

# LUMINOSITY ISSUES FOR THE $e^-e^-$ OPTION OF THE TESLA LINEAR COLLIDER

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## Abstract

The future TESLA linear  $e^+e^-$  collider can also be used for  $e^-e^-$  collisions at a center of mass energy of 500 GeV and beyond. A critical issue for the physics potential of this option is the achievable luminosity. For  $e^+e^-$  collisions, the pinch effect enhances the luminosity, while due to the repelling forces for  $e^-e^-$  collisions, the luminosity is significantly reduced and is more sensitive to beam separations. This report discusses an intra-train feedback to stabilize the luminosity and possibilities to partly overcome the luminosity degradation of the  $e^-e^-$  mode.

## 1 INTRODUCTION

The rich physics potential of the TESLA linear collider designed for  $e^+e^-$  collisions at  $\sqrt{s} = 500$  GeV can be extended to explore  $e^-e^-$  interactions. It has been shown,

Table 1: TESLA 500 parameter list.

Parameter	Symbol	Ref. Design
Center of mass energy	$E_{cm}$	500 GeV
Bunch charge	$N$	$2 \cdot 10^{10}$ 1/e
Bunches per train	$n_b$	2820
Bunch spacing	$t_b$	337 ns
Repetition rate	$f_{rep}$	5 Hz
Bunch length	$\sigma_z$	0.3 mm
Horiz. beam size at IP	$\sigma_x$	553 nm
Vert. beam size at IP	$\sigma_y$	5 nm
Vert. divergence at IP	$\sigma_{y'}$	$12.3 \mu\text{rad}$
Vert. emittance (norm.)	$\epsilon_y$	$0.03 \cdot 10^{-6}$ m
Energy loss (beamstr.)	$\delta_b$	3.3 %
Vertical Disruption	$D_y$	25
Luminosity $e^+e^-$ mode	$\mathcal{L}^{+-}$	$3.4 \cdot 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
Luminosity $e^-e^-$ mode	$\mathcal{L}^{--}$	$0.47 \cdot 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

that both spent  $e^-e^-$  beams can be safely extracted from the interaction point (IP) without changing the present  $e^+e^-$  layout [1]. In this report we discuss the achievable  $e^-e^-$  luminosity and its stabilization, for the given  $e^+e^-$  parameter set listed in Tab. 1. At TESLA, the luminosity is highly sensitive to beam separations  $\Delta y$  at the IP. This is due to the large disruption  $D_y$  of 25, a value beyond the accepted limit for the onset of the kink instability. In the case of  $e^+e^-$  collisions, the attracting forces ‘pinch’ the bunches enhancing the luminosity. However, for equally charged beams ( $e^-e^-$ ), the electrons repel and disrupt the beam: the luminosity is significantly reduced and is more sensitive to beam separations (see Fig. 1). A crossing an-

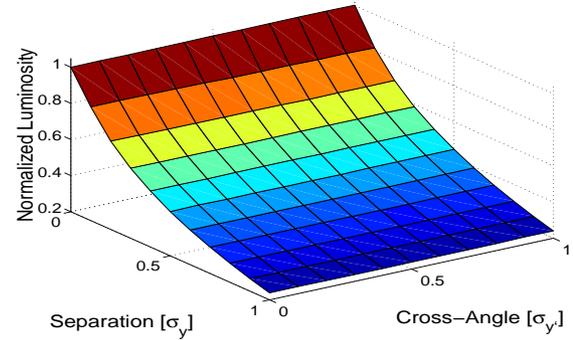


Figure 1: Normalized  $e^-e^-$  luminosity versus vertical beam separation and crossing angle (normalized to  $\sigma_y = 5$  nm and to  $\sigma_{y'} = 12 \mu\text{rad}$  resp.). Machine parameters used are listed in Tab. 1. Luminosity calculations performed with GUINEA PIG [3].

gle does not degrade the luminosity as it is in the  $e^+e^-$  case [2]. Sources of beam separations are Lorentz force detuning, wakefield effects, quadrupole vibrations. A major concern is the displacement of the final doublets transferred one-to-one into a beam position offset at the IP, since a vertical separation between two bunches of  $0.1 \sigma_y = 5 \text{ \AA}$  decreases the luminosity per bunch crossing by 17 % and of  $1 \sigma_y = 5$  nm even by 76 % (see Fig. 1). From bunch train to bunch train (5 Hz) the beam separation is expected to be as large as  $35 \sigma_y$  [4]. Obviously, a system is required to steer the beams back to collision already within a few bunches of the train. A correction is feasible on a bunch-to-bunch basis, due to the large bunch spacing of 337 ns for TESLA.

## 2 FEEDBACK SYSTEM

The schematic layout of the intra-train feedback system for the  $e^-e^-$  interactions is shown in Fig. 2. The aim is to design a fast and efficient system working at the bunch repetition frequency of 3.1 MHz.

A vertical separation  $\Delta y$  between two electron bunches at the IP becomes detectable even in a range well below the vertical beam size  $\sigma_y$  of 5 nm due to the strong beam-beam deflection (Fig. 3). The strong angular kick experienced by the bunches results in a measurable position shift at the final doublets located 3 m downstreams to the IP. Two beam position monitors (BPM) measure the positions of the incoming and spent bunch. A digital controller derives an estimate of the beam separation by means of a linear beam-beam deflection model. The correction is determined with a proportional-integral (PI) control algorithm. The P-

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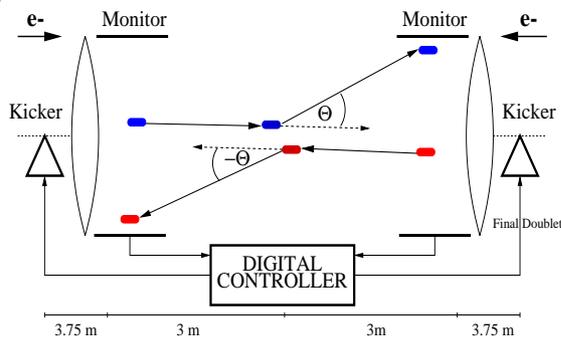


Figure 2: Layout of the  $e^+e^-$  feedback system at the IP.

controller ensures a fast response to incoming disturbances. The I-controller is needed to remove the steady state error in the case of a step disturbance. Correction kicks are applied to subsequent bunches with a latency of two bunches by two kickers. Commonly available kickers have a sufficiently short field rise time of 25 ns and produce a kick of up to  $0.12 \mu\text{rad}$  at a beam energy of 250 GeV [5]. Two kickers are sufficient to cover a control range of  $\pm 100 \sigma_y$ . A time varying controller with two models of the beam-

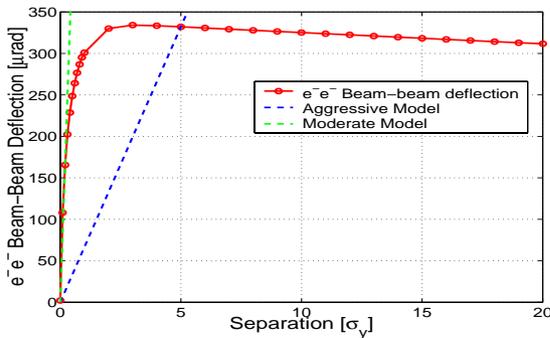


Figure 3: Beam-beam deflection as a function of beam separation for  $e^+e^-$  interaction in TESLA and the two linear models used by the time varying controller.

beam deflection is used as indicated in Fig. 3. The *aggressive* model, is given by  $\Phi = 64.4/\mu\text{rad} \cdot \Delta y/\sigma_y$ . It provides a fast response to large separations, but poor correction accuracy. Only 35 bunches are required to correct an bunch train separation of  $50 \sigma_y$ . However, the collisions of the following bunches can barely be kept within  $1.6 \sigma_y$ , since the model strongly overestimates small bunch separations. The correction accuracy is improved to a fraction of the vertical beam size, by switching to a *moderate* model:  $\Phi = 1000/\mu\text{rad} \cdot \Delta y/\sigma_y$ . This model is characterized by a negligible noise amplification and a slow step response. The correction accuracy achieved is  $0.02 \sigma_y$ .

Figure 4 shows the simulated feedback response to a stationary bunch train separation of  $50 \sigma_y$ . The simulation includes the following effects: residual beam position offsets due to higher-order mode effects in the linac; finite BPM resolution and analog-to-digital signal quantization

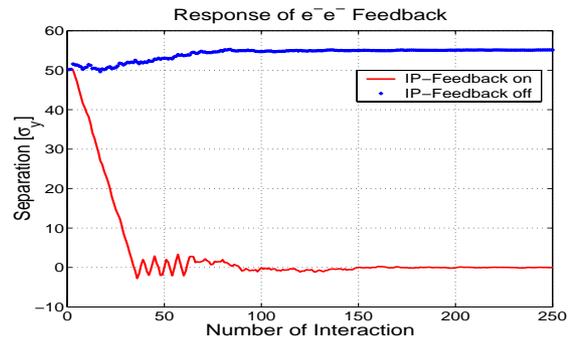


Figure 4: Response of time-varying controller. The aggressive model brings the beams within 35 bunches (interactions) into collision, the switch to the moderate model insures a high correction accuracy for the subsequent bunches.

of  $5 \mu\text{m}$ ; kicker field imperfections of 0.1 %; random variation of the beam-beam deflection by 10 % to include fluctuations, e.g. in bunch charge, bunch length, or beam size.

As a conclusion, the feedback system is capable of limiting the luminosity loss to 6% in case of a  $50 \sigma_y$  beam separation.

### 3 LUMINOSITY IMPROVEMENTS

The enhancement or reduction of the luminosity is described by the disruption (de-)enhancement factor  $H_D$ . It is 2 for  $e^+e^-$  with TESLA parameters, but only 0.34 for  $e^-e^-$ . There is no complete analytical expression for  $H_D$  (see e.g. [6]), therefore, a simulation of the beam-beam interaction is used to evaluate the luminosity [3].

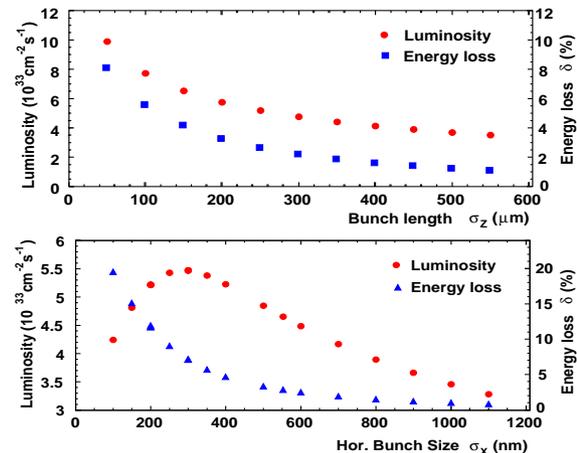


Figure 5: Luminosity as a function of the bunch length and horizontal bunch size for  $e^+e^-$  collisions using the TESLA parameters of Tab. 1. Simulations are performed with GUINEA PIG.[3]

In the case of flat beams ( $\sigma_y/\sigma_x \ll 1$ ) the luminosity for

Table 2: Luminosity and average beam energy loss due to beamstrahlung for  $e^-e^-$  collisions for different bunch lengths and horizontal beam sizes. The TESLA parameters in Tab. 1 have been used.

$\sigma_z$ ( $\mu\text{m}$ )	$\sigma_x$ (nm)	$\delta_b$ (%)	$\mathcal{L}$ ( $10^{33} \text{ cm}^{-2} \text{ s}^{-1}$ )
400	553	1.6	4.1
300	553	2.2	4.7
200	553	3.3	5.7
100	553	5.6	7.7
50	553	8.1	9.9
300	300	7.2	5.5
300	100	19.6	4.2

$E_{\text{cm}} = 500 \text{ GeV}$  can be expressed as

$$\mathcal{L} = 7.2 \cdot 10^{29} \text{ cm}^{-2} \text{ s}^{-1} \frac{\eta P_{\text{AC}} [\text{MW}]}{\sqrt{\epsilon_y [\text{m}]}} \sqrt{\delta_b} H_D, \quad (1)$$

with  $P_{\text{AC}}$  the overall AC power consumption,  $\eta$  the AC-to-beam power efficiency,  $\epsilon_y$  the normalized vertical emittance, and  $\delta_b$  the average energy loss due to beamstrahlung. Since it is trivial to increase the luminosity by increasing the power consumption, we limit the  $P_{\text{AC}}$  to 100 MW. TESLA has a favourable AC to beam power efficiency of  $\eta = 22\%$  due to the use of superconducting accelerating structures. The  $e^-e^-$  luminosity calculated for TESLA parameters is  $4.7 \cdot 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$  ( $H_D = 0.34$ ) compared to  $34 \cdot 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$  ( $H_D = 2.0$ ) for the  $e^+e^-$  case (see Tab. 1). Since the vertical emittance of  $3 \cdot 10^{-8} \text{ m}$  is already very demanding, the only reasonable way to improve the luminosity is to allow a larger average beam energy loss  $\delta_b$ . In addition, one can expect a larger  $H_D$  for smaller vertical disruption  $D_y$ . Looking at the analytical expressions for  $\delta_b$  and  $D_y$ ,

$$\delta_b = 0.86 \frac{r_e^3 \gamma N^2}{\sigma_x^2 \sigma_z}, \quad \text{and} \quad D_y = \frac{2N r_e}{\gamma \sigma_x \sigma_y} \sigma_z, \quad (2)$$

the bunch length  $\sigma_z$  is the only adequate parameter to tune. (Here,  $N$  denotes the bunch charge,  $r_e$  the classical electron radius,  $\gamma$  the Lorentz factor, and  $\sigma_{x,y}$  the horizontal and vertical beam sizes respectively.) A reevaluation of the bunch compressor scheme for TESLA showed, that a compression to  $\sigma_z = 300 \mu\text{m}$  is indeed possible, which yields to an increase in luminosity and to a better performance of the feedback system as for the previous case of  $\sigma_z = 400 \mu\text{m}$  [7].

The luminosity is enlarged by a reduction of the bunch length, with the expense of an increased beamstrahlung induced energy loss  $\delta_b$  (see Fig. 5 and Tab. 2). A moderate increase of  $\delta_b$  seems to be tolerable for physics, since the luminosity spectrum of  $e^-e^-$  collisions is narrower than the spectrum for  $e^+e^-$  (Fig. 6). A bunch length reduction does not spoil the spectrum significantly.

An additional gain in luminosity is achieved by reducing the horizontal spot size down to  $300 \mu\text{m}$  (see Fig. 5 and

Tab. 2). In this case, the luminosity increases by 14 %, but  $\delta_b$  is enlarged significantly to 7.2 %.

## 4 CONCLUSION

The large disruption parameter for the high luminosity TESLA parameters demands a sophisticated beam stabilization system for beam collisions. The intra-train feedback system is capable of limiting the maximum luminosity loss to 6 % in the case of an initial beam separation of  $50 \sigma_y$ . The  $e^-e^-$  luminosity for the TESLA  $e^+e^-$  parameters is by a factor of 7.6 smaller than the  $e^+e^-$  luminosity due to the anti-pinch effect. A further increase of luminosity is only possible by reducing the bunch length and the horizontal spot size with the expense of a larger energy loss.

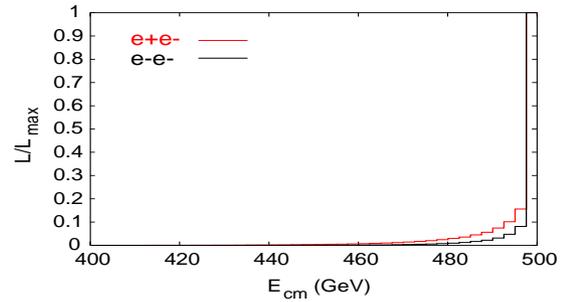


Figure 6: Normalized luminosity spectrum for  $e^-e^-$  collisions compared to  $e^+e^-$ . TESLA high luminosity parameters from Tab. 1 are used.

## 5 ACKNOWLEDGMENT

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