrix
- Single DAC generating IF signal

References: 31

Signal Processing Block Diagram: SEL



- IF direct I&Q sampling
- digital filtering
- I&Q to Phase&Magnitude - COordinate Rotation Digital Computer (CORDIC)
- SEL mode
- Microphonics Compensation
- single DAC generating IF signal



References: 31

Digital SEL Tests

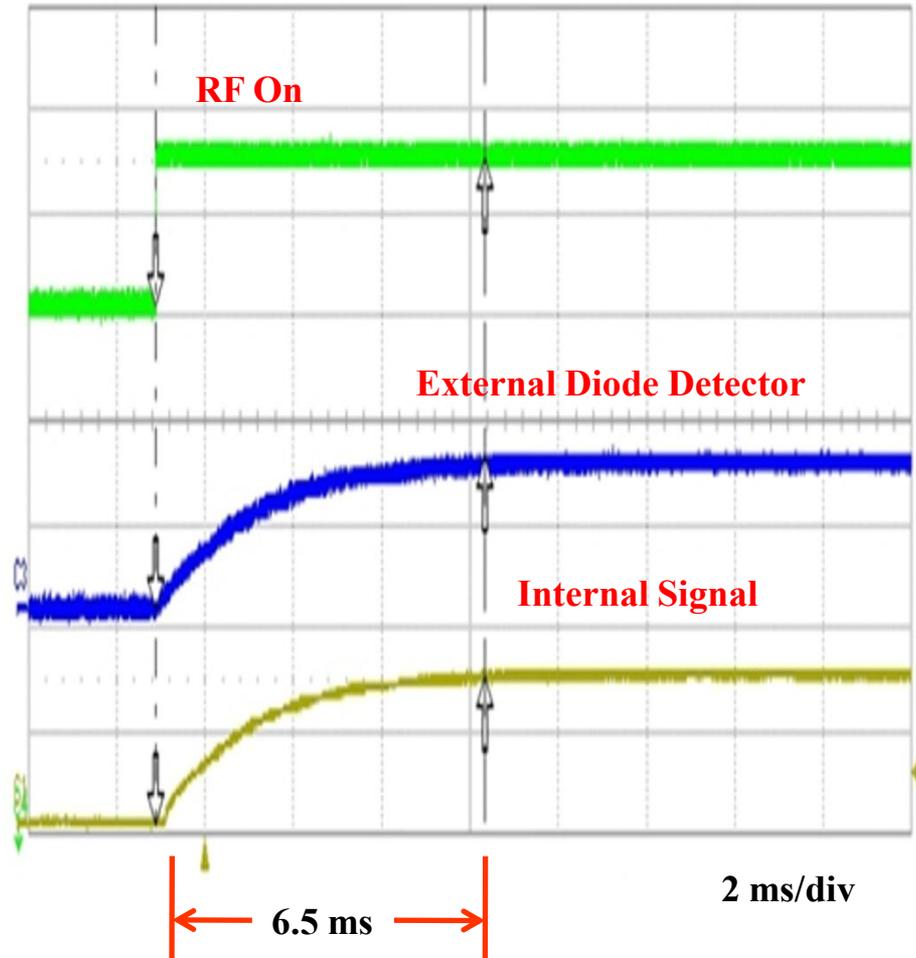
SEL mode

- Detuned the cavity by +/- 50 kHz and RF system tracked it.
- RF turn on of the detuned cavity system works perfect, no excessive power needed!

Microphonics compensation

- Phase regulation: phase noise dropped from 1.2 deg RMS down to 140 mdeg RMS
- AM noise when compensator is ON is around 0.2 % . (w/o amplitude feedback)

0 to 20 MV/m in 6.5 ms!



References: 30

CORDIC Algorithm

- **C**Oordinate **R**otation **D**igital **C**omputer
- Iterative method for determining magnitude and phase angle
 - **Avoids multiplication and division**
- $N_{\text{bits}} + 1$ clock cycles per sample
- Can also be used for vectoring and linear functions (eg. $y = mx + b$)
- Exploits the similarity between 45° , 22.5° , 11.125° , etc. and Arctan of 0.5, 0.25, 0.125, etc.
- **Multiplies are reduced to shift-and-add operations**

Angle	Tan ()	Nearest 2^{-N}	Atan ()
45	1.0	1	45
22.5	0.414	0.5	26.6
11.25	0.199	0.25	14.04
5.625	0.095	0.125	7.13
2.8125	0.049	0.0625	3.58
1.406125	0.0246	0.03125	1.79
0.703125	0.0123	0.01563	0.90

$$[x', y'] = [x, y] \cdot \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$$

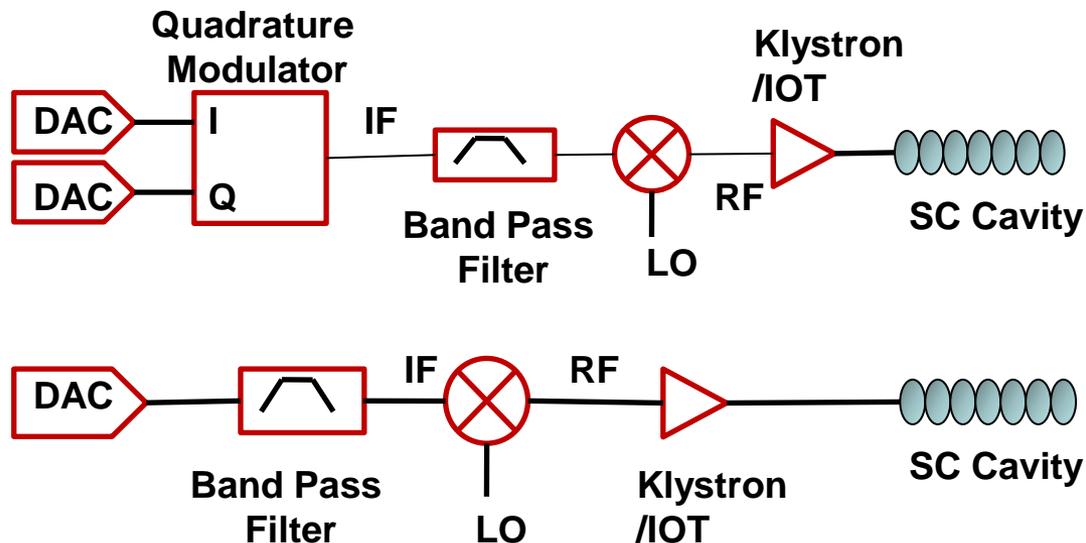


$$\begin{aligned} x_{i+1} &= K_i [x_i - y_i \cdot d_i \cdot 2^{-i}] \\ y_{i+1} &= K_i [y_i + x_i \cdot d_i \cdot 2^{-i}] \end{aligned}$$

References: 33, 34

Transmitter/Up Conversion

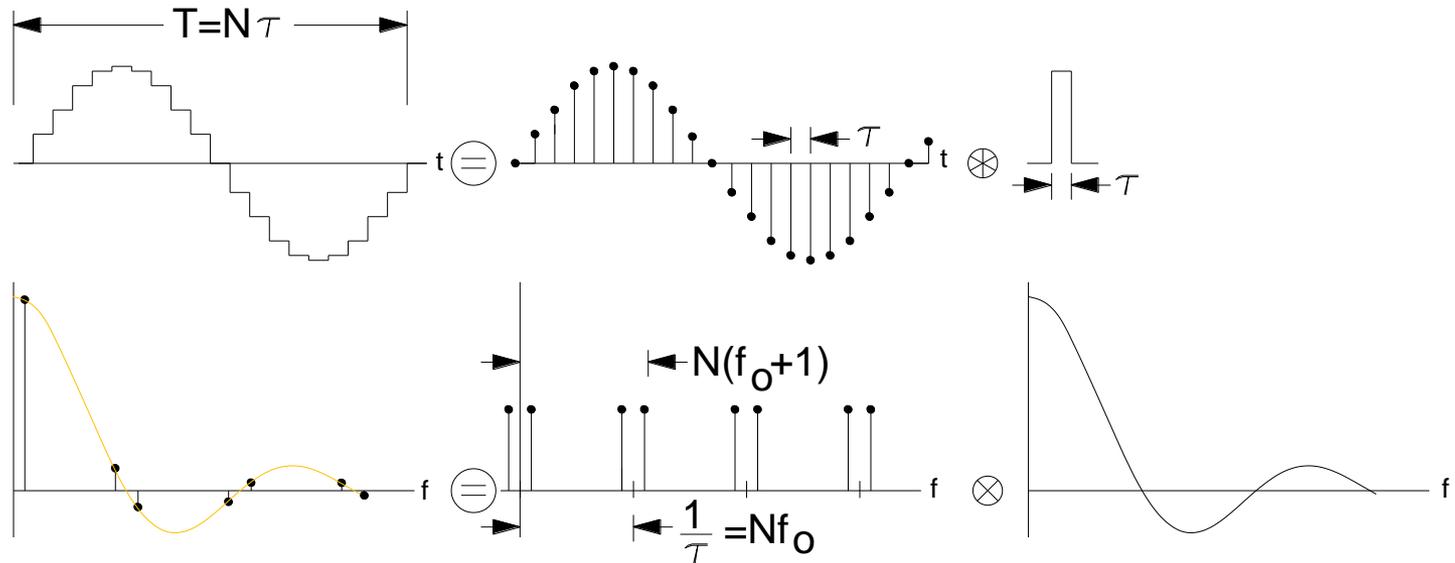
- DAC typically the same number of bits as the ADC
- DAC needs to be fast enough to support IF generation or RF Conversion if Direct Sampling
- Mixer specification (notably IP3) can be relaxed from cavity mixer.
- Depending on pre-amp (solid state) and power amplifier (Klystron/IOT), you may need to filter out LO.



Direct Digital IF Signal Generation

Single DAC can eliminate Quadrature Modulator

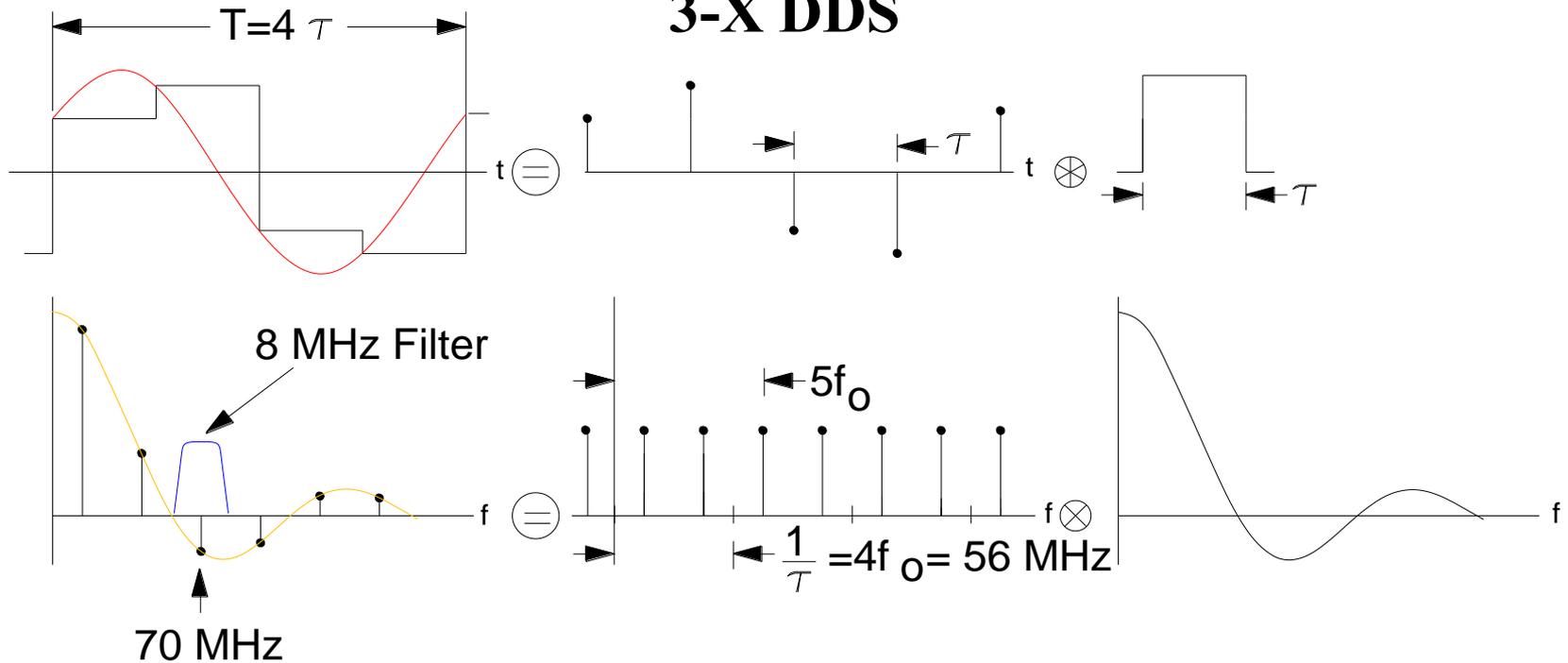
See Larry Doolittle web page: <http://recycle.lbl.gov/~ldoolitt/plan50MHz/>



- Concept use one of the harmonics out of your ADC for your IF frequency.
- For a 10-X system two disadvantages to using second or third harmonic frequencies are:
 - Small signal content.
 - Analog filter requirements.

Direct Quadrature IF Up Conversion

3-X DDS



- Ratios of f_3 to f_1 is 1:5.
- 70 MHz component is 14 MHz away from nearest neighbor.
- Commercial drop in 8 MHz BW filter available for \$30.
- One can show that the harmonic contains the proper phase signal and is:

$$A \sin(2\pi f_0 + \varphi) \Rightarrow B_k A \sin(2\pi(kf_S \pm f_0)t + \varphi) \text{ where } k = 0, 1, 2 \dots$$

Cavity Resonance Control

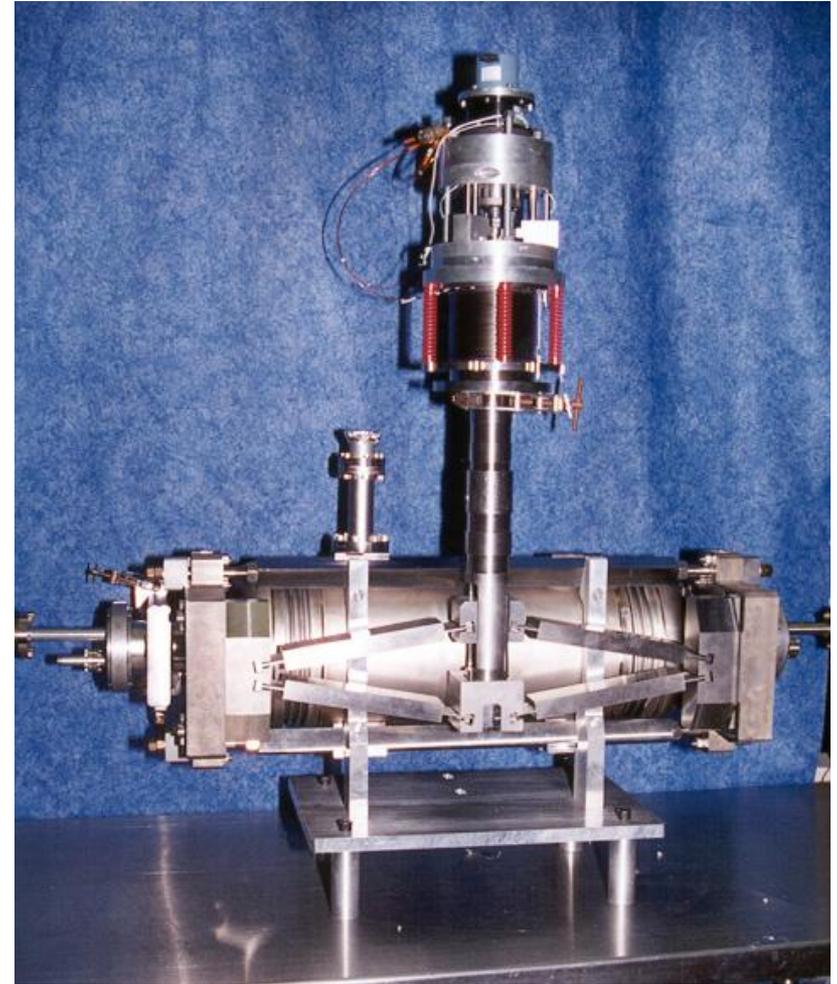
Goals of a resonance control system

- Keep the cavity as close as possible to the reference frequency, ultimately minimizing forward power.
- Compensates for Lorentz detuning for pulsed systems
- Minimize microphonics to assist electronic feedback
- **Reliable and maintainable**

Tuning Methods

- Stepper Motor: speed < 1 Hz
- Piezo tuner: speed > 1 Hz

References: 19



Prototype tuner for CEBAF Upgrade

Cavity Resonance Control Over 20 Years

- Example CEBAF (1986) to CEBAF Upgrade (2008)

	Frequency	Gradient	Bandwidth	Lorentz detuning	Range	Resolution	Tuning method	Drive
CEBAF	1497 MHz	5 MV/m	220 Hz	75 Hz	+/- 200 kHz	10 Hz	Ten/Comp	Stepper
CEBAF Upgrade	1497 MHz	20 MV/m	50 Hz	800 Hz (est.)	+/- 200 kHz	< 1Hz	Tension	Stepper & PZT

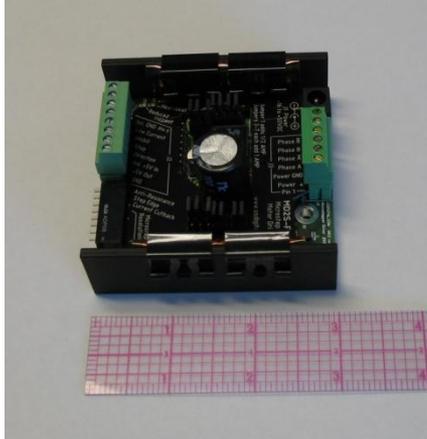
- *Gradients increased five fold in 20 years bringing Lorentz detuning into play and the need to keep klystron size small.*
- *Tuner designs responded with faster tuning methods (PZT) and increased resolution.*
- *Future/Now: active mechanical compensation of microphonics*

References: 19

Coarse/Slow Tuner

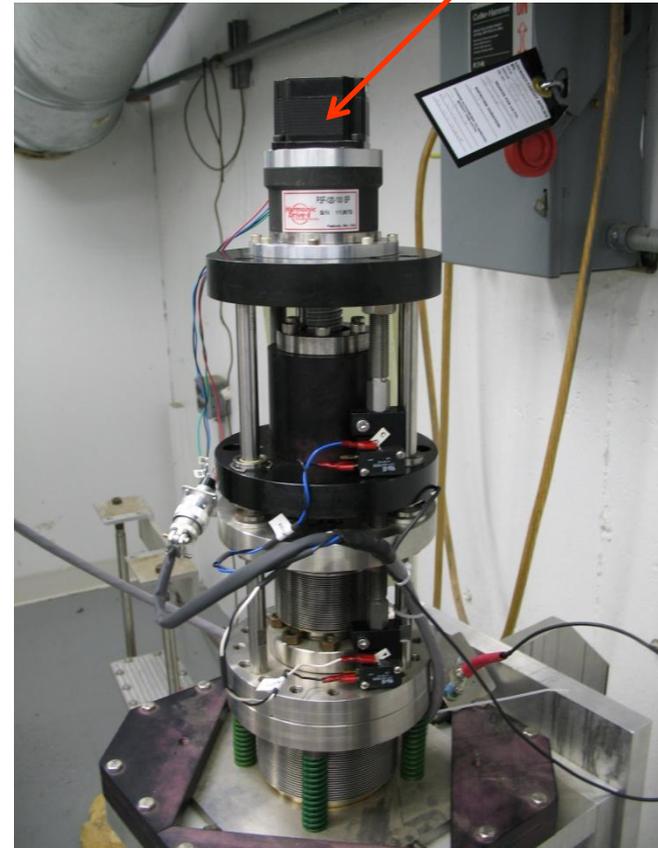
Stepper Motor:

- Recover cavity from large excursions associated with down time activities or Cryogenic trips.
- Keeps the Fast Tuner centered
- Control can be slow < 1 sec



Stepper Motor Driver

Stepper motor



JLAB Upgrade Tuner assembly

Fine/Fast Tuner

Piezo-Electric Tuner (PZT):

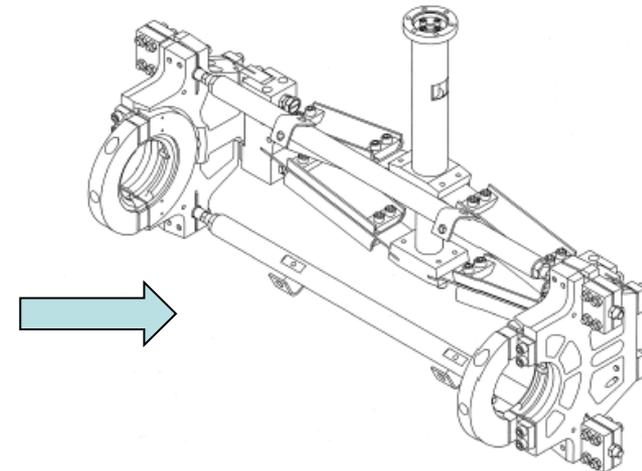
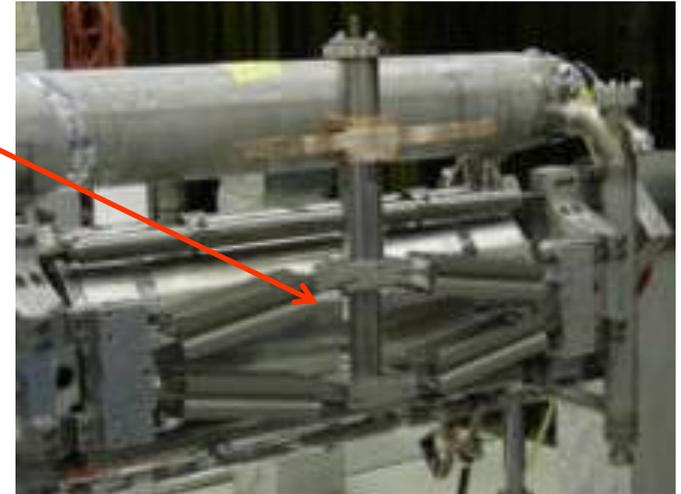
- Large Industrial base for Piezo and electronics
- **Recover or compensate for Lorentz Detuning (Feed Forward or Feedback)**
- Minimizes small changes in resonance do to He pressure.
- Speed < 1 ms
- Control logic embedded in FPGA or fast DSP
- **Warm Stroke greater than Cold Stroke**



Has been demonstrated to minimize cavity microphonics

Upgrade Tuner for SL21 and FEL03 Cryomodules

- **Scissor jack mechanism**
 - Ti-6Al-4V Cold flexures & fulcrum bars
 - Cavity tuned in tension only
 - Attaches on hubs on cavity
- **Warm transmission**
 - Stepper motor, harmonic drive, piezo and ball screw mounted on top of CM
 - Openings required in shielding and vacuum tank
- **No bellows between cavities**
 - Need to accommodate thermal contraction of cavity string
 - Pre-load and offset each tuner while warm

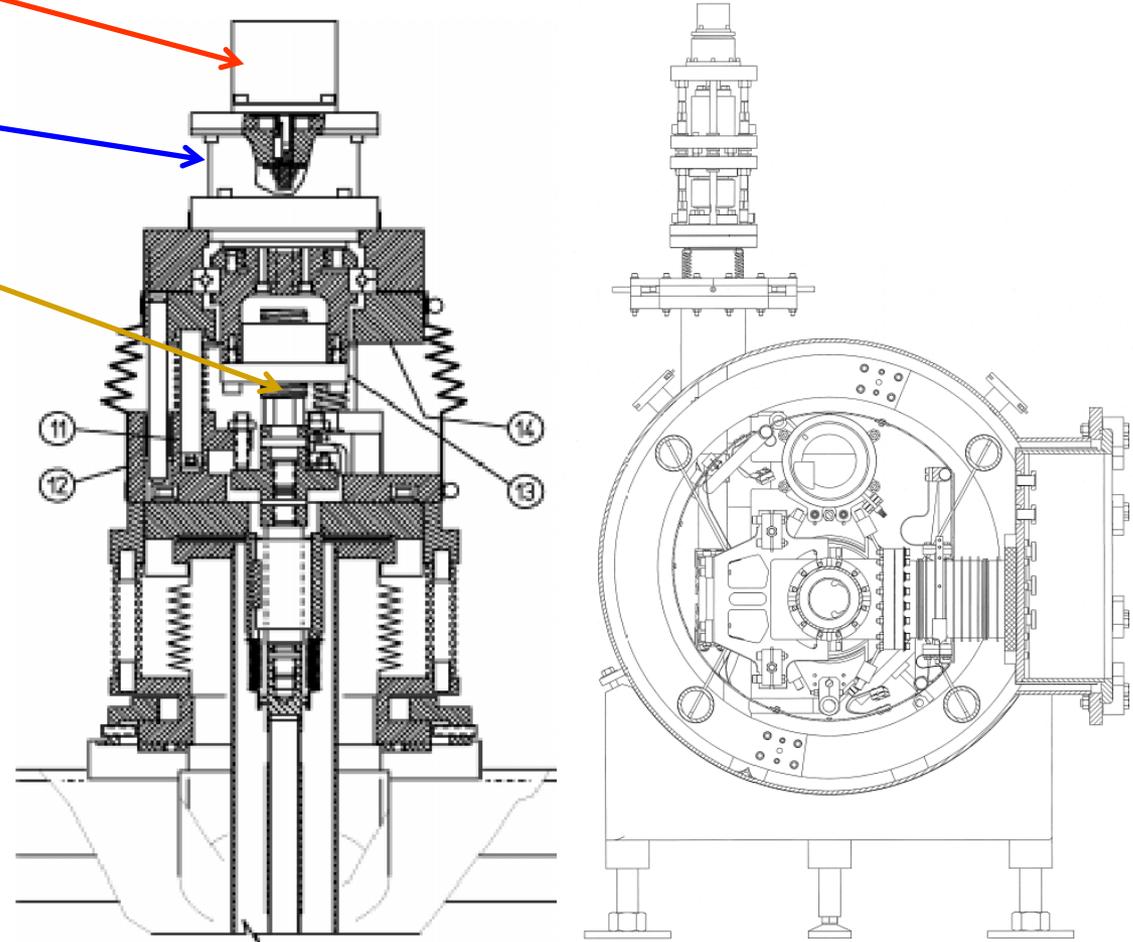


Evolution of the tuner!

References: 19

Warm Drive Components and Cross Section of Upgrade CM

- Stepper Motor
 - 200 step/rev
 - 300 RPM
- Harmonic Drive
 - Gear Reduction = 80
- Low voltage piezo
 - 150 V
 - 50 μm stroke
- Ball screw
 - Lead = 4 mm
 - Pitch = 25.75 mm
- Bellows/slides
 - axial thermal contraction

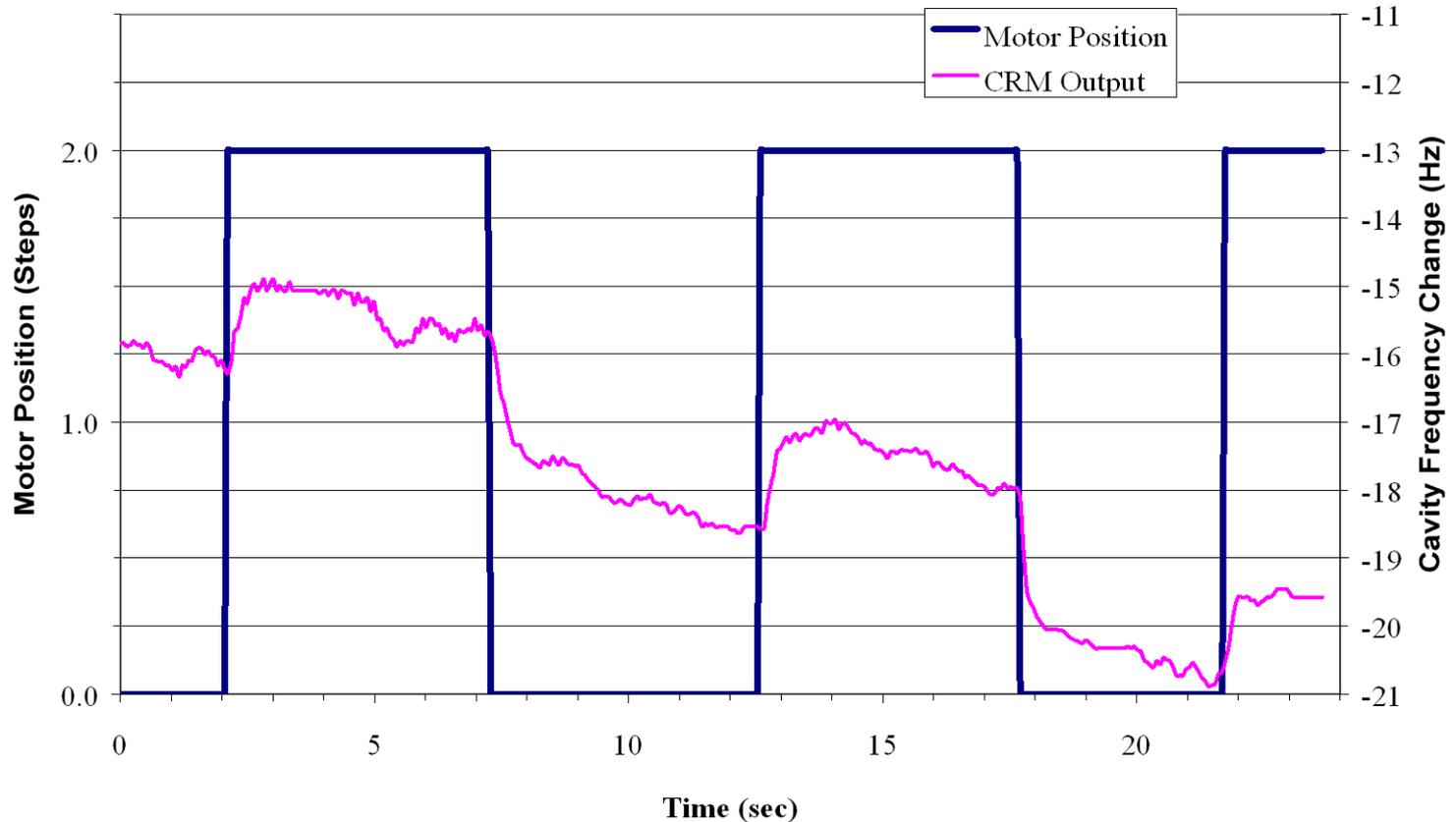


References: 19

CEBAF Upgrade Coarse Tuner Resolution/Deadband Test

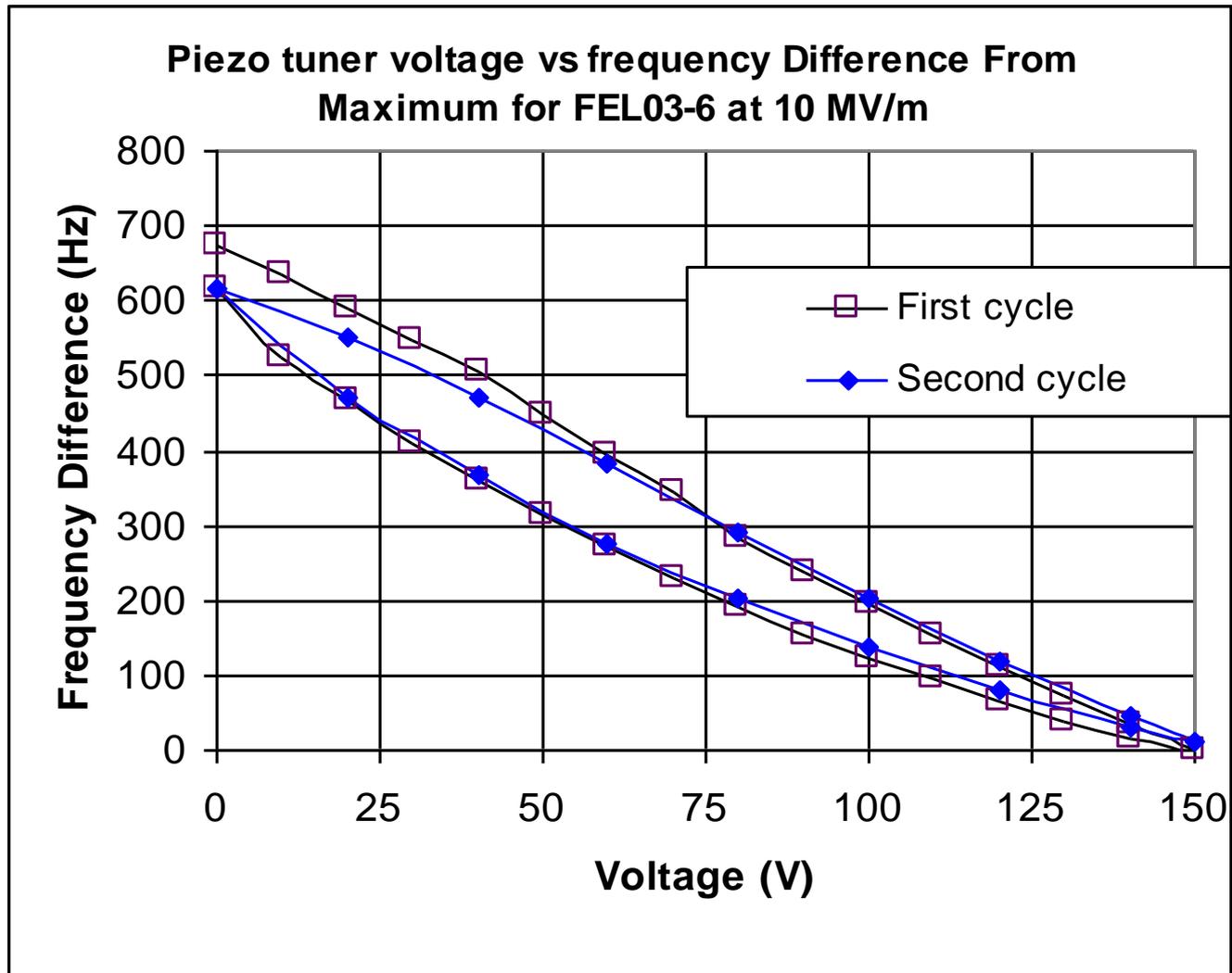
Resolution/Deadband < 2 Hz

Drift due to Helium pressure fluctuations



References: 3

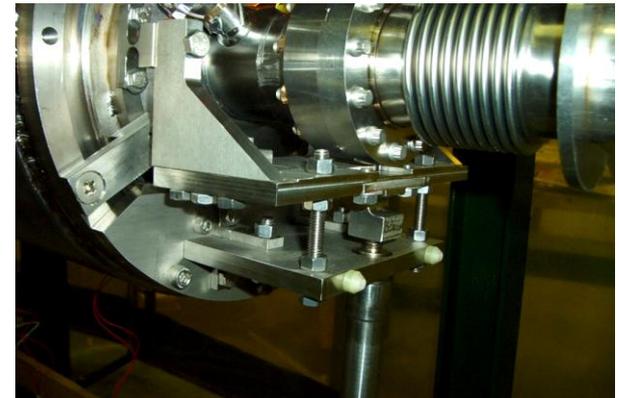
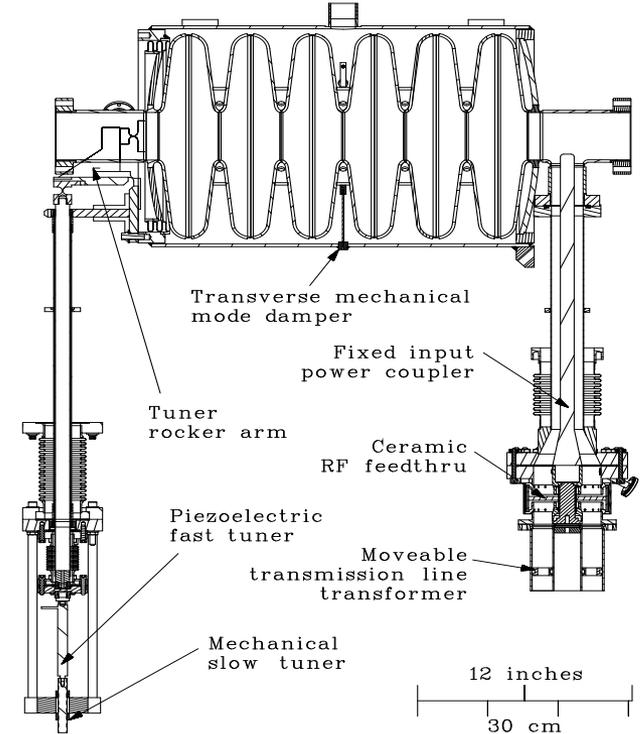
Upgrade Tuner – SL21 / FEL03 : Resolution (Piezo Hysteresis)



References: 3

RIA Tuner (MSU)

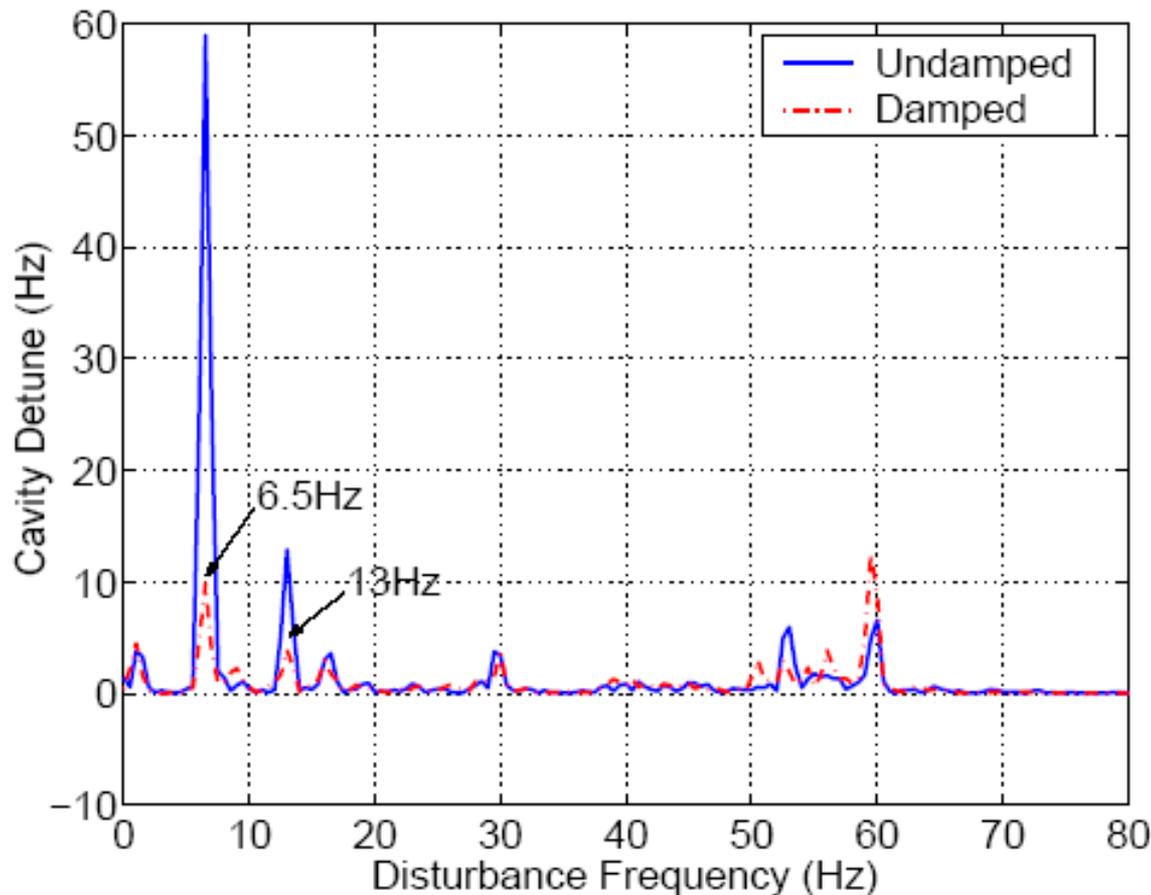
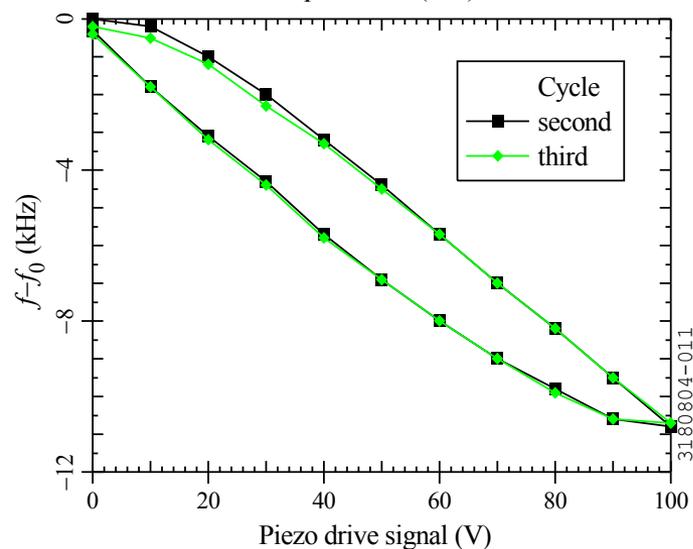
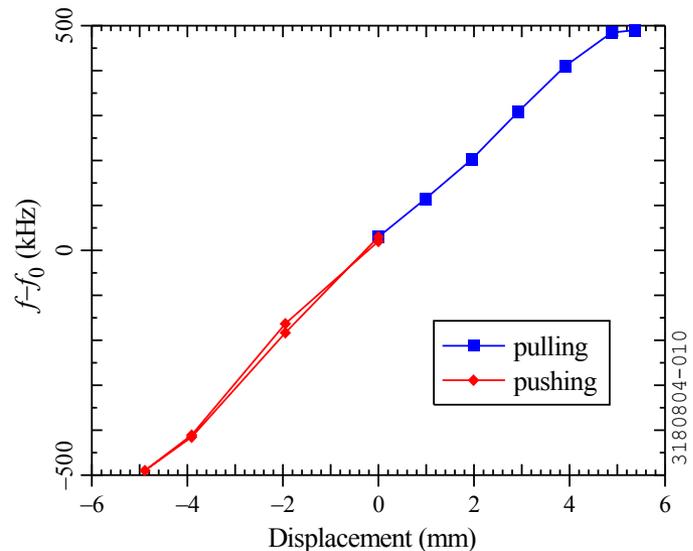
- **Mechanism**
 - Stainless steel rocker arm and drive rod
 - Attaches to chocks on cavity
 - Attaches via flexures and threaded studs to helium vessel head
 - Cavity tuned in compression or tension
- **Cold transmission – compressive/tensile force on drive rod**
- **Stepper motor and piezo external to vacuum tank**
- **Bellows on vacuum tank**
 - Need to accommodate relative thermal contraction of cavities
 - Allow tuner transmission to float (unlocked) during cooldown
 - Pre-load each tuner while warm, account for vacuum loading on bellows



References: 19

RIA Tuner – Test Results:

Coarse and Fine Tuner Range; Active Feed-forward Control

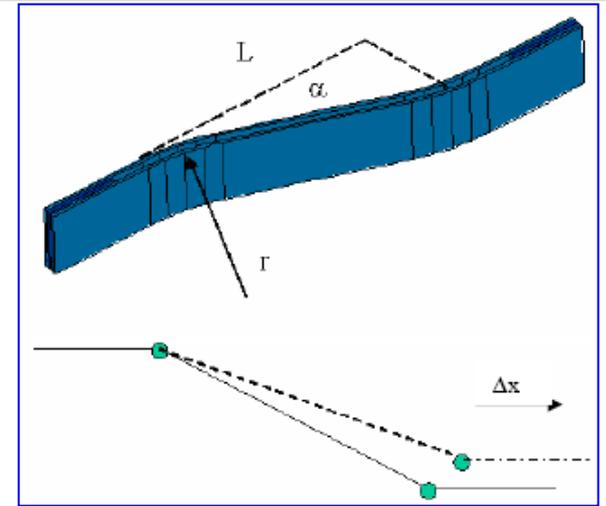


T. Kandil LINAC 2004

References: 19

Blade Tuners

- 1 mm fine tuning (on cavity) → ΔF on all piezo (sum) \approx 3.5 kN
- 1 kHz fast tuning → \approx 3 μm cavity displacement → \approx 4 μm piezo displacement
- 4 μm piezo displacement → \approx ΔF on all piezo \approx 11.0 N
- \sim 1 Hz resolution (sufficient if $<5\text{Hz}$)

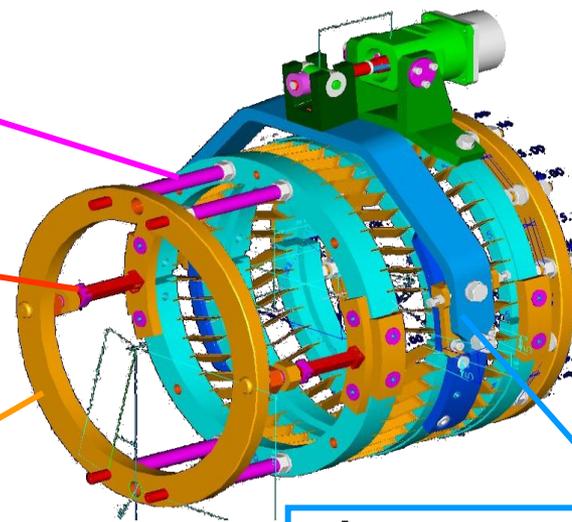


Stiffeners bars could be used in working cond. as safety devices.

Piezo

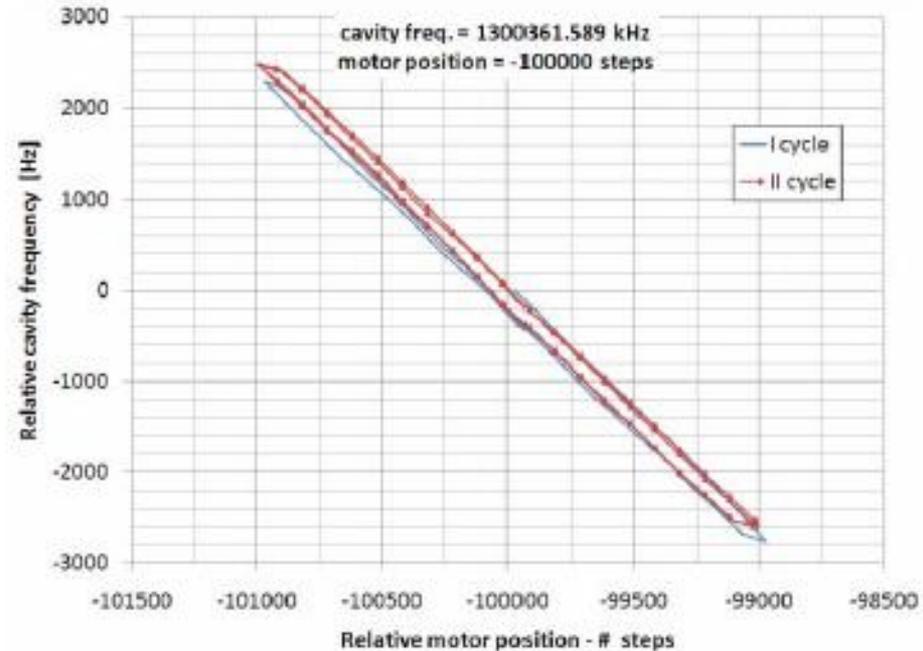
Ti or SS ring welded on the tank

Leverage arm



References: 19, 21

ILC-TTF Blade Tuners



- **Mechanism – All cold, in vacuum components**
 - Stainless Steel frame
 - Low voltage 40 mm Noliac Piezo
 - Attaches to helium vessel shell
 - Phytron stepper motor with planetary gear box
 - Cavity tuned in tension or compression – blades provide axial deflection

References: 21

PZT Power Supply

Piezo tuner is basically a capacitive device.

Current is only needed during dynamic tuning

$$I = C \frac{dV}{dt} \sim j\omega CV$$

Which ultimately determines the size of your power supply.

Example: JLAB PZT

Voltage Range : 0 to 150 volts (full stroke)

Capacitance: 21 uF (warm)

Tuning range: 0 to 2000 Hz (0 to 150 Vdc)

We have observed a mechanical perturbation at a frequency of 8 Hz

The perturbation effect on cavity detuning is 60 Hz (@ 1497 MHz)

PZT Power Supply

Goal is to damp the 8 Hz Perturbation

Since it has 60 Hz detuning the PZT voltage will need to be compensate over the range of

$$60 / 2000 \times V = 4.5 \text{ Volts}$$

Putting this into the previous equation ($I=j\omega CV$) gives us

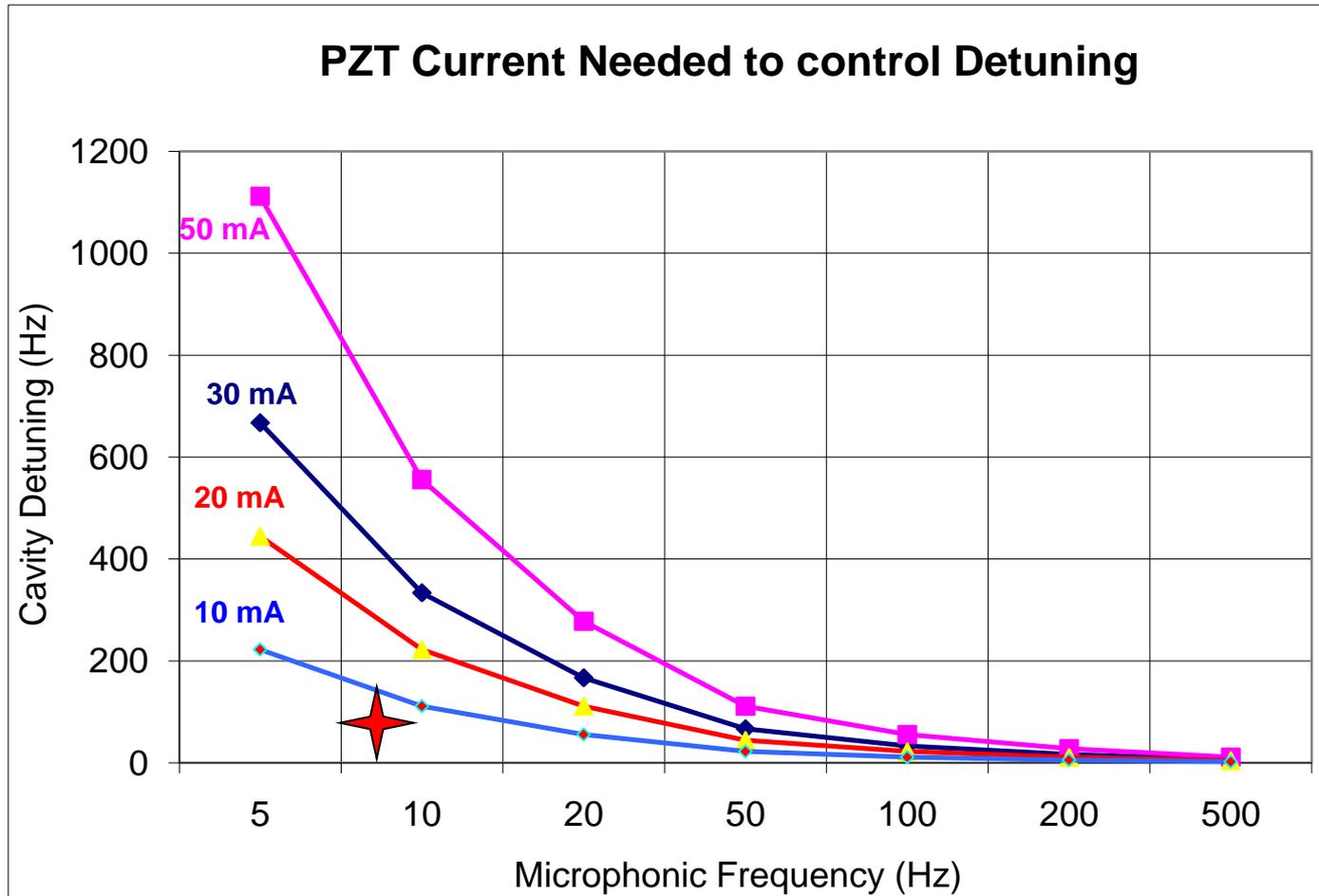
$$I = 2 \times \pi \times 8\text{Hz} \times 21\mu\text{F} \times 4.5 = 4.75 \text{ mA}$$

Which is a relatively small power supply.

As a comparison a system with a 1000 volt PZT (same stroke), and a similar disturbance the current required is 31.7 mA

Some thought needs to go into PZT voltage for safety too!

PZT Power Supply

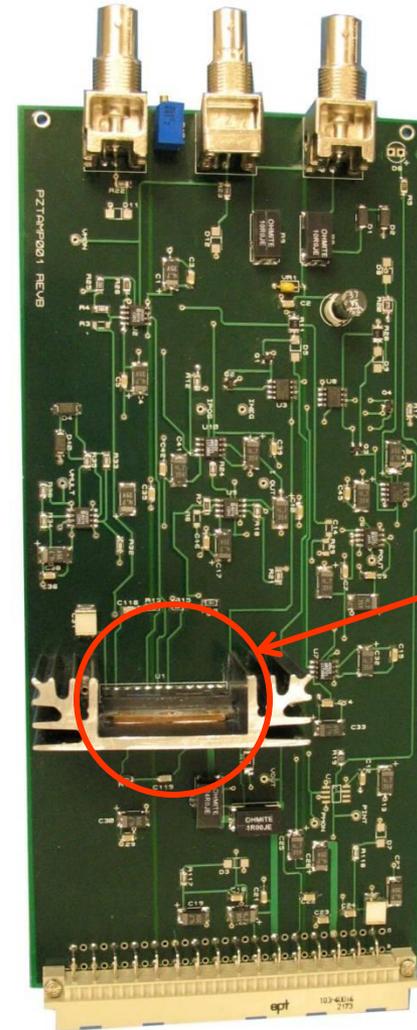
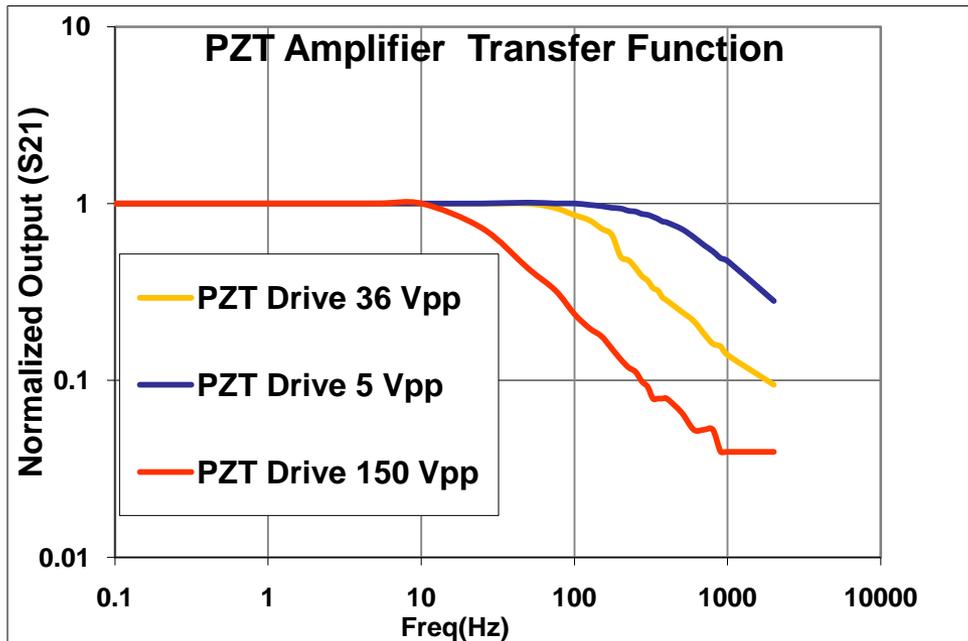


Assumes 150 Vdc PZT with 2000 Hz full stroke

JLAB Piezo Tuner

Features

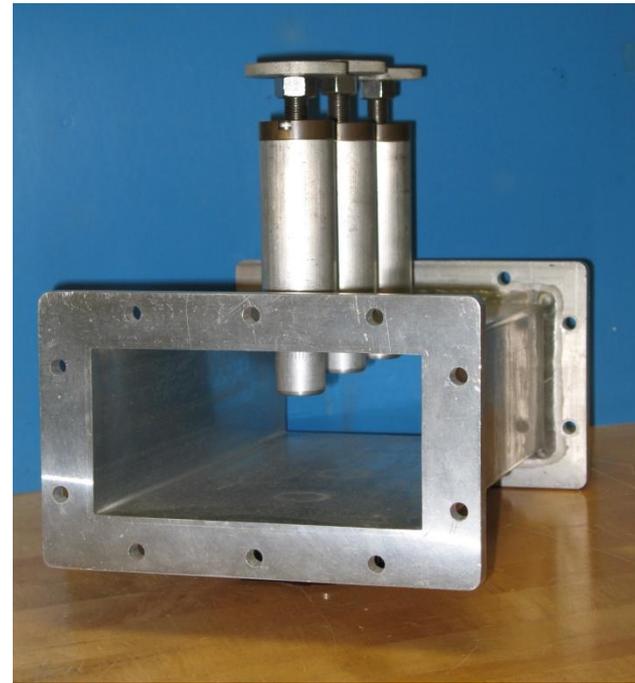
- Commercial APEX piezo driver amplifier.
- 0 to 150 V at 50 mA.
- Bandwidth (FS): 10 Hz
- Packaging: 3U Eurocard x8



**APEX
Amplifier**

Waveguide Stub Tuning

- Commonly used to adjust coupling
- Could also be used to compensate for detuning
- Issues:
 - Part of the waveguide becomes part of the resonant system
 - Speed for dynamic control of microphonics
 - Good for tuning Q_L higher ...not so much lower



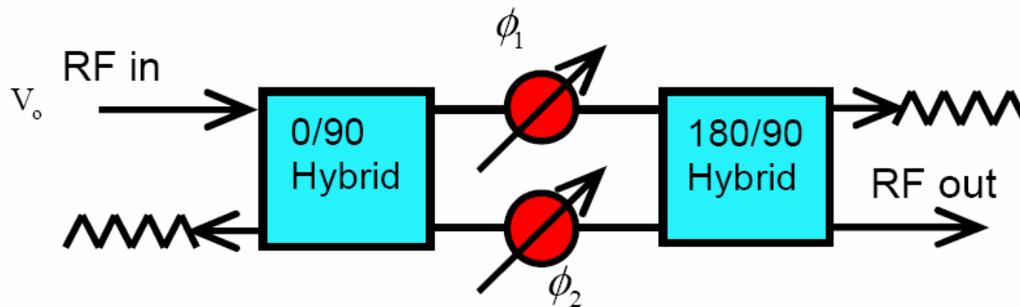
JLAB uses a three stub tuner to adjust cavity Q_{ext}

References: 19

High Power Modulators

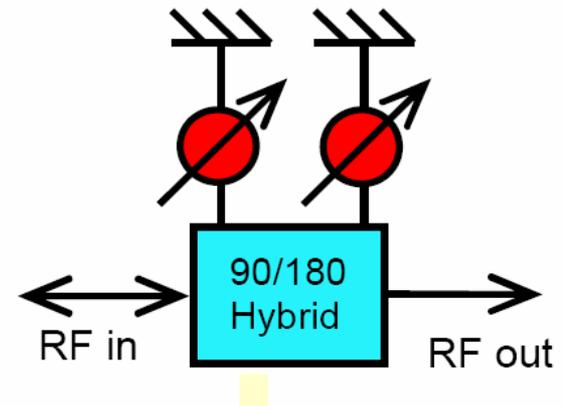
- Solution for linacs powering multiple cavities from one power source, especially cw designs.
- **Need to compare cost and complexity between RF power source and power supply for ferrites**

Vector Modulator



$$V_{out} = jV_{inc} \cos(\phi_1 - \phi_2) e^{j(\phi_1 + \phi_2)}$$

Phase Shifter



References: 19

Summary

Challenges - Thoughts

- Design LLRF with respect to what is needed by the accelerator and the cryomodule.

Example: A proton/ion LLRF control system doesn't need light source precision!

- Field control requirements beyond 0.05° and $.01\%$ control are pushing the limits of the receiver hardware.

Trade offs between process gain (increased latency) and loop gain need to be made to reach beyond these values.

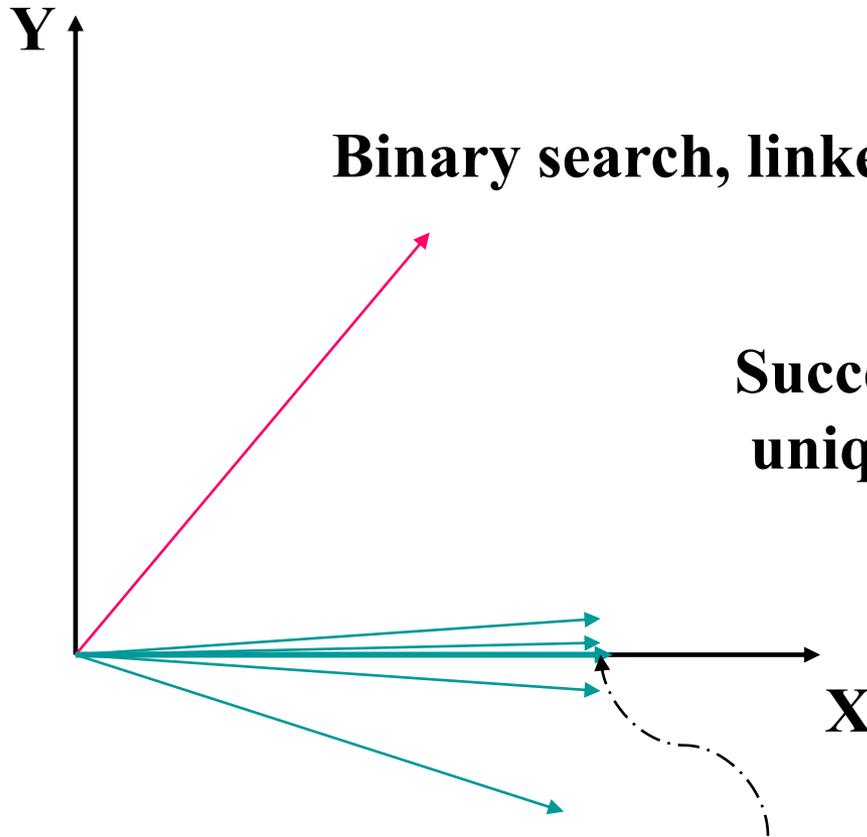
- A lot of room to grow in fast mechanical control. Could have big pay off in reduced amplifier power

Good Luck!

Acknowledgement - References

- [1] L. Merminga, J. Delayen, "On the optimization of Qext under heavy beam loading and in the presence of microphonics", CEBAF-TN-96-022
- [2] M. Liepe, et al, Proceedings of the 2005 Particle Accelerator Conference, Knoxville, USA
- [3] K. Davis, T. Powers, "Microphonics Evaluation for the CEBAF Energy Upgrade", JLAB-TN-05-040
- [4] D. Schulze, "Ponderomotive Stability of RF Resonators and Resonator Control Systems", KFK 1493, Karlsruhe (1971); ANL Translation ANL-TRANS-944 (1972).
- [5] J. R. Delayen, "Phase and Amplitude Stabilization of Superconducting Resonators", Ph. D. Thesis, California Institute of Technology, 1978.
- [6] T. Plawski, private conversations, plawski@jlab.org
- [7] A.S. Hofler et al, Proceedings of the 2004 Linear Accelerator Conference, Lubeck, Germany
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CORDIC Functionally.....



Binary search, linked to $\text{sgn}(Y)$

$$d_i = \begin{cases} +1, & \text{if } y_i < 0 \\ -1, & \text{if } y_i \geq 0 \end{cases}$$

Successively add angles to produce unique angle vector

$$\phi = \sum_i d_i \cdot \arctan(2^{-i})$$

$$z_{i+1} = z_i - d_i \cdot \arctan(2^{-i})$$

Resultant lies on X
(real) axis
with a residual gain of 1.6

Transmitter/Up Conversion

