STUDY OF STOCHASTIC COOLING AT ACR

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Abstract

We studied availability of a stochastic cooling for a cooling accumulation of RI beam in the ACR. In the ACR fast cooling is essential for an RI beam with large emittance and momentum spread because the RI has an intrinsic life time. In general the stochastic cooling is useful to obtain a fast cooling time in a region where emittance and momentum spread are large. From calculations under some conditions, we could get a very short cooling time (< 0.1 s) and confirm that the stochastic cooling is available with cooling of the RI beam in the ACR.

1 INTRODUCTION

One of purposes for the accumulator cooler ring [1] (ACR) at the MUSES project[2] is cooling of an ion beam including a radio-isotope (RI) beam produced by projectile-fragmentation in the Big-RIPS. Due to production mechanism the RI beam has large emittance (ε_x ; horizontal, ε_y ; vertical) and momentum spread ($\Delta p/p$). Moreover, due to multi-turn injection, ε_x of the beam injected into the ACR is very large. In the ACR initial values of ε_x, ε_y and $\Delta p/p$ are 125 π mm*mrad, 10 π mm*mrad and ±0.15 %. Requirement of cooling in the ACR is to have a very fast cooling time for the RI beam with large ε_x, ε_y and $\Delta p/p$ because the RI has an intrinsic life time.

Stochastic cooling[3] is one of useful methods for cooling of the ion beam. In particular, a fast cooling time is obtained by the stochastic cooling in a region of large ε_x, ε_y and $\Delta p/p$ as the initial beam in the ACR. On the other hand, in a region of small ε_x, ε_y and $\Delta p/p$, the cooling time of the stochastic cooling is longer than that of electron cooling. In this way the stochastic cooling will be used as pre-cooling that reduces initial large ε_x, ε_y and $\Delta p/p$ to about 0.1 times. After pre-cooling the electron cooling will be used to make final small values of ε_x, ε_y and $\Delta p/p$.

We calculated transverse and longitudinal cooling times of the stochastic cooling in several conditions. In this paper we will mention calculations and results. Availability of stochastic cooling will be also discussed.

2 TRANSVERSAL COOLING

The transversal cooling time of the stochastic cooling is given by[4],

$$\frac{1}{\tau} = -\frac{W}{N}\left\{ -g_1\sin\Delta\mu + \frac{1}{2}g_1^2 F \right\} \qquad (1)$$

where

W ; band-width of a feed back system
N ; total number of particles
$\Delta\mu$; phase advance between pickup and kicker
g_1 ; $g\sqrt{\beta_p\beta_k}$, g is gain of a feed back system and β_p and β_k is β values of pickup and kicker
F ; M+U, M is mixing factor and U is noise factor given, (noise of system) divided (beam noise per Schottky band)

Using parameters of a beam and a system, g is given

$$g = \frac{(qe)^2 f_0 Z_p f_k N G_{amp}}{\beta E W} \qquad (2)$$

where

q ; charge of beam
f_0 ; revolution frequency
Z_p ; coupling impedance between beam and pickup
f_k ; efficiency of kicker
G_{amp} ; gain of amplifier
β ; Lorentz parameter of beam
E ; energy of beam

From (1) and (2), we can get an optimum gain (G_{amp_opt}) to get a minimum cooling time as shown in (3)

$$G_{amp\_opt} = \frac{\sin\Delta\mu}{(M+U)}\frac{W}{N}\frac{\beta E}{(qe)^2 f_0 Z_p f_k} \qquad (3)$$

Output power of an amplifier for G_{amp_opt} is given

$$P = k(T + T_n)\left(1 + \frac{1}{U}\right)W G_{amp\_opt}^2 \qquad (4)$$

where, k is Boatsmann constant and T and T_n are temperatures of the amplifier and a pickup system including a pre-amplifier. Using eq. (4) we calculated P's for $^{11}Be^{4+}$ (400 MeV/u), $^{39}Ca^{20+}$ (300 MeV/u), $^{132}Sn^{50+}$ (200 MeV/u) and $^{200}Pb^{80+}$ (100 MeV/u) with $\Delta p/p = \pm0.15$ % and $\varepsilon_x = 100$ π mm*mrad. In the calculation we assumed
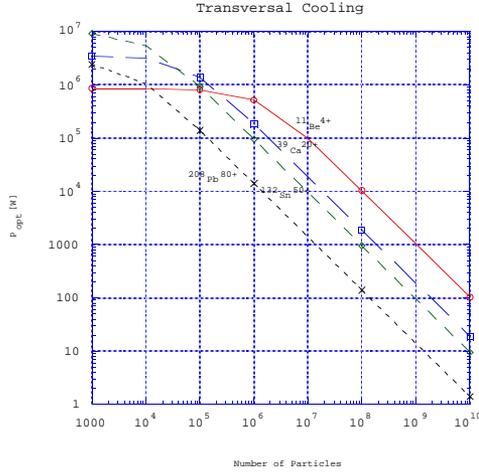
Fig. 1 Optimum output power of an amplifier

T_n=200 K, W=2 GHz and Z_p=100 Ω. The other parameters of the ACR are shown in ref [1]. Results are shown in Fig. 1 in term of dependence of number of particles. As shown in Fig. 1, the obtained P's are very large especially for small number of particles as RI beam. From the result, we studied the cooling times under limited power of the amplifier (P_{lim}).

In a power-limited system the cooling time is given

$$\frac{1}{\tau_{lim}} = \frac{1}{\tau_{opt}} \frac{G_{amp\_lim}}{G_{amp\_opt}} \left(2 - \frac{G_{amp\_lim}}{G_{amp\_opt}}\right) \qquad (5)$$

where, subscript "lim" means the limited system and t_{opt} is a minimum cooling time obtained from eqs. (1), (2) and (3). In eq. (5) G_{opt_lim} has a value obtained under the condition $P=P_{lim}$ in eq. (4).
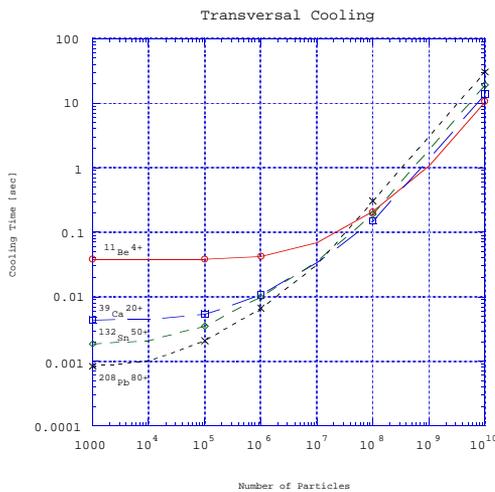

Fig. 2 Transversal cooling time

Under the assumption of P_{lim} = 1 kW we calculated the cooling times for several beams with several number of particles. In Fig. 2 the results are shown. As shown in Fig. 2, the obtained cooling time is less than 0.1 s for particle number of $10^3 \sim 10^6$ as RI beam. In particular for beam with a high charge the cooling time is very fast.

3   LONGITUDINAL COOLING

We also studied longitudinal cooling time by a notch filter method[5] which cooling is done in a region of dispersion free. Similar to the transversal cooling, the cooling time of the longitudinal cooling   is limited by output power of the amplifier.   In the power-limited system the cooling time is given by the same equation as eq. (5). For the longitudinal cooling t_{opt} is given

$$\tau_{opt} = \left(\frac{N}{W}\right)\left(1 + \frac{W^2}{12W_c^2}\right)(1+U(0)) \qquad (6)$$

where W_c is average frequency of the amplifier and U(0) is give by

$$U(0) = \left(1 + \frac{W^2}{12W_c^2}\right)^{-1}\left(\frac{f_0}{\kappa W_c}\frac{E_0}{\Delta E_0}\right)^2 U_p \qquad (7)$$

where, ΔE is spread of energy and

$$\kappa = \left|\frac{1}{\gamma} - \frac{1}{\gamma_t}\right|\left(\frac{\gamma}{1+\gamma}\right)$$

where g is Lorentz parameter and γ_t is transition γ. G_{amp_opt} and P for the longitudinal cooling are given by

$$_{amp\_opt} = \frac{1}{2}\frac{A}{(qe)^2}\frac{1}{NW_c}\left(1+\frac{W}{12W_c}\right)^{-1}\frac{E_0}{|\kappa Z_p f_k|}\frac{1}{1+U(0)} \qquad (8)$$

$$P = \frac{1}{3}k(T+T_n)WG_{amp\_opt}^2\left(1+\frac{1}{U(0)}\right) \qquad (9)$$

where A is a mass number of the beam.   The other parameters which don't explain in eqs. (6) ~ (9) are the same as the transverse cooling.

We calculated particle number dependence of the cooling time. Kinds of particles and conditions are the same as those used in the transversal cooling. In Fig. 3 results are shown. Excluding Be, the obtained cooling times are less than 0.1 s for number of particles < 10^6. In particular the cooling time of particle with high charge is very fast. These tendencies are similar to the transversal cooling.

We also calculated cooling times for several values of temperatures of a pickup system (T_n) and coupling impedances (Z_p).   Fig. 4 and 5 show T_n and Z_p dependences. In both calculations we assumed number of particles 10^5.   For calculation of T_n dependence we assumed Z_p = 200 Ω and for that of Z_p dependence, T_n =
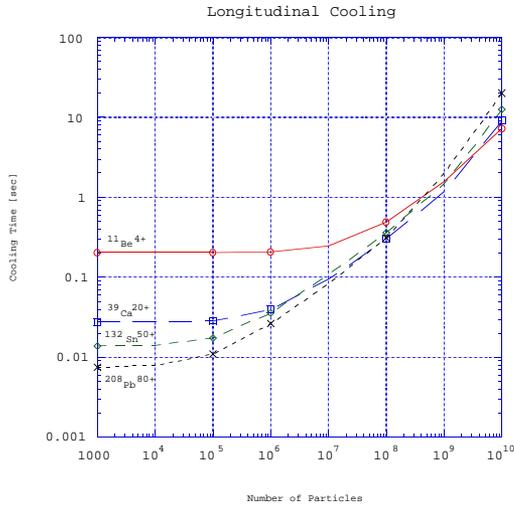
Longitudinal Cooling

Fig. 3 Longitudinal cooling time.

200 K. As shown in Fig. 4 the T_n dependence is weak. Cooling times of highly charged beams are shorter than 0.01 s even in 200 K. It is due to good signal-to-noise ratio because voltage induced by the highly charged beam at the pickup is much larger than that by noise. As shown in Fig. 5 Z_p dependence is strong especially for region below 50 Ω. To obtain t < 0.1 s Z_p is required Z_p > 200 Ω.

Longitudinal Cooling
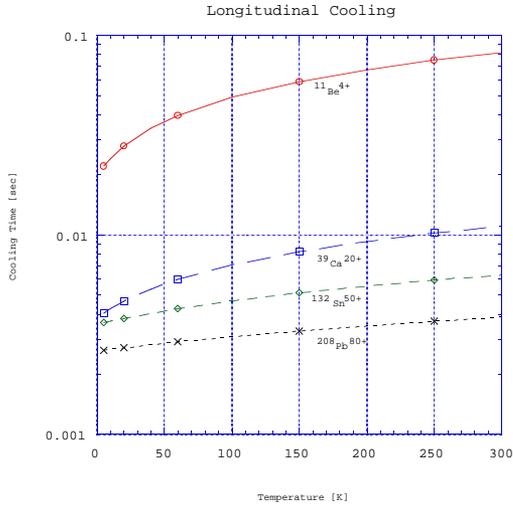

Fig. 4 T_n dependence of cooling time. Here number of particles is 10^5.

4 Availability of stochastic cooling

From calculations in sec. 2 and 3 we obtained fast cooling times in almost whole region. This indicates that the stochastic cooling is available with the cooling of the RI beam in the ACR.
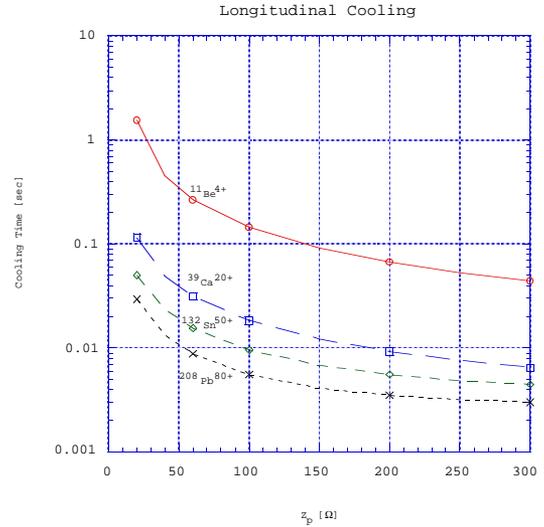
Longitudinal Cooling

Fig. 5 Z_p dependence of cooling time. Here number of particles is 10^5.

One of the important things to construct a system of the stochastic cooling in the ACR is to make a pickup system with large coupling impedance. The large coupling impedance is also important to reduce a needed output gain of the amplifier because a voltage from pickup itself is large.

Another important thing is to cool down pickup and pre-amplifier system. From result of T_n dependence the system is cooled down below 200 K. Considering noise of pre-amplifier, the system may be cooled down by liquid nitrogen.

On the base of the calculation we are designing the pickup system with high coupling impedance and will measure it using electron beam.

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