



# Low Emittance Muon Colliders

Rolland Johnson,  
Muons, Inc.

In February, Muons, Inc. and the Fermilab TD sponsored the second annual low-emittance muon collider workshop at Fermilab (~85 participants). Muon Colliders are looking more feasible. Synergies with the ILC and Neutrino Factories can be important.

Papers can be found at <http://www.muonsinc.com>  
workshop link is at <http://www.muonsinc.com/mcwfeb07/> also see  
<http://www.muonsinc.com/mcwfeb06/presentations/LEMCWorkshop.pdf>

# Related Muon Work at PAC07

- MOPAS012 - **Magnets for the MANX Cooling Demonstration Experiment**  
V. Kashikhin...
- MOPAN117 - **Magnet Systems for Helical Muon Cooling Channels**  
S. A. Kahn...
- MOPAN118 - **High Field HTS Solenoid for Muon Cooling**  
S. A. Kahn...
- WEPMS071 - **Evidence for Fowler-Nordheim behavior in RF Breakdown**  
M. BastaniNejad...
- THPAN103 - **G4BeamLine Program for Matter-dominated Beam Lines**  
T. J. Roberts...
- THPMN096 - **Stopping Muons Beams**  
M. A. C. Cummings...
- THPMN110 - **Design of the MANX 6D Demonstration Experiment**  
K. Yonehara...
- THPMN094 - **Simulations of Parametric-resonance Ionization Cooling**  
D. Newsham...
- THMN095 - **Muon Bunch Coalescing**  
R. P. Johnson...
- THPMN106 - **Use of Harmonic RF Cavities in Muon Capture for NFs or MCs**  
D. Neuffer...



# New inventions, new possibilities

- Muon beams can be cooled to a few mm-mr (normalized)
  - allows HF RF (implies Muon machines and ILC synergy)
- Muon recirculation in ILC cavities => high energy, lower cost
  - Each cavity used 10 times for both muon charges
  - Potential 20x efficiency wrt ILC approach offset by
    - Muon cooling
    - Recirculating arcs
    - Muon decay implications for detectors, magnets, and radiation
- A low-emittance high-luminosity collider
  - high luminosity with fewer muons
  - First LEMC goal:  $E_{\text{com}}=5 \text{ TeV}$ ,  $\langle L \rangle = 10^{35}$
  - Revised goal is 1.5 TeV to complement the LHC
- Many new ideas in the last 5 years. A new ball game!
  - (many new ideas have been developed with DOE SBIR-STTR funding)



# Muons, Inc. SBIR/STTR Collaboration:

- Fermilab:
  - Victor Yarba, Ivan Gonin, Timer Khabiboulline, Gennady Romanov, Daniele Turrioni
  - Dave Neuffer
  - Mike Lamm
  - MCTF-APC, V. Shiltsev, S. Geer, A. Jansson, M. Hu, D. Bromelsiek, Y. Alexehin,...
  - Chuck Ankenbrandt, Katsuya Yonehara
  - Milorad Popovic, Al Moretti, Jim Griffin
  - Sasha Zlobin, Emanuela Barzi, Vadim Kashikhin, Vladimir Kashikhin
  
- IIT:
  - Dan Kaplan, Linda Spentzouris
  
- JLab:
  - Yaroslav Derbenev, Alex Bogacz, Kevin Beard, Yu-Chiu Chao, Robert Rimmer
  
- Muons, Inc.:
  - Rolland Johnson, Bob Abrams, Mohammad Alsharo'a, Mary Anne Cummings, Stephen Kahn, Sergey Korenev, Moyses Kuchnir, David Newsham, Tom Roberts, Richard Sah, Cary Yoshikawa (underlined are new-3 are from Lucent)

First named are subgrant PI.



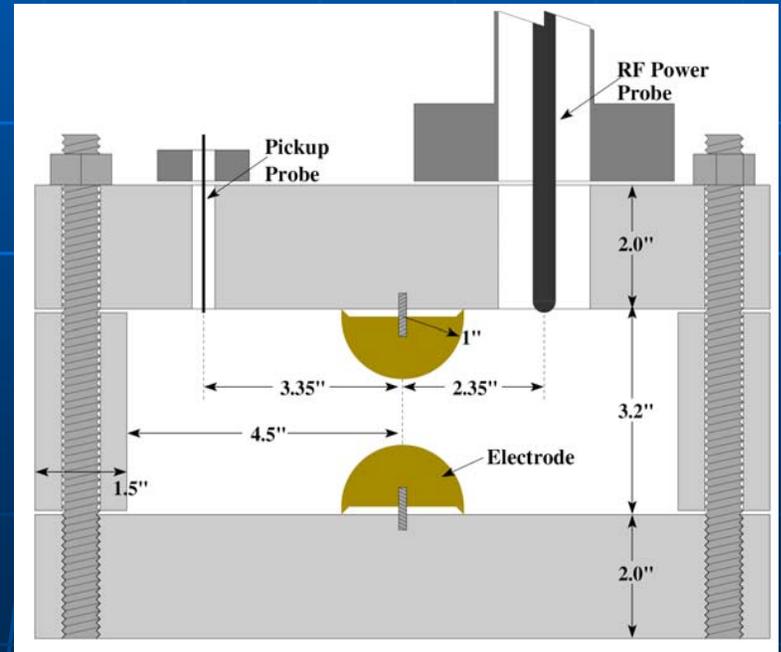
# Recent Inventions and Developments

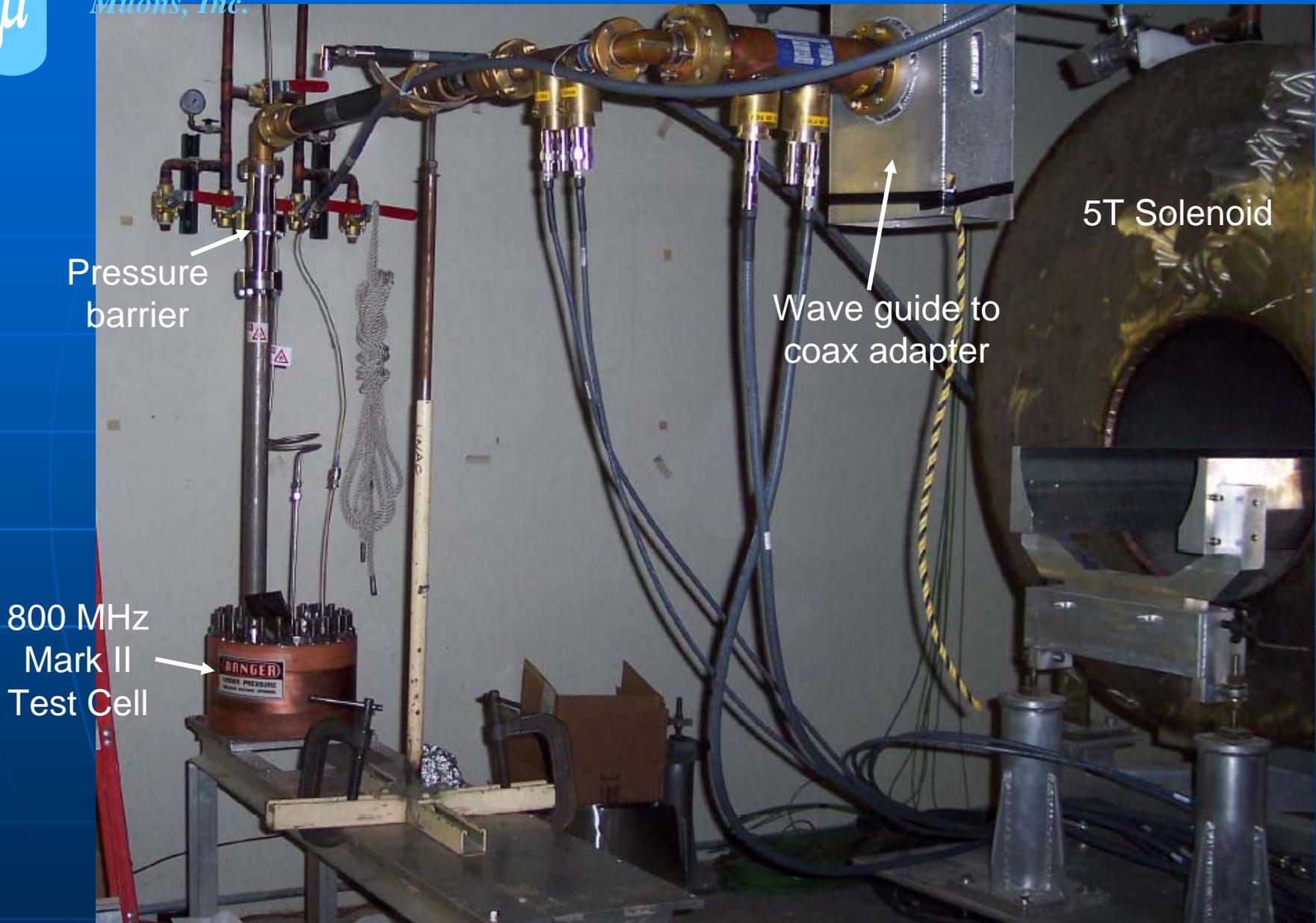
- **New Ionization Cooling Techniques**
  - Emittance exchange with continuous absorber for longitudinal cooling
  - Helical Cooling Channel (HCC)
    - Effective 6D cooling (simulations: cooling factor >50,000 in 160 m)
  - Momentum-dependent Helical Cooling Channel
    - 6D Precooling device (e.g. stopping muon beams)
    - 6D cooling demonstration experiment (MANX)
  - Ionization cooling using a parametric resonance
- **Methods to manipulate phase space partitions**
  - Reverse emittance exchange using absorbers
  - Bunch coalescing (neutrino factory and muon collider share injector)
- **Technology for better cooling**
  - Pressurized RF cavities
    - simultaneous energy absorption and acceleration and
    - phase rotation, bunching, cooling to increase initial muon capture
    - Higher Gradient in magnetic fields than in vacuum cavities
  - High Temperature Superconductor for very high field magnets
    - Faster cooling, smaller equilibrium emittance



# Pressurized High Gradient RF Cavities

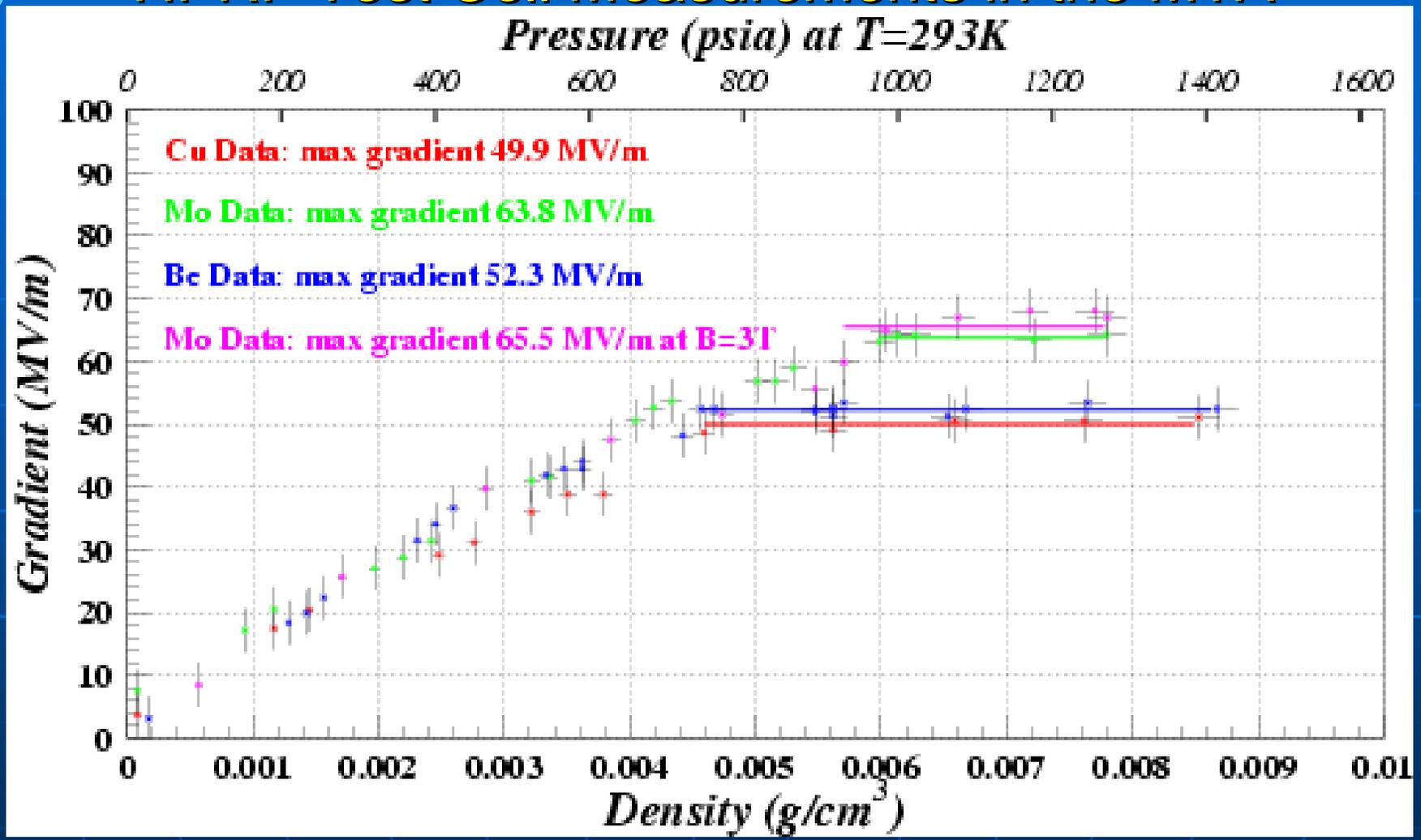
- Copper plated, stainless-steel, 800 MHz test cell with GH2 to 1600 psi and 77 K in Lab G, MTA
- Paschen curve verified
- Maximum gradient limited by breakdown of metal
  - fast conditioning seen, no limitation by external magnetic field!
- Cu and Be have same breakdown limits ( $\sim 50$  MV/m), Mo  $\sim 60$ , W  $\sim 70$







# HPRF Test Cell Measurements in the MTA

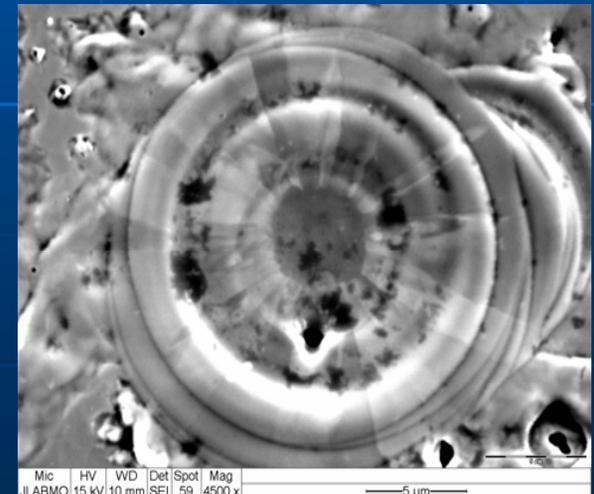
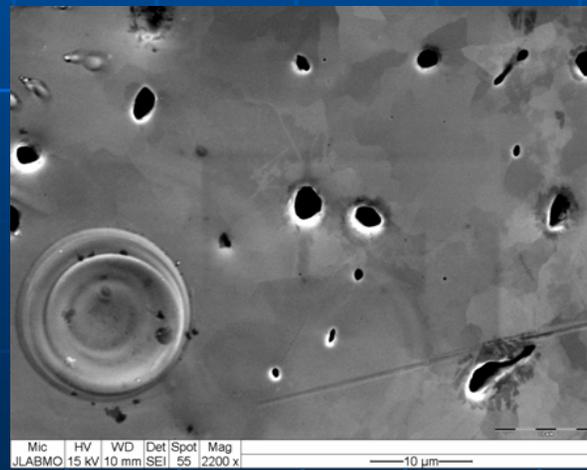
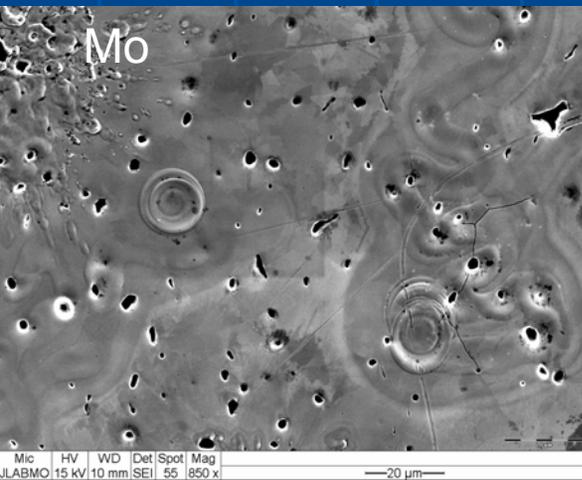
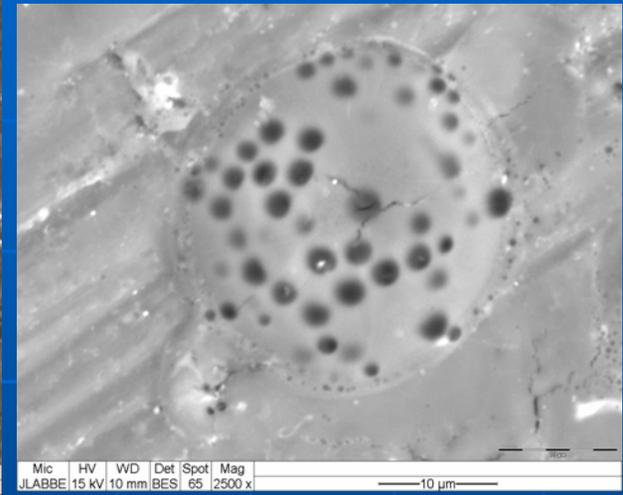
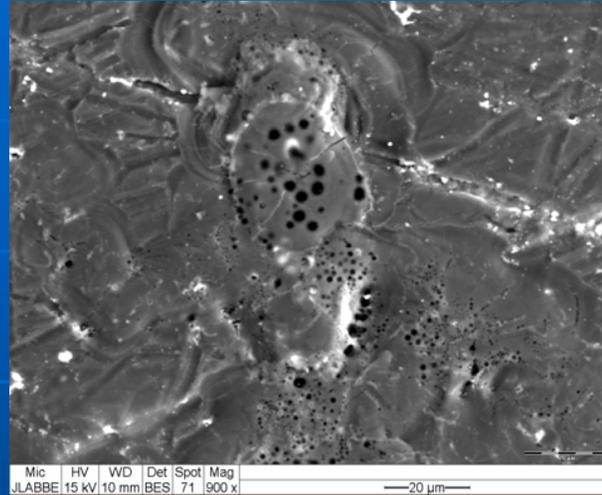
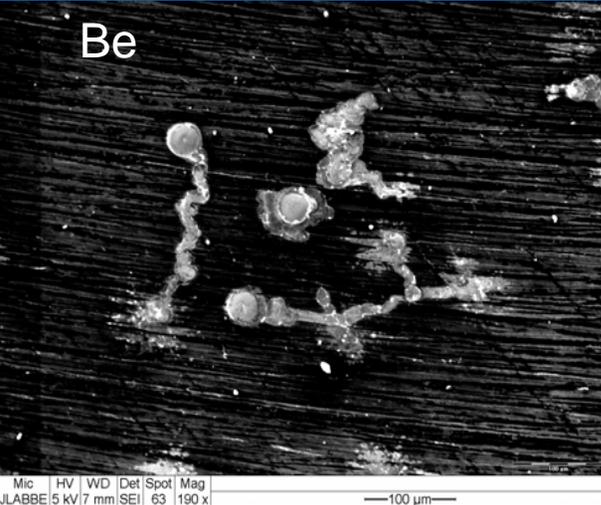


Results show no B dependence, much different metallic breakdown than for vacuum cavities. **Need beam tests to prove HPRF works.**



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# Understanding RF Breakdown in High Pressure Cavities: Scanning Electron Microscope Pictures of HP Electrodes



RoI - 6/26/2007

PAC07

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See WEPMS071 - Evidence for Fowler-Nordheim behavior in RF Breakdown



# Technology Development in Technical Division

HTS at LH2 shown, in LHe much better

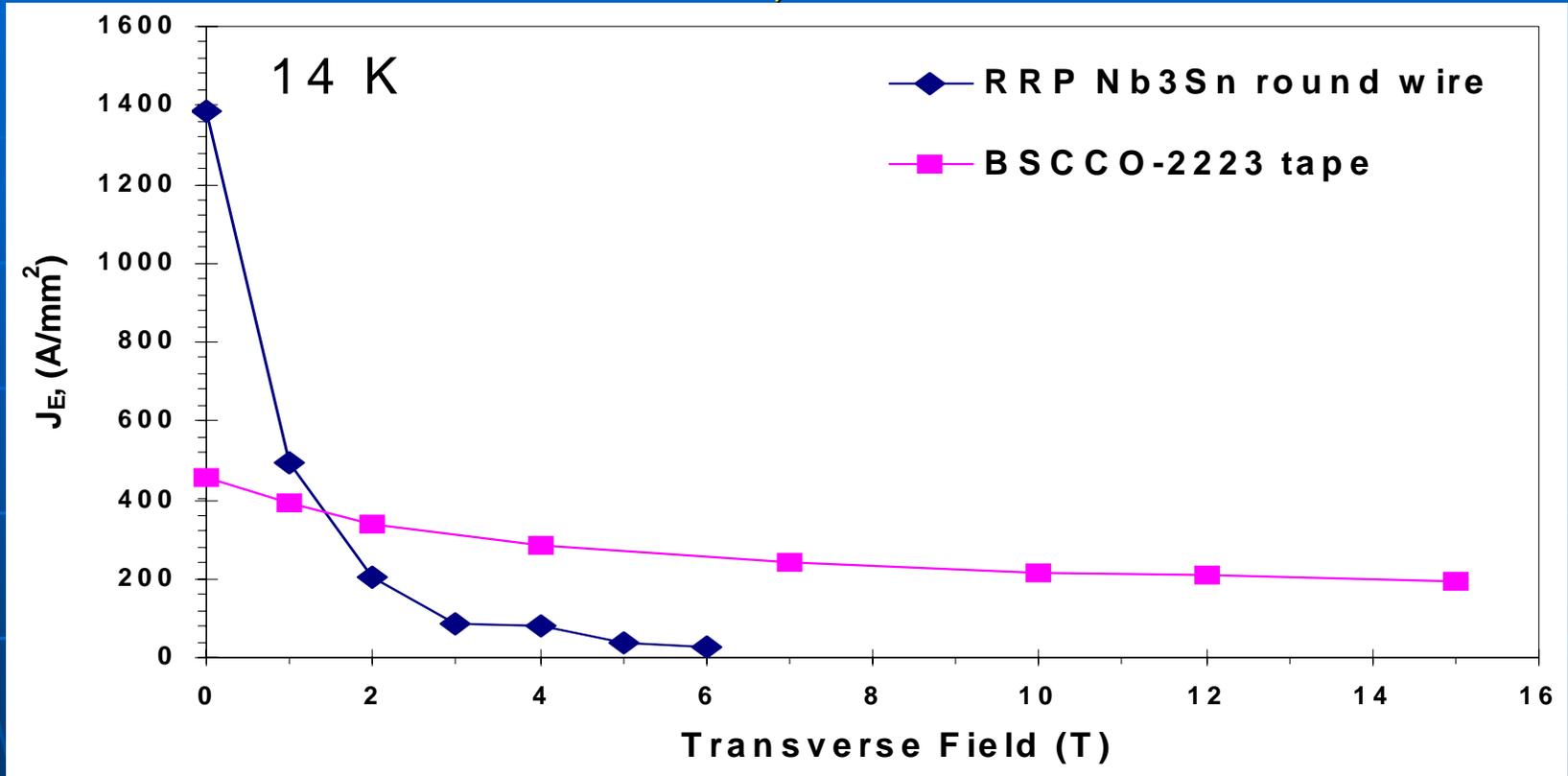


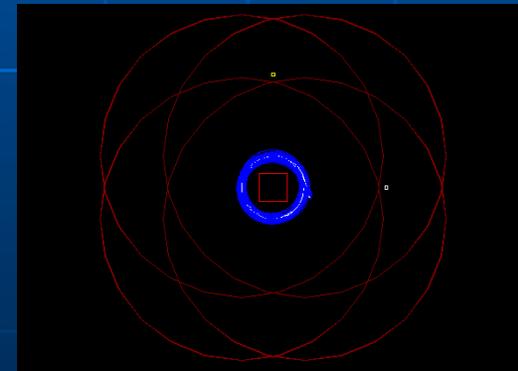
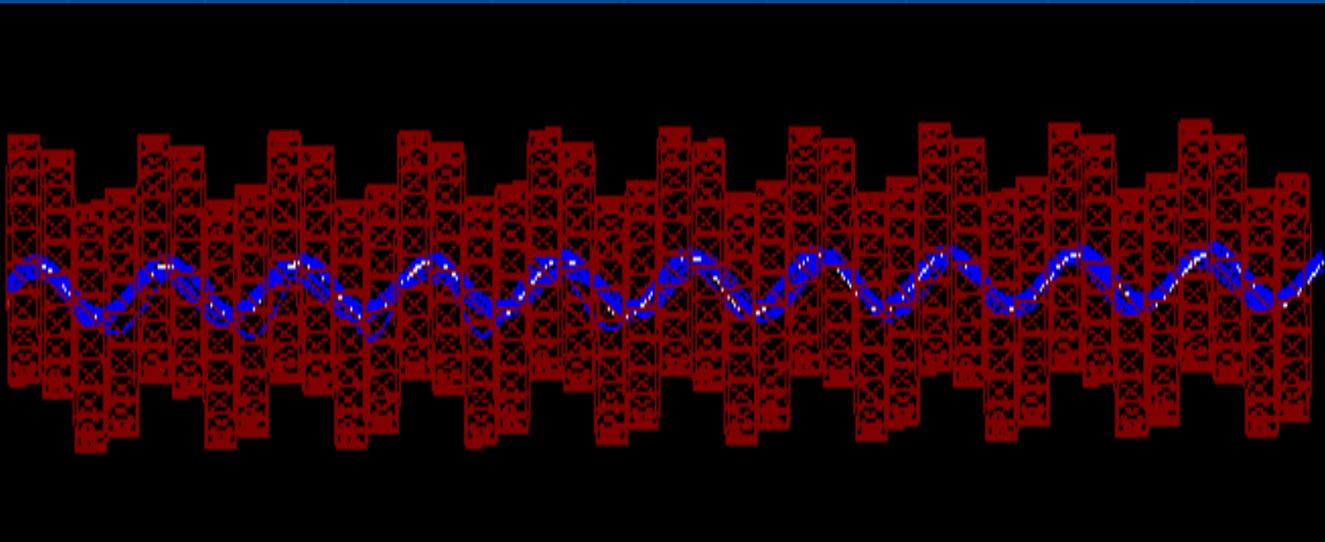
Fig. 9. Comparison of the engineering critical current density,  $J_E$ , at 14 K as a function of magnetic field between BSCCO-2223 tape and RRP Nb<sub>3</sub>Sn round wire.

Emanuela Barzi et al., Novel Muon Cooling Channels Using Hydrogen Refrigeration and HT Superconductor, PAC05

# 6-Dimensional Cooling in a Continuous Absorber

see Derbenev, Yonehara, Johnson

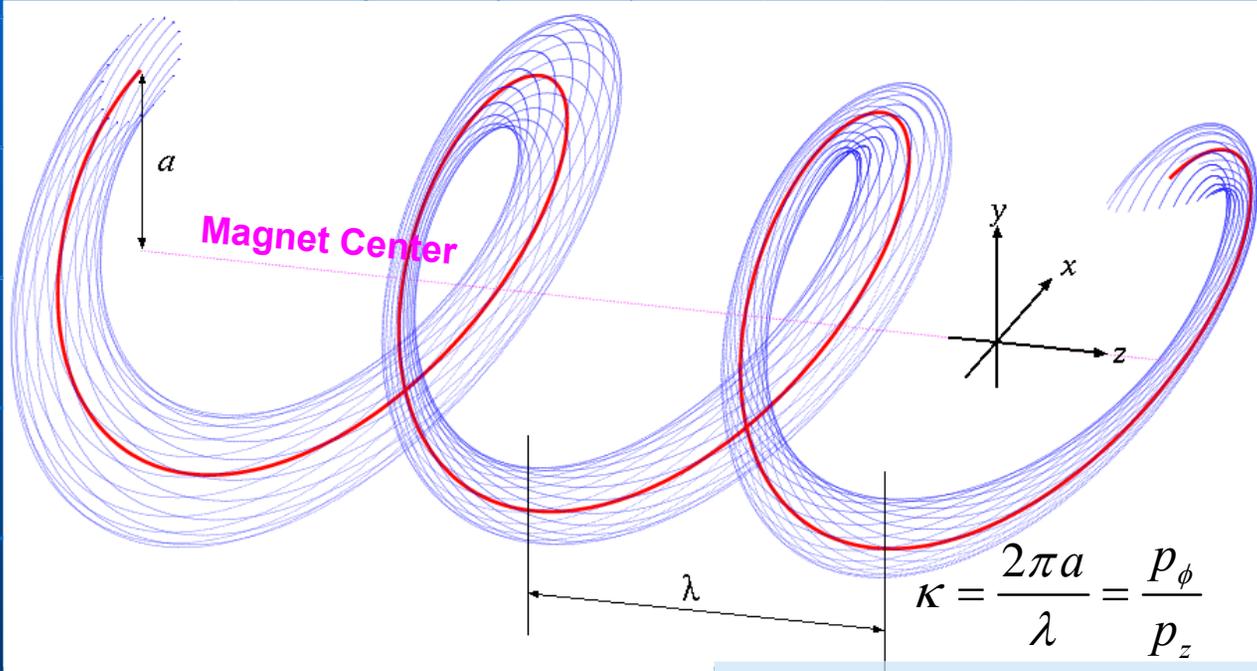
- Helical cooling channel (HCC)
  - Continuous absorber for emittance exchange
  - Solenoidal, transverse helical dipole and quadrupole fields
  - Helical dipoles known from Siberian Snakes
  - z-independent Hamiltonian
  - Derbenev & Johnson, Theory of HCC, April/05 PRST-AB





# Particle Motion in Helical Magnet

Combined function magnet (invisible in this picture)  
Solenoid + Helical dipole + Helical Quadrupole



**Red: Reference orbit**

**Blue: Beam envelope**

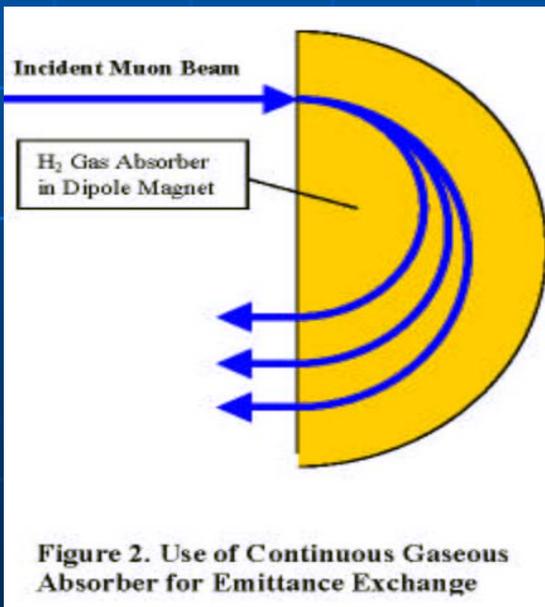
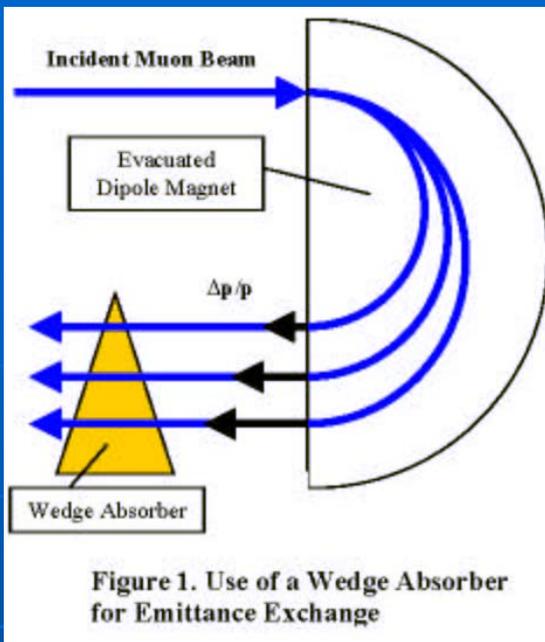
Dispersive component makes longer path length for higher momentum particle and shorter path length for lower momentum particle.

$$f_{\uparrow} \propto b_{\phi} \cdot p_z \quad \text{Repulsive force}$$

$$f_{\downarrow} \propto -b_z \cdot p_{\phi} \quad \text{Attractive force}$$

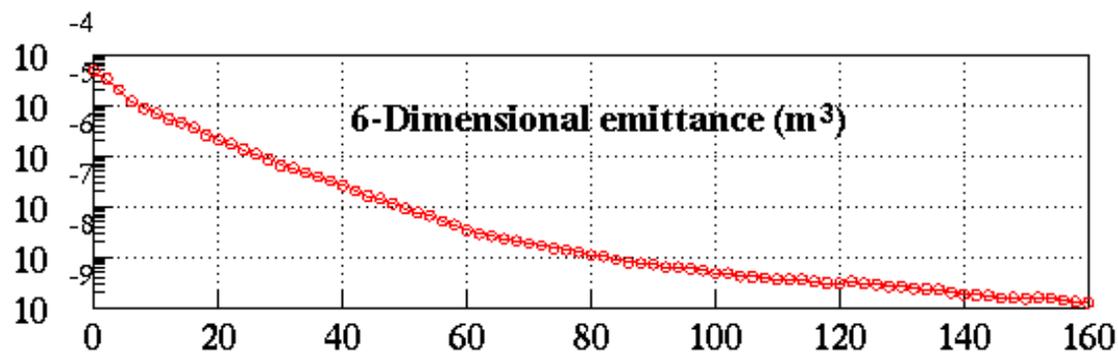
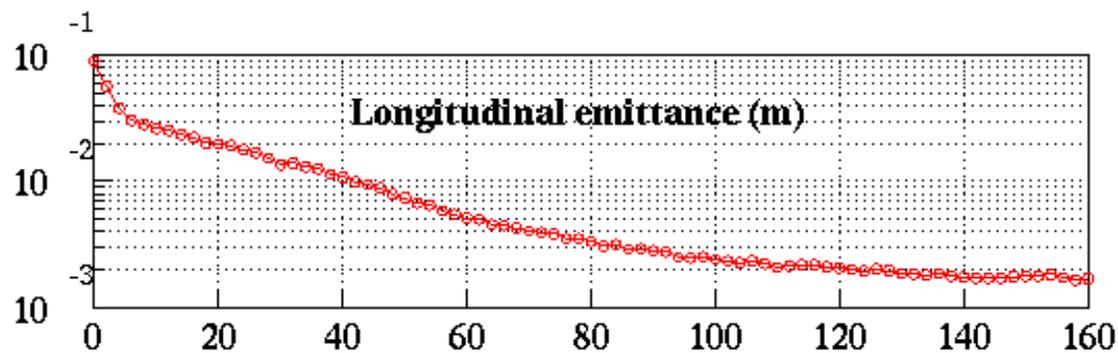
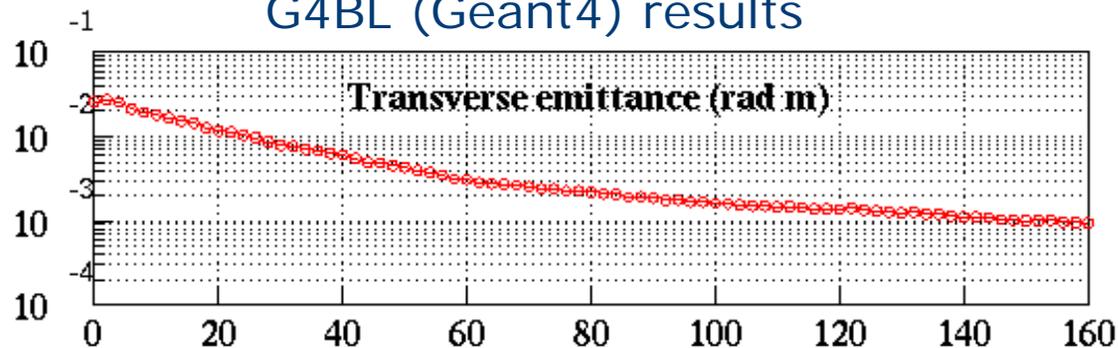
$$f_{\text{central}} = \frac{e}{m} (b_{\phi} \cdot p_z - b_z \cdot p_{\phi})$$

**terms have opposite sign**



$\lambda = 1.0 \text{ m}$     $\lambda = 0.8 \text{ m}$     $\lambda = 0.6 \text{ m}$     $\lambda = 0.4 \text{ m}$

### G4BL (Geant4) results



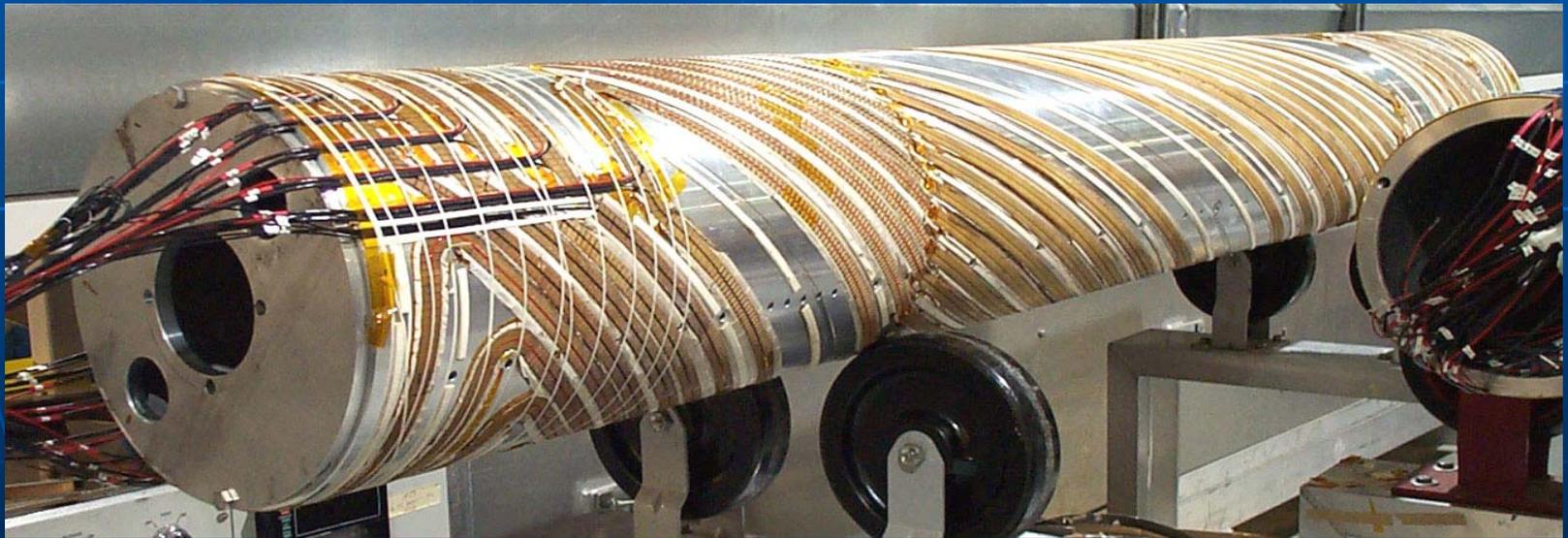
**6D Cooling factor ~ 50,000**   **z (m)**



# Hydrogen Cryostat for Muon Beam Cooling

Technology for HCC components:

HTS (nice BSSCO data from TD Ph I), Helical magnet design,  
low T Be or Cu coated RF cavities, windows, heat transport, refrigerant  
Cryostat for the 6DMANX cooling demonstration experiment (proposal 7)



BNL Helical Dipole magnet for AGS spin control

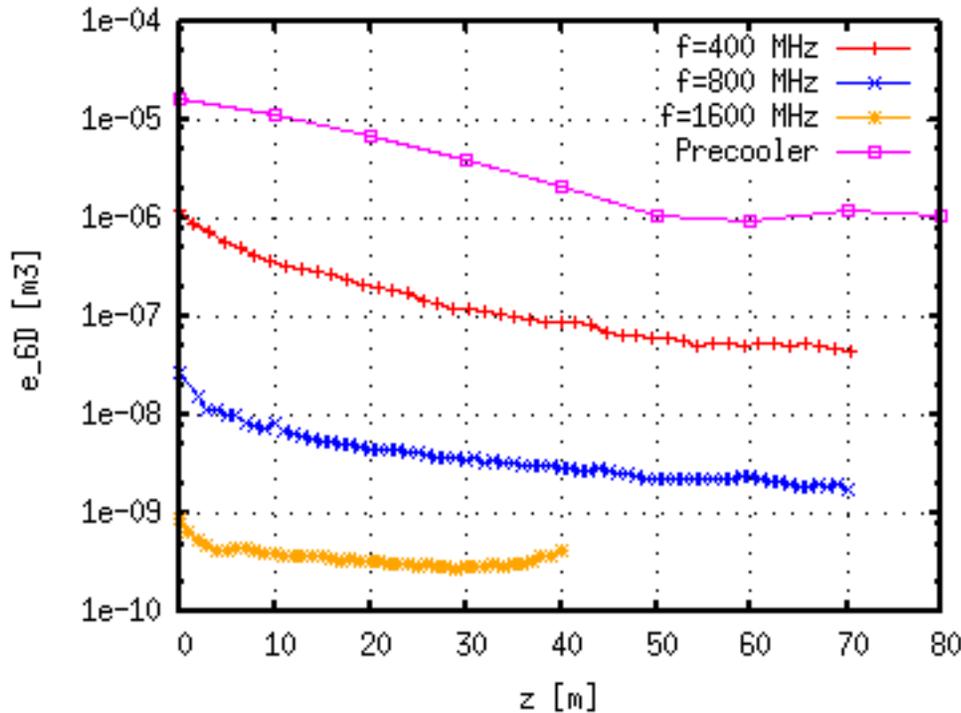




# Precooler + HCCs



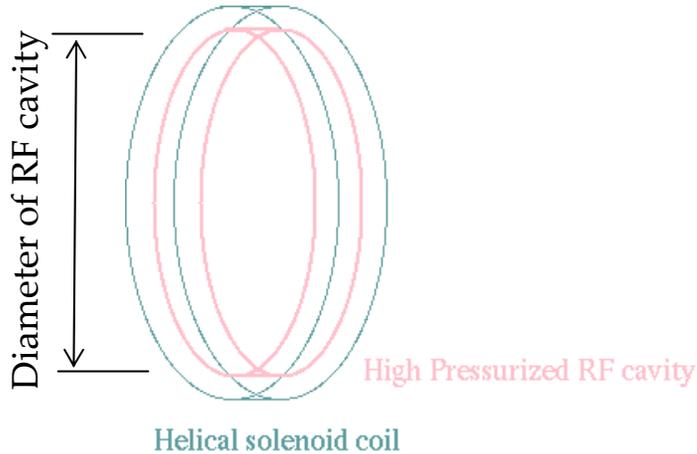
*Solenoid + High Pressurized RF*



- The acceptance is sufficiently big.
- Transverse emittance can be smaller than longitudinal emittance.
- Emittance grows in the longitudinal direction.



# Incorporate RF cavity in helical solenoid coil

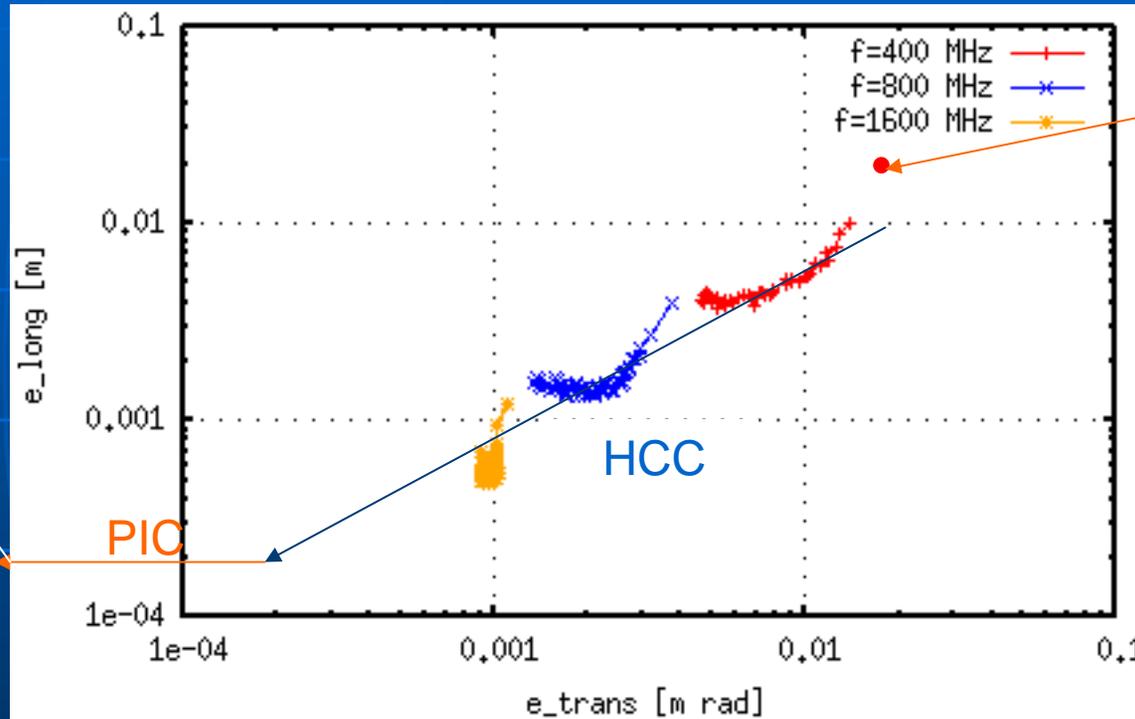


- Use a pillbox cavity (but no window this time).
- RF frequency is determined by the size of helical solenoid coil.
  - Diameter of 400 MHz cavity = 50 cm
  - Diameter of 800 MHz cavity = 25 cm
  - Diameter of 1600 MHz cavity = 12.5 cm
- The pressure of gaseous hydrogen is 200 atm to adjust the RF field gradient to be a practical value.
  - The field gradient can be increased if the breakdown would be well suppressed by the high pressurized hydrogen gas.

<i>parameter</i>	$\lambda$	$\kappa$	$B_z$	$bd$	$bq$	$bs$	$f$	<i>Inner d of coil</i>	<i>Maximum b</i>	$E$	<i>rf phase</i>
<i>s</i>	$m$		$T$	$T$	$T/m$	$T/m^2$	$GHz$	$cm$	<i>Snake   Slinky</i>	$MV/m$	<i>degree</i>
<i>1st HCC</i>	1.6	1.0	-4.3	1.0	-0.2	0.5	0.4	50.0	12.0   6.0	16.0	140.0
<i>2nd HCC</i>	1.0	1.0	-6.8	1.5	-0.3	1.4	0.8	25.0	17.0   8.0	16.0	140.0
<i>3rd HCC</i>	0.5	1.0	-13.6	3.1	-0.6	3.8	1.6	12.5	34.0   17.0	16.0	140.0



# Yonehara HCC Fernow-Neuffer Plot



Initial point

REMEX  
+coalescing

PIC

HCC

Cooling required for 5 TeV COM,  $10^{35}$  Luminosity Collider, shown later.  
 Need to also look at losses from muon decay to get power on target.  
 Higher magnetic fields from HTS can get required HCC performance.



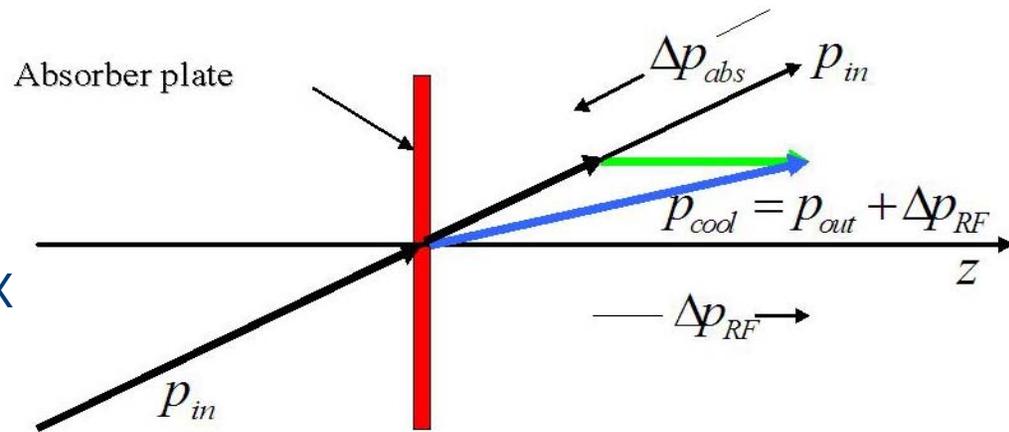
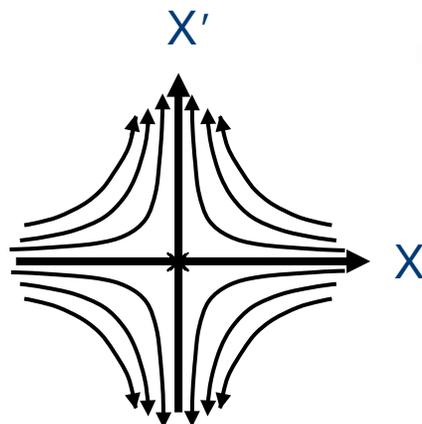
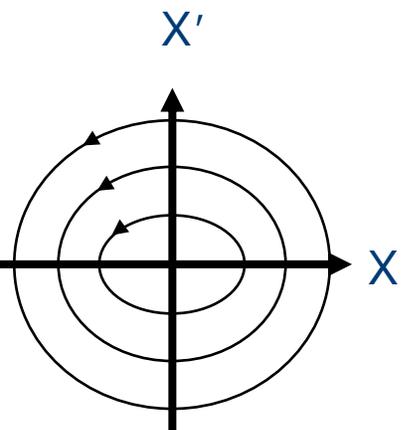
# Parametric-resonance Ionization Cooling

Excite 1/2 integer parametric resonance (in Linac or ring)

- Like vertical rigid pendulum or 1/2-integer extraction
- Elliptical phase space motion becomes hyperbolic
- Use  $xx' = \text{const}$  to reduce  $x$ , increase  $x'$
- Use IC to reduce  $x'$

Detuning issues being addressed (chromatic and spherical aberrations, space-charge tune spread). Simulations underway. New progress by Derbenev.

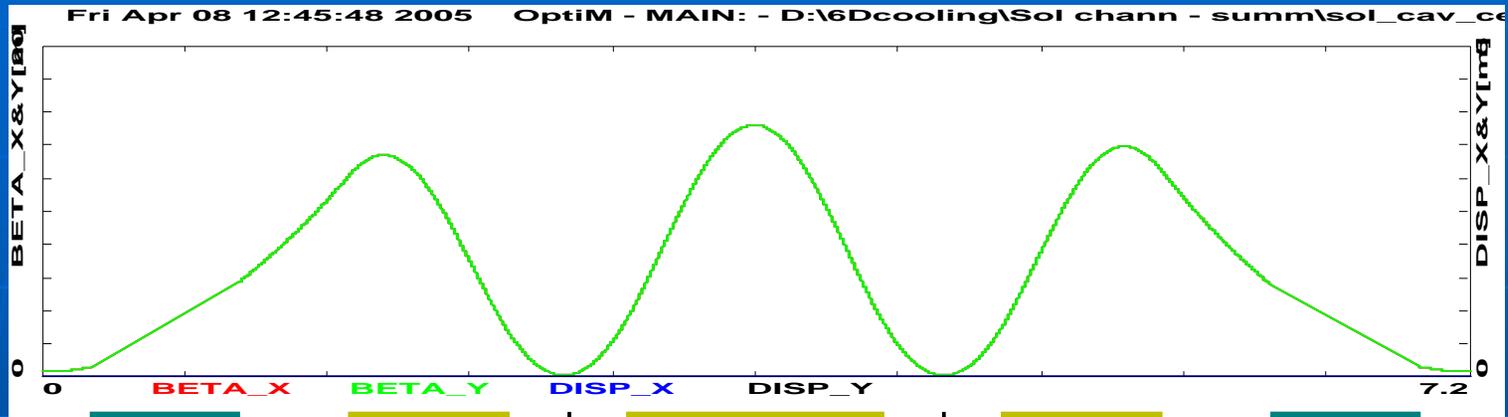
See Sah, Newsham, Bogacz



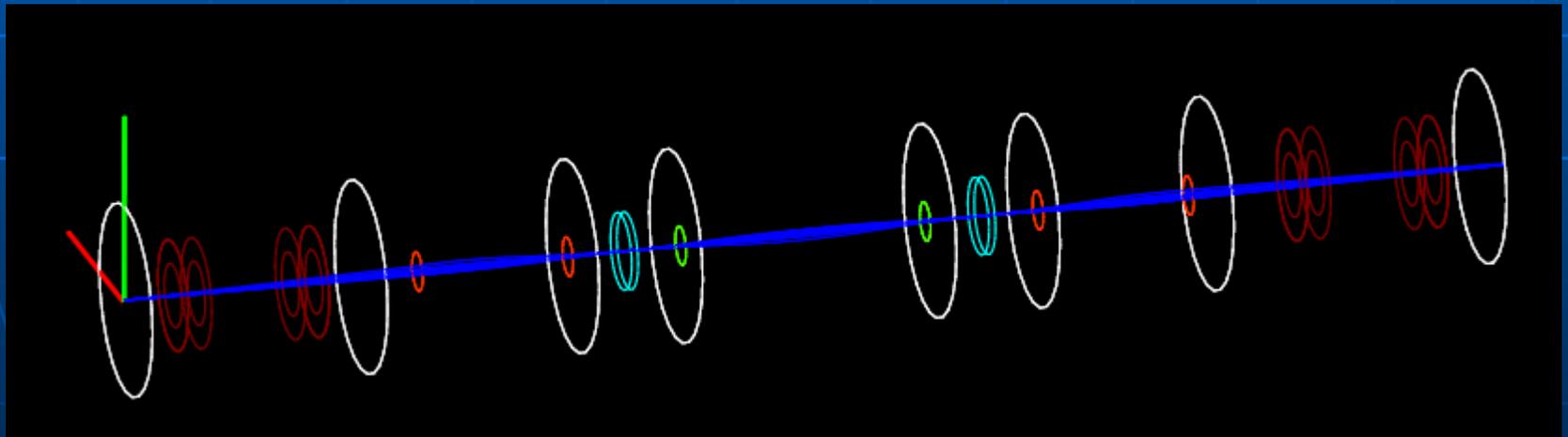


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Example of triplet solenoid cell on  $\frac{1}{2}$  integer resonance with RF cavities to generate synchrotron motion for chromatic aberration compensation.



P-dependent focal length is compensated by using rf to modulate  $p$ .

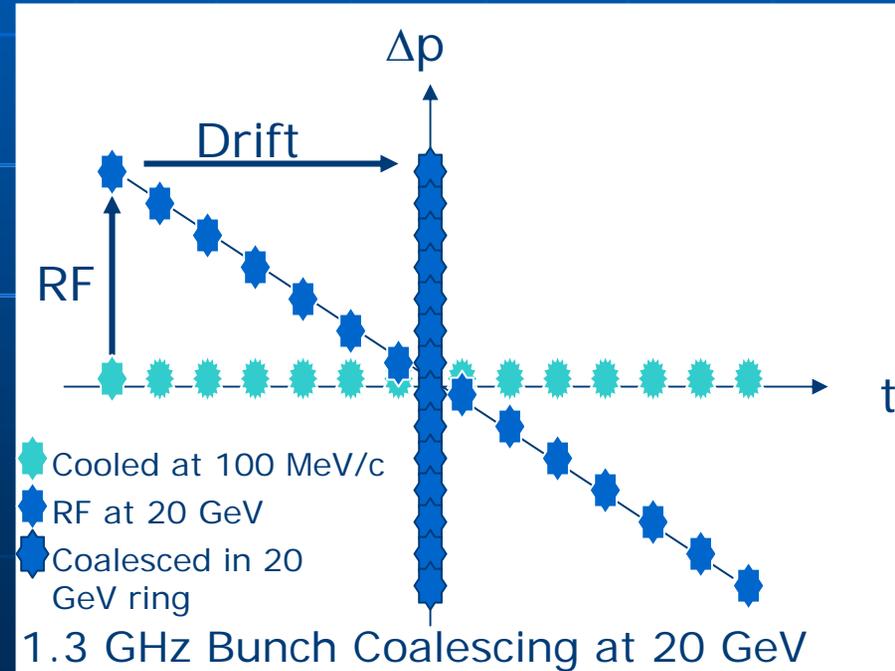
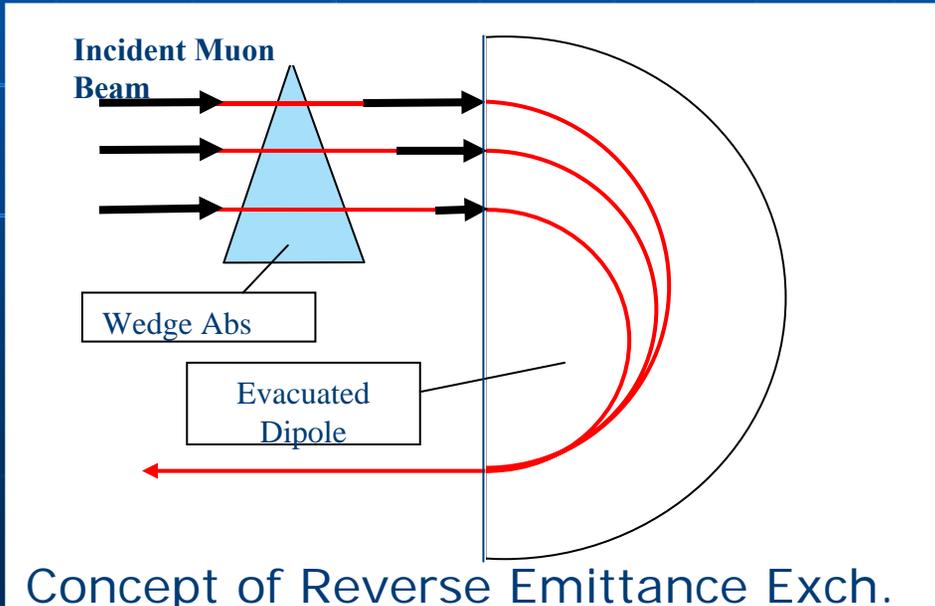


OptiM (Valeri Lebedev) above and G4beamline (Tom Roberts) below.

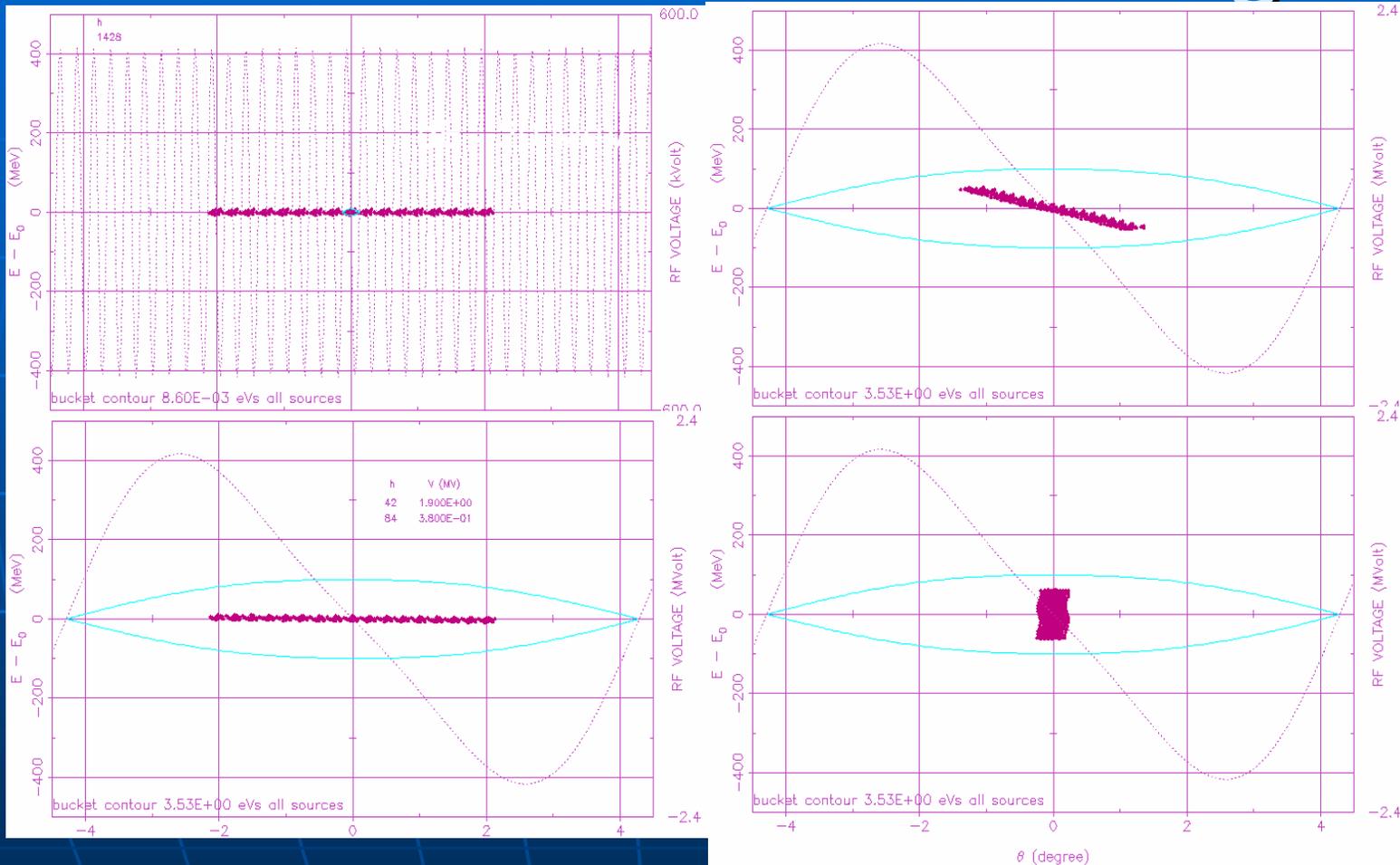


# Reverse Emittance Exchange, Coalescing

- $p(\text{cooling}) = 100 \text{ MeV}/c$ ,  $p(\text{colliding}) = 2.5 \text{ TeV}/c \Rightarrow$  room in  $\Delta p/p$  space
- Shrink the transverse dimensions of a muon beam to increase the luminosity of a muon collider using wedge absorbers
- 20 GeV Bunch coalescing in a ring a new idea for ph II
- Neutrino factory and muon collider now have a common path



# Bhat et al. Coalescing



20 GeV muons in a 100 m diameter ring



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# 6DMANX demonstration experiment

Muon Collider And Neutrino Factory eXperiment

See Kashikhin, Yonehara

- To Demonstrate
  - Longitudinal cooling
  - 6D cooling in cont. absorber
  - Prototype precooler
  - Helical Cooling Channel
  - Use for stopping muon beams
  - New technology



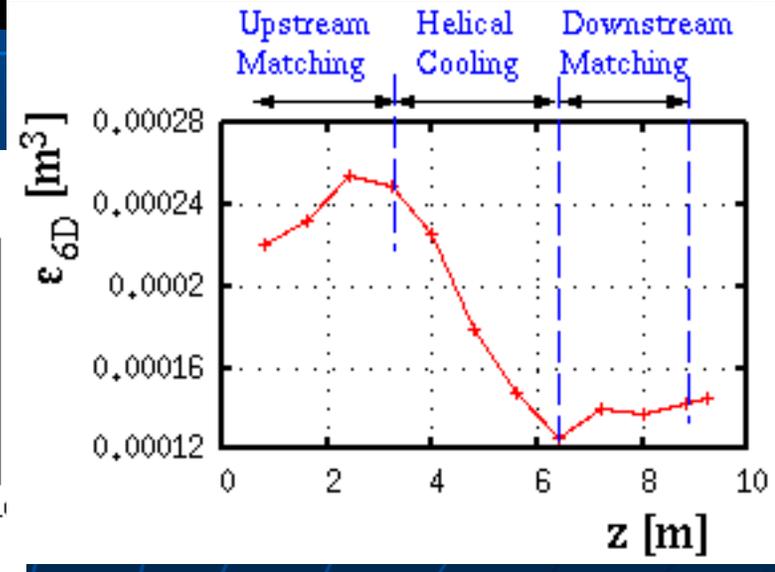
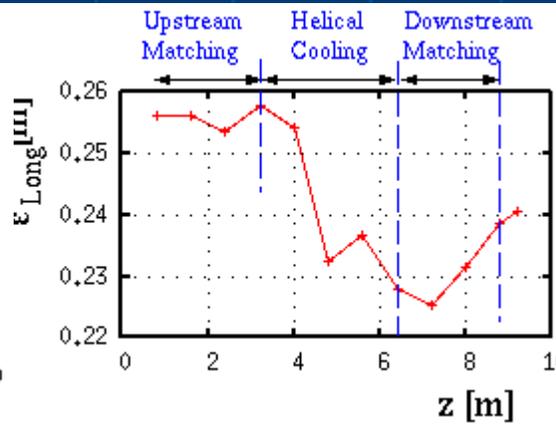
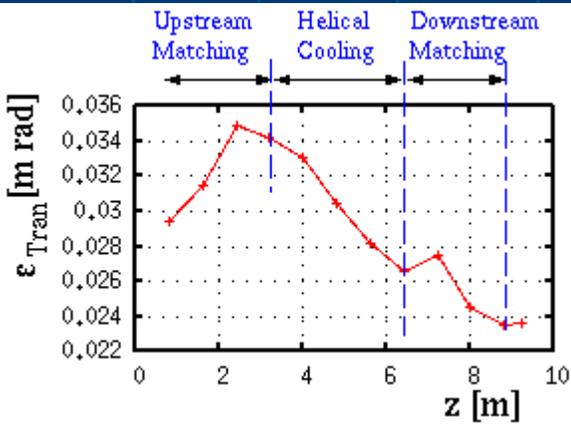
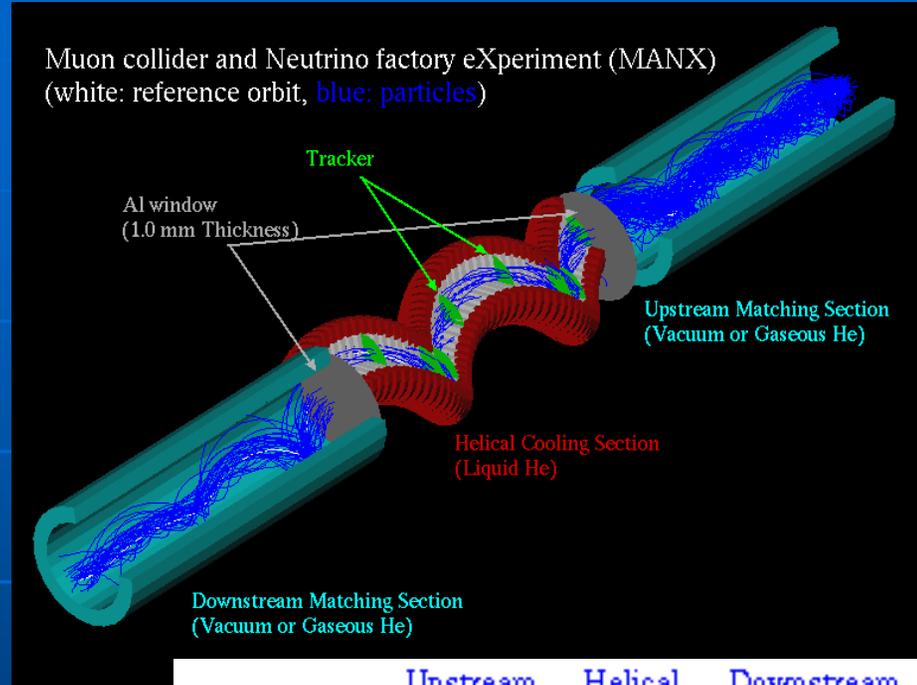
# Katsuya's Simulation study

## Initial beam profile

- Beam size (rms):  $\pm 60$  mm
- $\Delta p/p$  (rms):  $\pm 40/300$  MeV/c
- $x'$  and  $y'$  (rms):  $\pm 0.4$



- Obtained cooling factor:  $\sim 200\%$
- Transmission efficiency: 32%
- **But is matching necessary??!**





# Progress on new ideas described:

H<sub>2</sub>-Pressurized RF Cavities

Continuous Absorber for Emittance Exchange

Helical Cooling Channel

Parametric-resonance Ionization Cooling

Reverse Emittance Exchange

RF capture, phase rotation, cooling in HP RF Cavities

Bunch coalescing

Z-dependent HCC

MANX 6d Cooling Demo

(For other paths to LEMCs, see

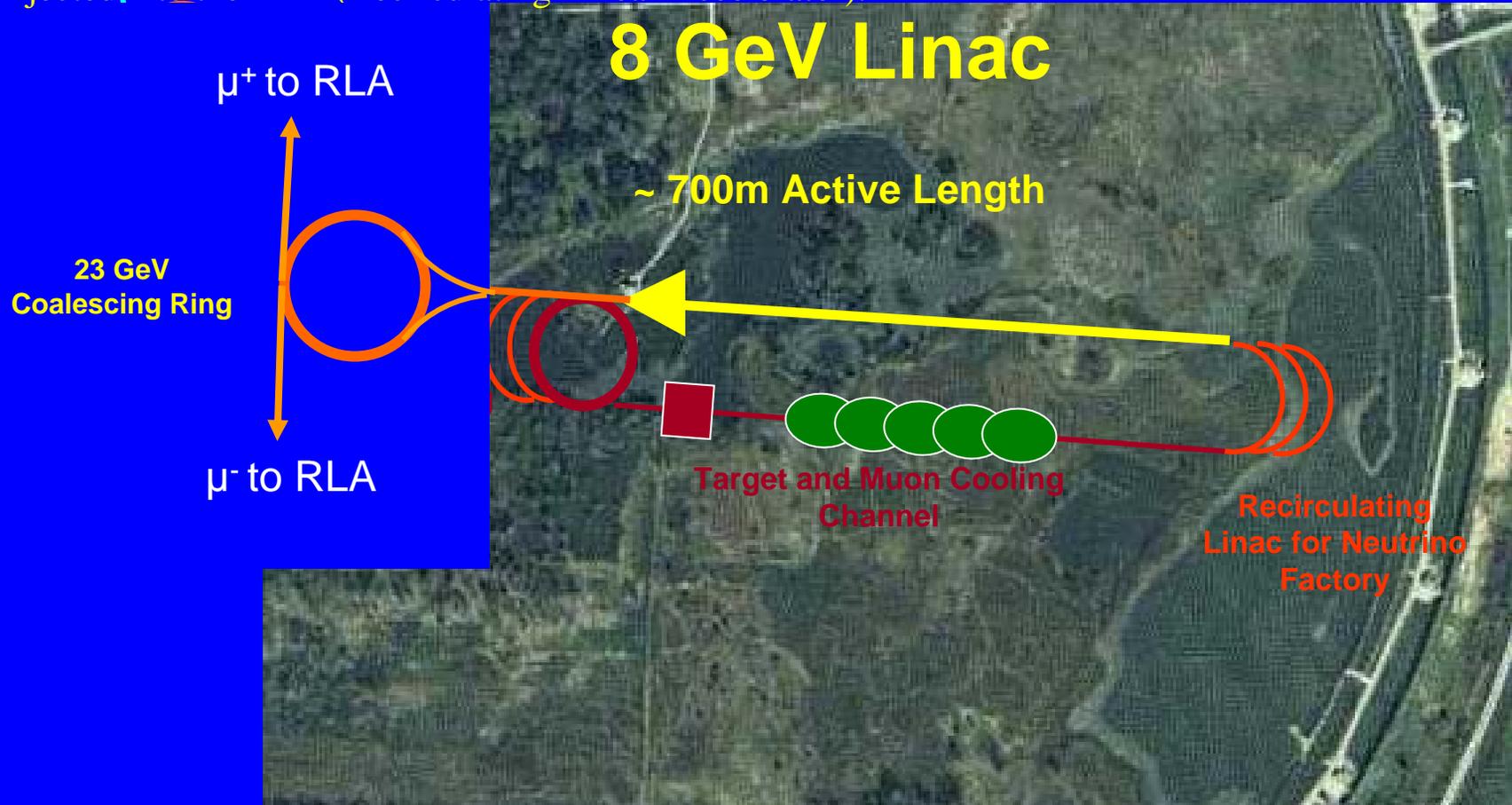
THPMS090 A Complete Scheme of Ionization Cooling for a Muon Collider, - Palmer et al., and

THPMS082 Muon Acceleration to 750 GeV in the Fermilab Tevatron Tunnel for a 1.5 TeV mu+ mu- Collider - Summers et al.)



# Muon Collider use of 8 GeV SC Linac

Instead of a 23 GeV neutrino decay racetrack, we need a 23 GeV Coalescing Ring. Coalescing done in 50 turns (~1.5% of muons lost by decay). 10 batches of  $10 \times 1.6 \times 10^{10}$  muons/bunch become 10 bunches of  $1.6 \times 10^{11}$ /bunch. Plus and minus muons are coalesced simultaneously. Then 10 bunches of each sign get injected into the RLA (Recirculating Linear Accelerator).





5 TeV ~ SSC energy reach

~5 X 2.5 km footprint

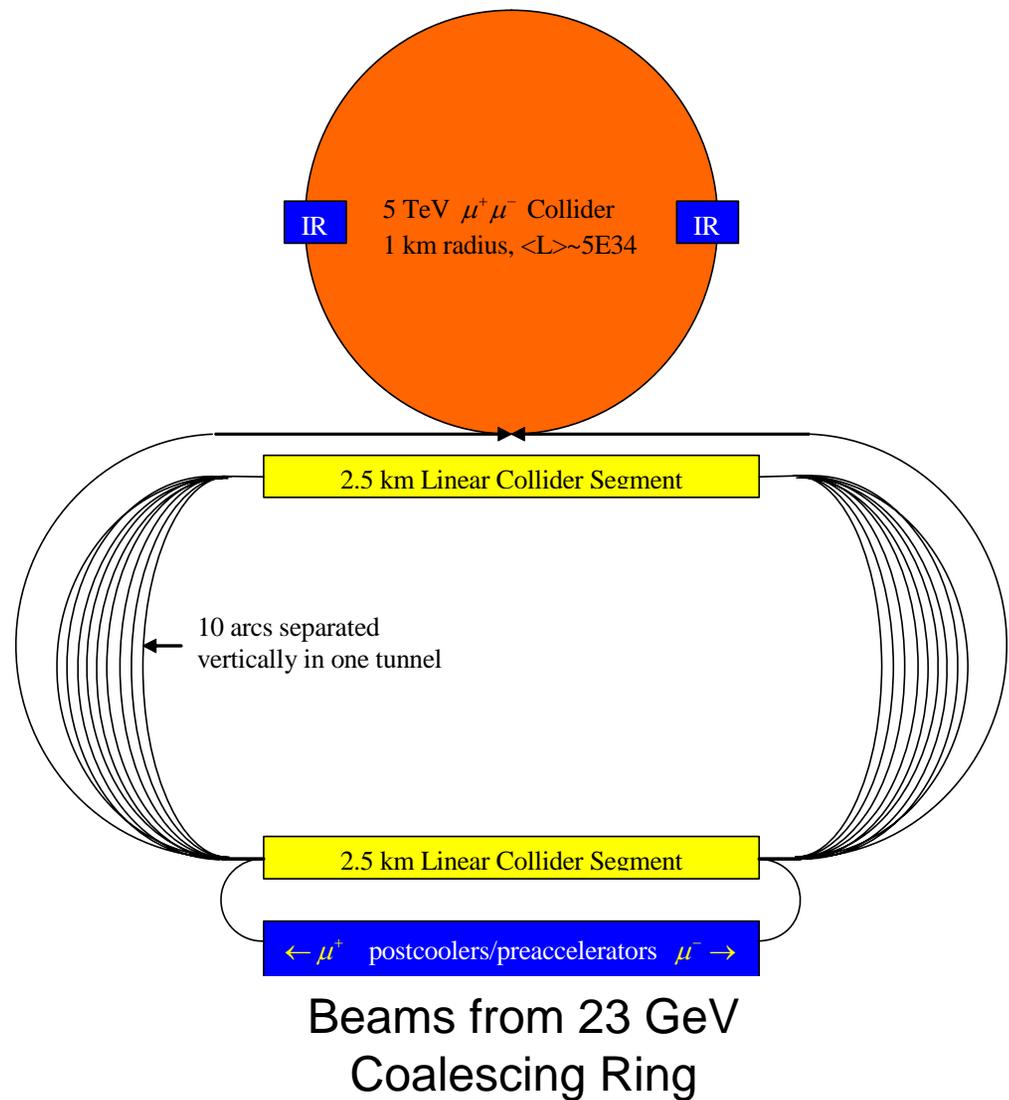
Affordable LC length (half of baseline 500 GeV ILC), includes ILC people, ideas

More efficient use of RF: recirculation and both signs

High L from small emittance!

1/10 fewer muons than originally imagined:

- a) easier p driver, targetry
- b) less detector background
- c) less site boundary radiation





# Muon Collider Emittances and Luminosities

• After:	$\epsilon_N$ tr	$\epsilon_N$ long.
– Precooling	20,000 $\mu\text{m}$	10,000 $\mu\text{m}$
– Basic HCC 6D	200 $\mu\text{m}$	100 $\mu\text{m}$
– Parametric-resonance IC	25 $\mu\text{m}$	100 $\mu\text{m}$
– Reverse Emittance Exchange	2 $\mu\text{m}$	2 cm

At 2.5 TeV on 2.5 TeV

$$L_{peak} = \frac{N_1 n \Delta v}{\beta^* r_\mu} f_0 \gamma = 10^{35} / \text{cm}^2 - \text{s}$$

$$\gamma \approx 2.5 \times 10^4 \quad n = 10$$

$$f_0 = 50 \text{kHz} \quad N_1 = 10^{11} \mu^-$$

$$\Delta v = 0.06 \quad \beta^* = 0.5 \text{cm}$$

$$\sigma_z = 3 \text{mm} \quad \Delta\gamma / \gamma = 3 \times 10^{-4}$$

$$\tau_\mu \approx 50 \text{ms} \Rightarrow 2500 \text{turns} / \tau_\mu$$

20 Hz Operation:

$$\langle L \rangle \approx 4.3 \times 10^{34} / \text{cm}^2 - \text{s}$$

$$Power = (26 \times 10^9)(6.6 \times 10^{13})(1.6 \times 10^{-19}) = 0.3 \text{MW}$$

$$0.3 \mu^+ / p$$



# Benefits of low emittance approach

Lower emittance allows lower muon current for a given luminosity.

This diminishes several problems:

- radiation levels due to the high energy neutrinos from muon beams circulating and decaying in the collider that interact in the earth near the site boundary;
- electrons from the same decays that cause background in the experimental detectors and heating of the cryogenic magnets;
- difficulty in creating a proton driver that can produce enough protons to create the muons;
- proton target heat deposition and radiation levels;
- heating of the ionization cooling energy absorber; and
- beam loading and wake field effects in the accelerating RF cavities.

Smaller emittance also:

- allows smaller, higher-frequency RF cavities with higher gradient for acceleration;
- makes beam transport easier; and
- allows stronger focusing at the interaction point since that is limited by the beam extension in the quadrupole magnets of the low beta insertion.

**See the LEMC Workshop web page. And please  
come to the next workshop in February, 2008!**



# Low Emittance Muon Collider

## Next Steps: we are getting close!

- A detailed plan for at least one complete cooling scheme with end-to-end simulations of a 1.5 TeV com MC,
- Advances in new technologies; e.g. an MTA beamline for HPRF tests, HTS for deep cooling, HCC magnet design
- And a really good 6D cooling demonstration experiment proposed to Fermilab



# High-Energy High-Luminosity Muon Colliders

- Are precision lepton machines at the energy frontier
- Are possible and affordable with new inventions and new technology
- Can take advantage of ILC advances
- Can be achieved in physics-motivated stages
- Require more effort from DPB and DPF communities
  - Please join in!